



# Fundamentals of Microelectronics

## الکترونیک ۲

### فصل ۸ – تقویت کننده عملیاتی (آپ امپ)

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دانشگاه بلوچستان

## Chapter 8 Operational Amplifier as A Black Box

- **8.1 General Considerations**
- **8.2 Op-Amp-Based Circuits**
- **8.3 Nonlinear Functions**
- **8.4 Op-Amp Nonidealities**
- **8.5 Design Examples**

# Chapter Outline

## General Concepts

- Op Amp Properties

## Linear Op Amp Circuits

- Noninverting Amplifier
- Inverting Amplifier
- Integrator and Differentiator
- Voltage Added

## Nonlinear Op Amp Circuits

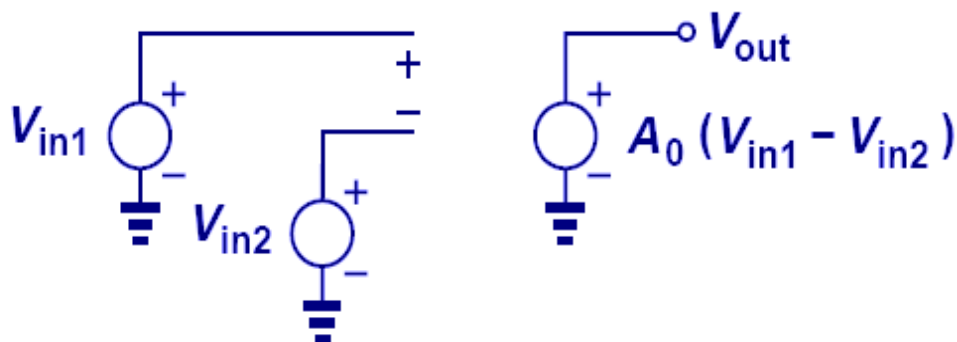
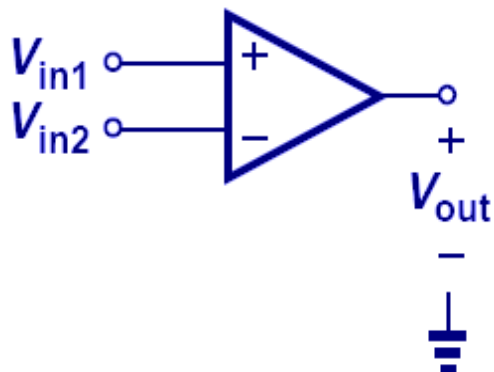
- Precision Rectifier
- Logarithmic Amplifier
- Square Root Circuit

## Op Amp Nonidealities

- DC Offsets
- Input Bias Currents
- Speed Limitations
- Finite Input and Output Impedances



# Basic Op Amp



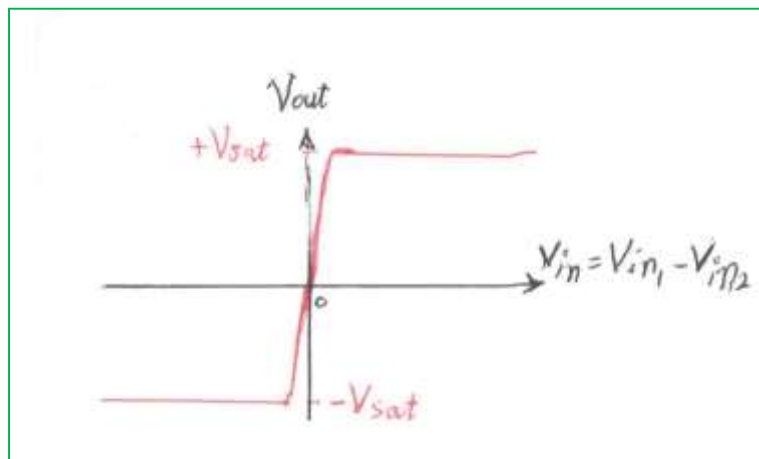
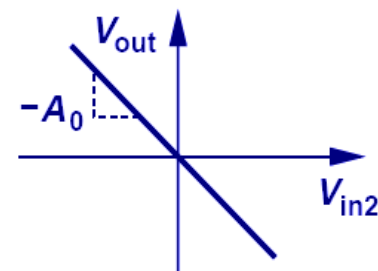
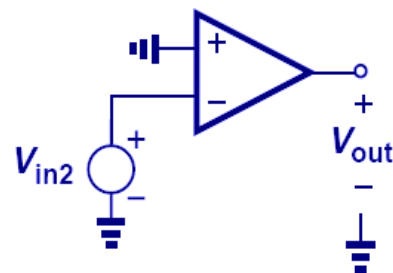
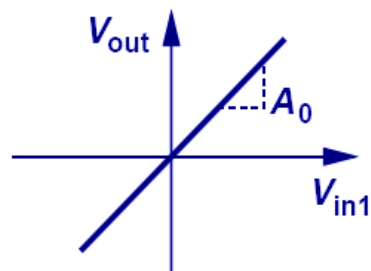
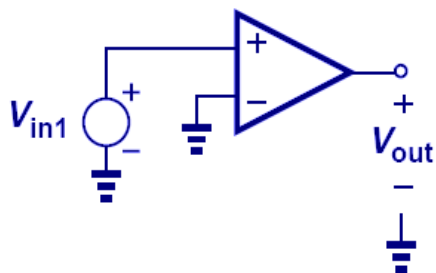
$$V_{out} = A_0 (V_{in1} - V_{in2})$$

- Op amp is a circuit that has two inputs and one output.
- It amplifies the difference between the two inputs.



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# Inverting and Non-inverting Op Amp

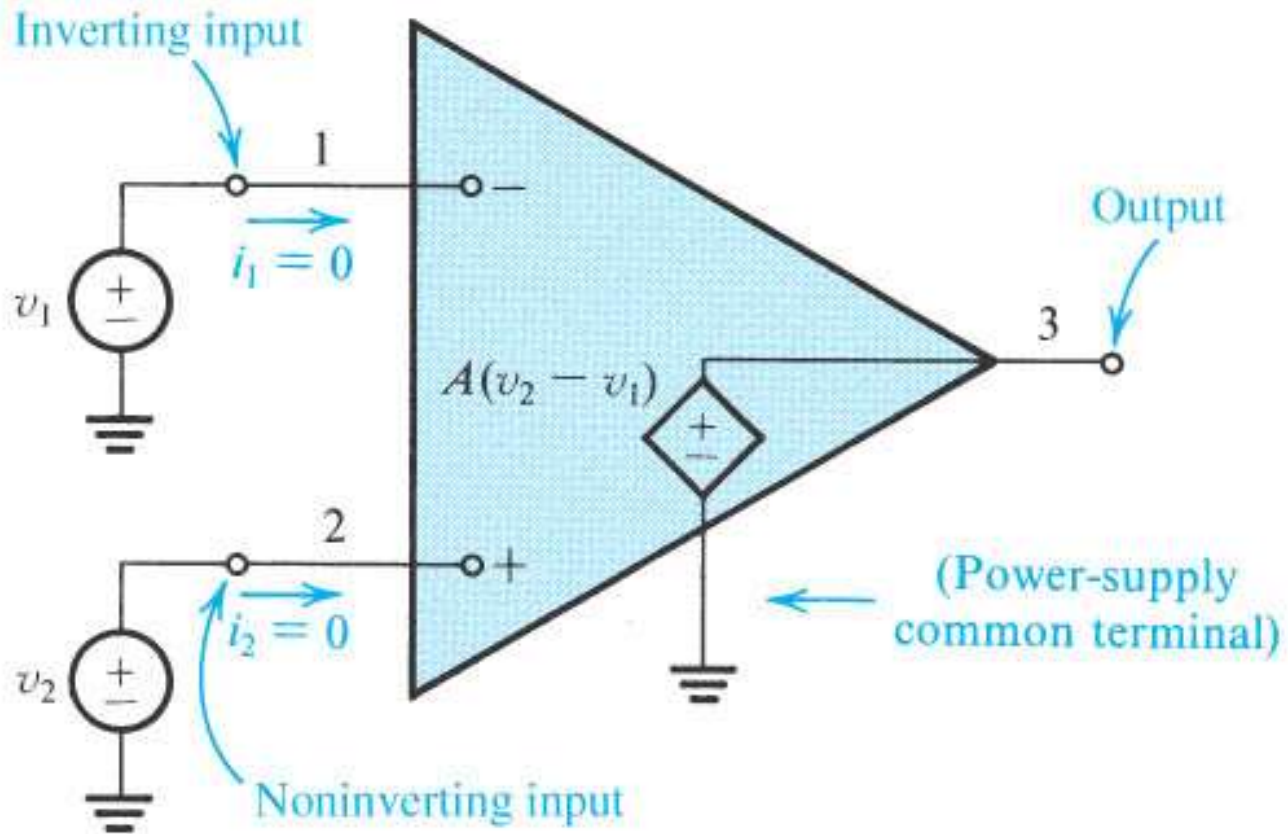


- If the negative input is grounded, the gain is positive.
- If the positive input is grounded, the gain is negative.

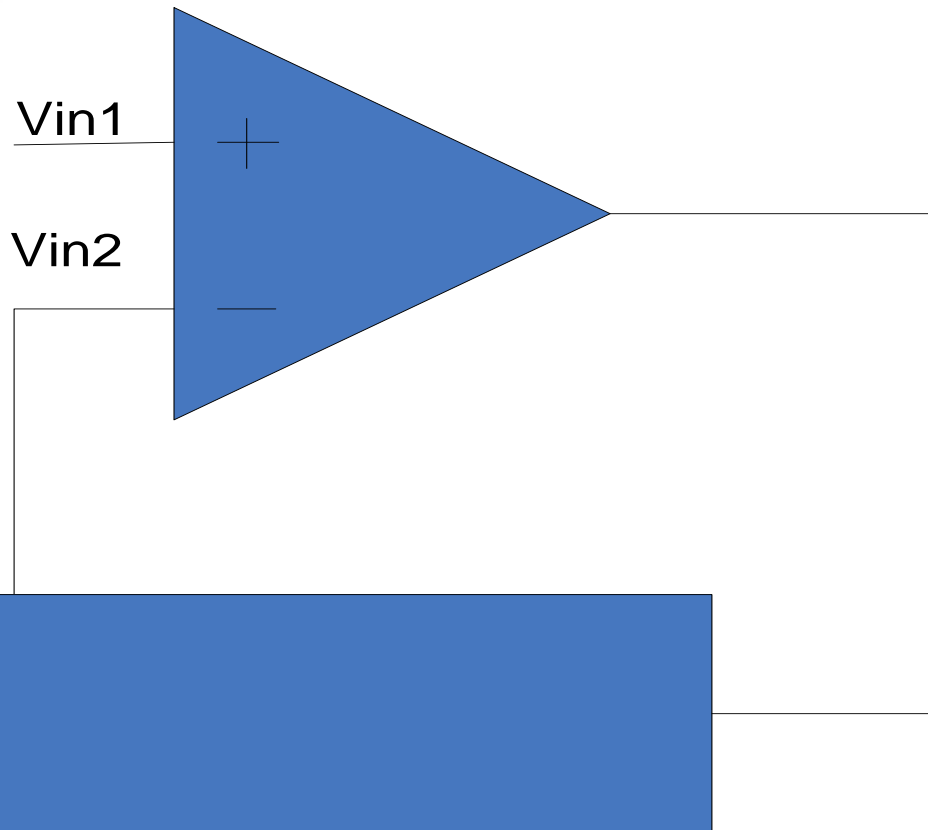
# Ideal Op Amp

- **Infinite gain**
- **Infinite input impedance**
- **Zero output impedance**
- **Infinite speed**

# Ideal Op Amp



# Virtual Short



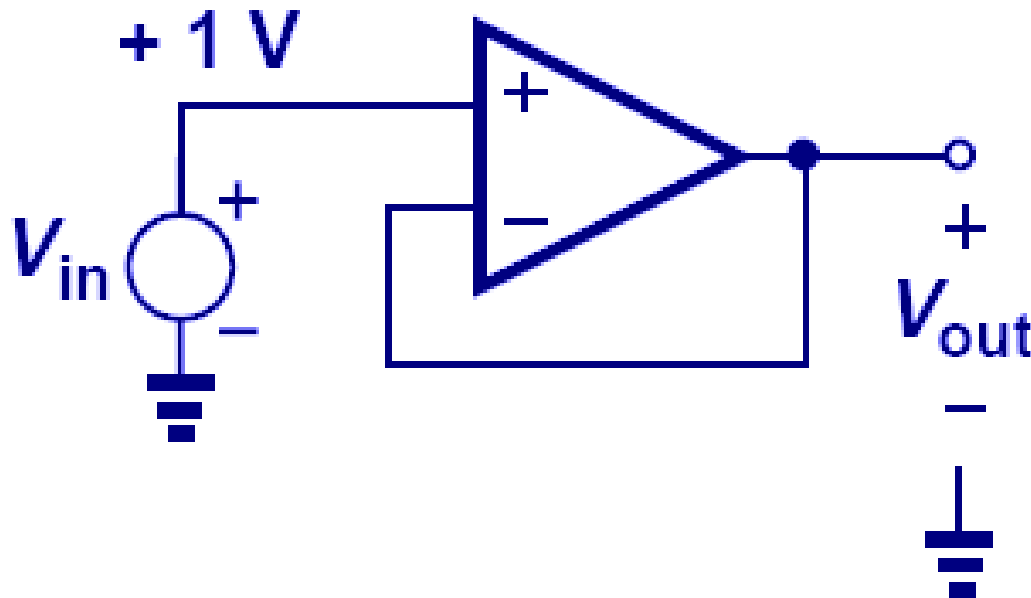
$$V^- \approx V^+$$

$$I_{in1} = I_{in2} \approx 0$$

➤ Due to infinite gain of op amp, the circuit forces  $V_{in2}$  to be close to  $V_{in1}$ , thus creating a virtual short.

# Unity Gain Amplifier

$$A_0 = 1000$$



$$V_{out} = A_0(V_{in1} - V_{in2})$$

$$= A_0(V_{in} - V_{out}).$$

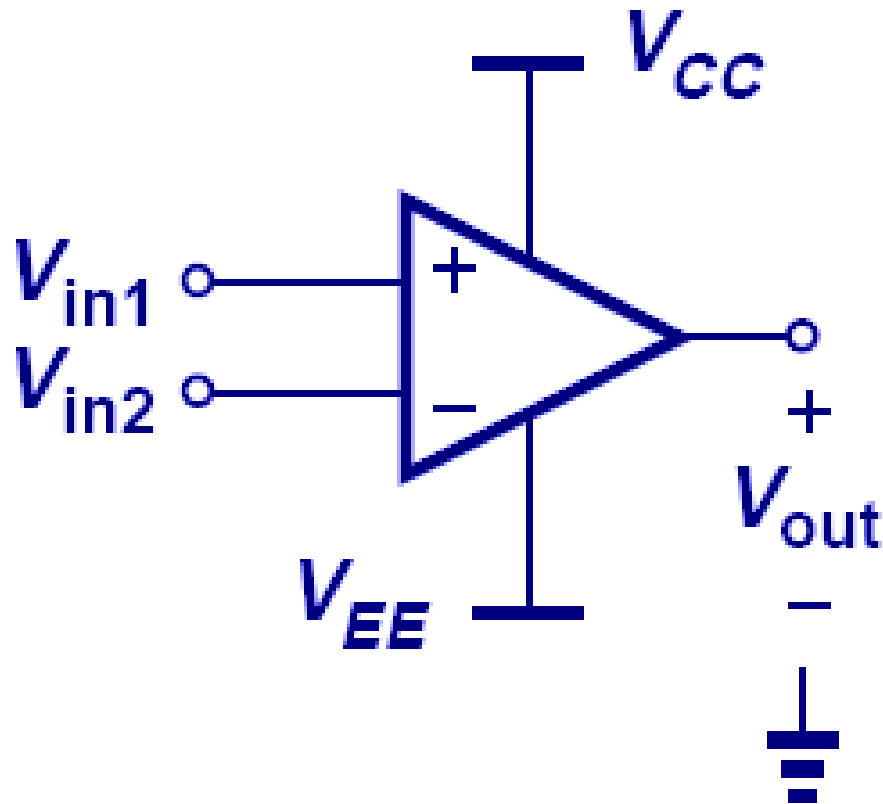
$$V_{out} = A_0(V_{in} - V_{out})$$

$$\frac{V_{out}}{V_{in}} = \frac{A_0}{1 + A_0}$$

$$A_0 = 1000,$$

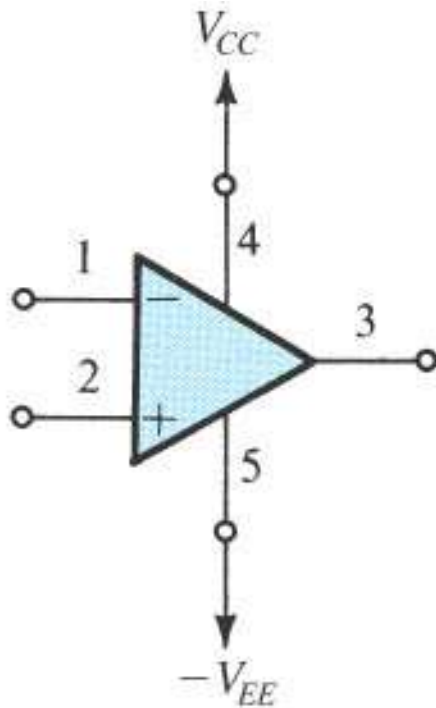
$$V_{in} = 1 \text{ V, and } V_{out} = 0.999 \text{ V.}$$

## Op Amp with Supply Rails

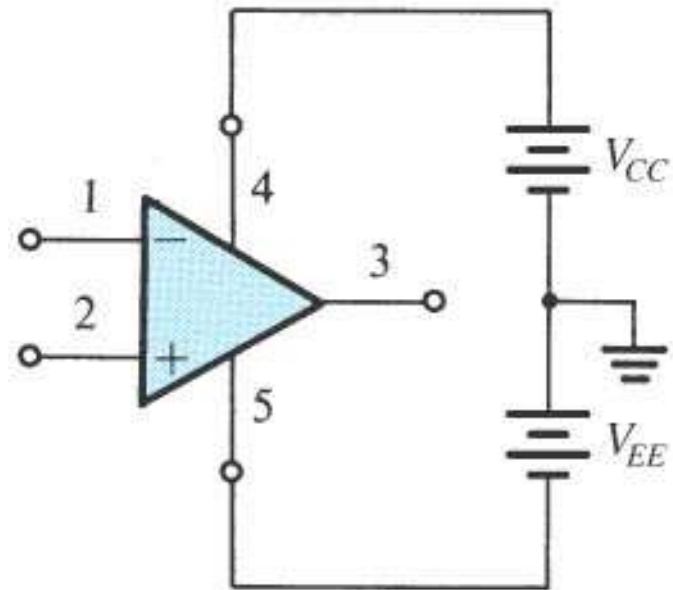


- To explicitly show the supply voltages,  $V_{CC}$  and  $V_{EE}$  are shown.
- In some cases,  $V_{EE}$  is zero.

# Op Amp with Supply Rail

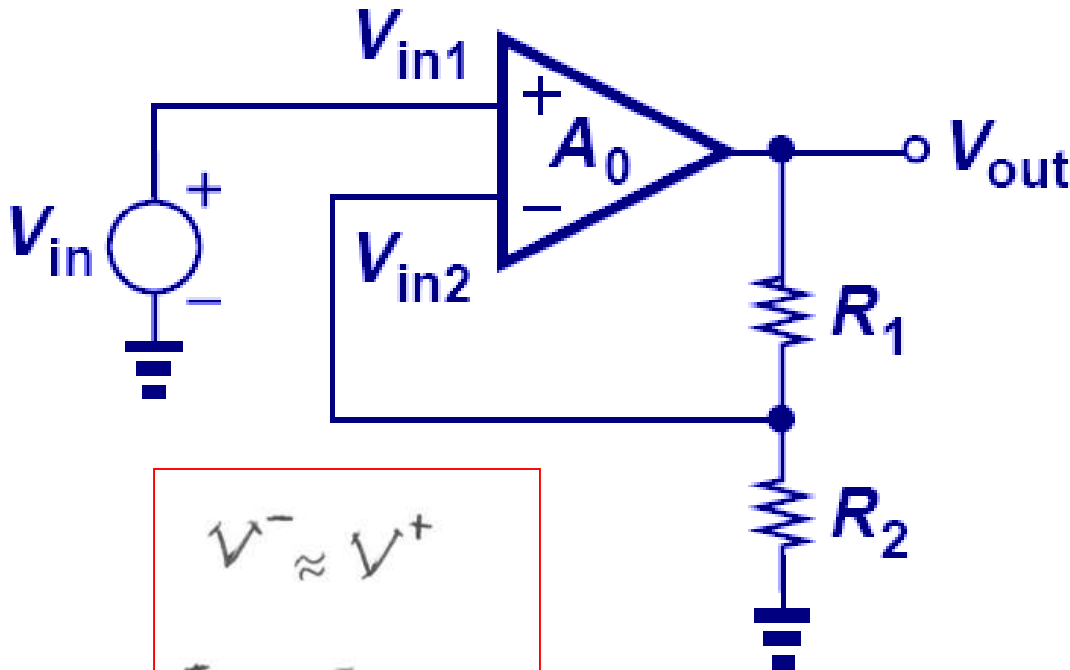


(a)



(b)

# Noninverting Amplifier (Infinite $A_0$ )



$$V_{in2} = \frac{R_2}{R_1 + R_2} V_{out}$$

$$V_{in1} \approx V_{in2}$$

$$\frac{V_{out}}{V_{in}} = 1 + \frac{R_1}{R_2}$$

$$V^- \approx V^+$$

$$I_{in1} = I_{in2} \approx 0$$

- A noninverting amplifier returns a fraction of output signal thru a resistor divider to the negative input.
- With a high  $A_0$ ,  $V_{out}/V_{in}$  depends only on ratio of resistors, which is very precise.

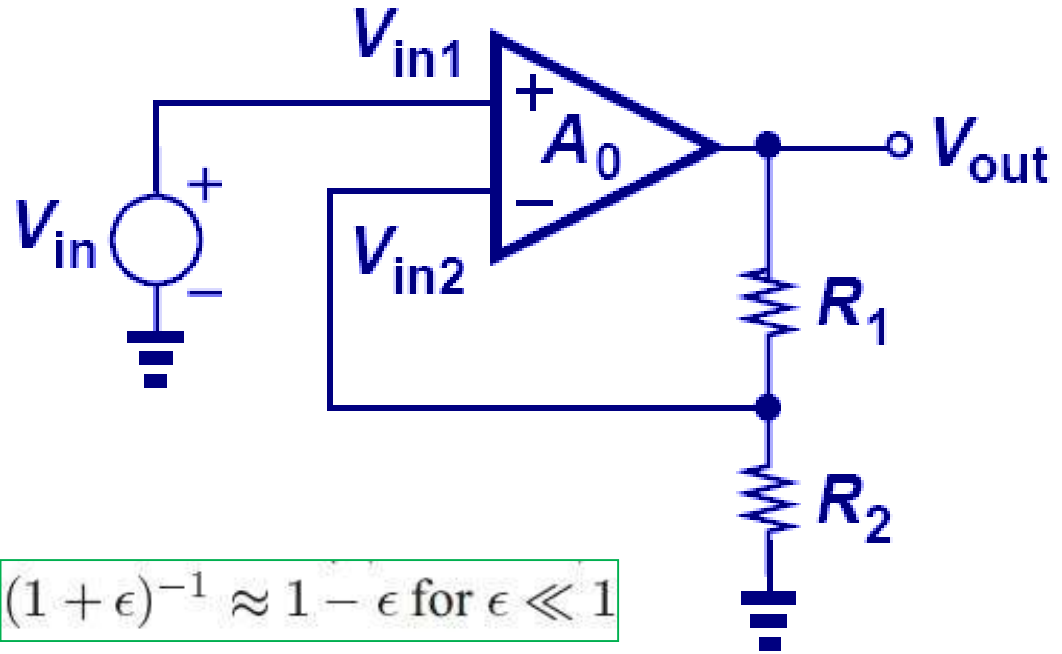
## Noninverting Amplifier (**Finite $A_0$** )

$$(V_{in1} - V_{in2})A_0 = V_{out}$$

$$\frac{V_{out}}{V_{in}} = \frac{A_0}{1 + \frac{R_2}{R_1 + R_2}A_0}$$

$$A_0 R_2 / (R_1 + R_2) \gg 1$$

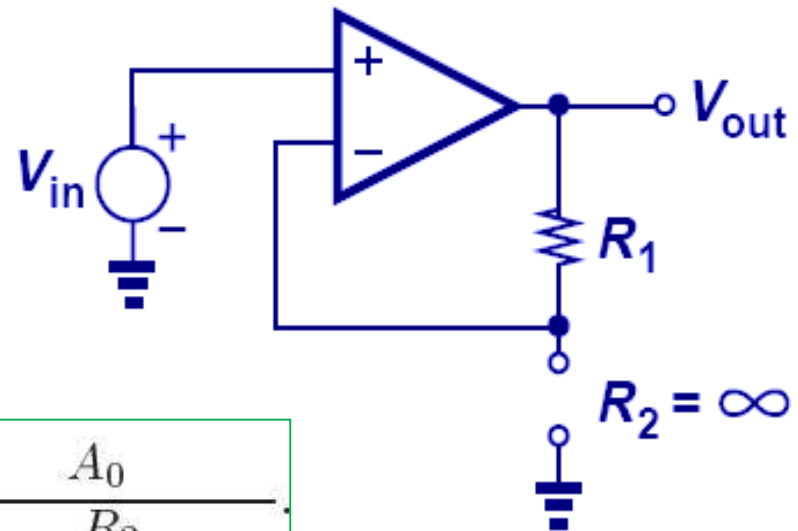
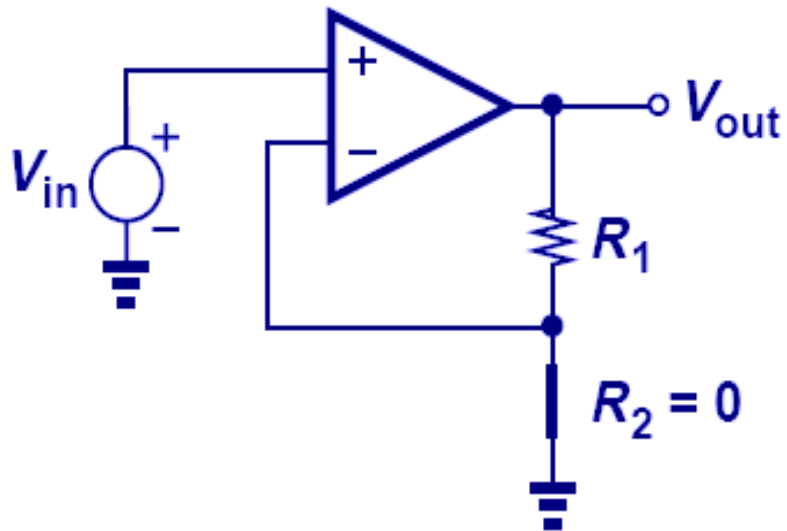
$$(1 + \epsilon)^{-1} \approx 1 - \epsilon \text{ for } \epsilon \ll 1$$



$$\frac{V_{out}}{V_{in}} \approx \left(1 + \frac{R_1}{R_2}\right) \left[1 - \left(1 + \frac{R_1}{R_2}\right) \frac{1}{A_0}\right]$$

➤ The error term indicates the larger the closed-loop gain, the less accurate the circuit becomes.

## Example 8.2: Extreme Cases of $R_2$ (Infinite $A_0$ )

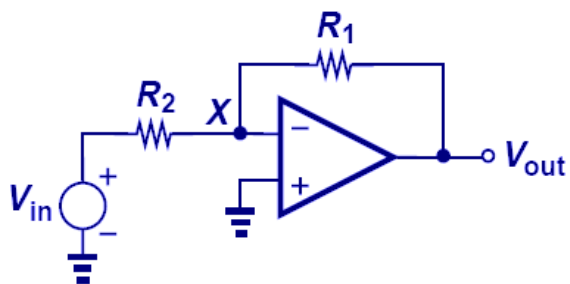


$$\frac{V_{out}}{V_{in}} = \frac{A_0}{1 + \frac{R_2}{R_1 + R_2} A_0}$$

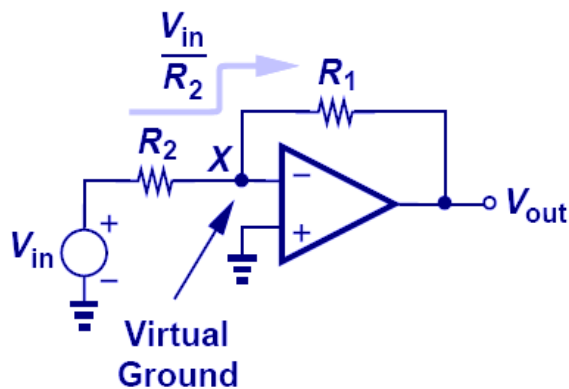
- If  $R_2$  is zero, the loop is open and  $V_{out}/V_{in}$  is equal to the intrinsic gain of the op amp.
- If  $R_2$  is infinite, the circuit becomes a unity-gain amplifier and  $V_{out}/V_{in}$  becomes equal to one.



# Inverting Amplifier

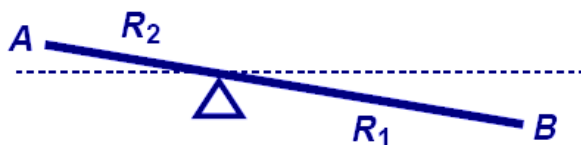


(a)



(b)

$$V^- \approx V^+$$
$$I_{in1} = I_{in2} \approx 0$$



(c)

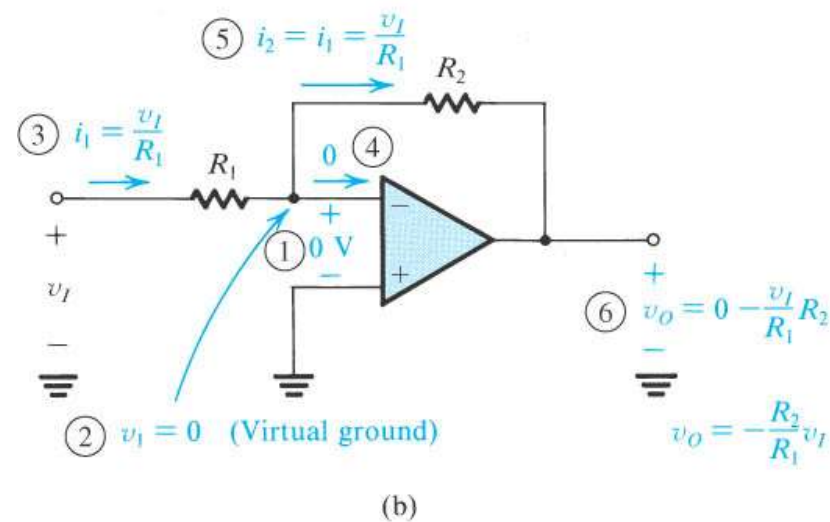
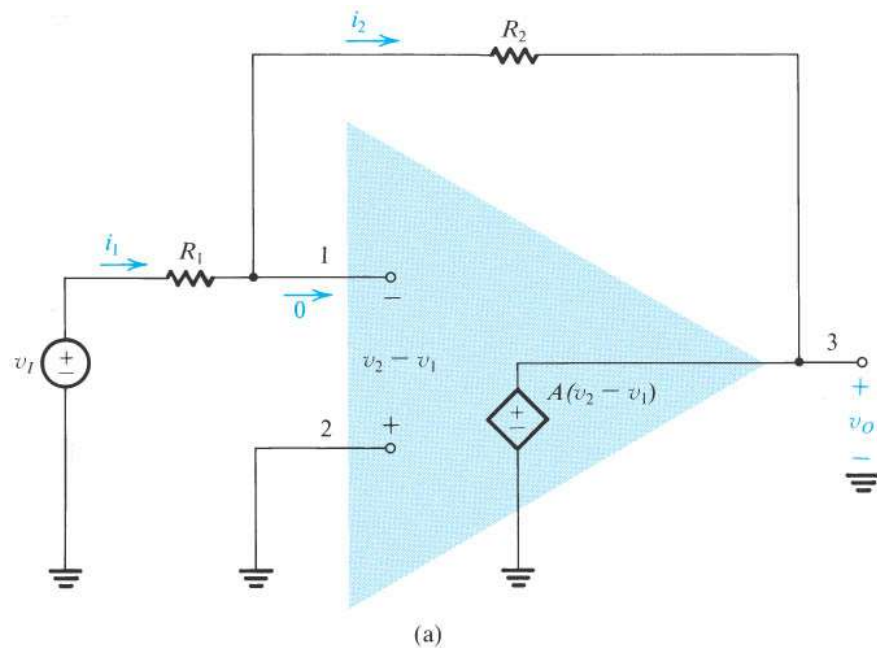
$$\frac{0 - V_{out}}{R_1} = \frac{V_{in}}{R_2}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_1}{R_2}$$

➤ Infinite  $A_0$  forces the negative input to be a virtual ground.



# Inverting Amplifier



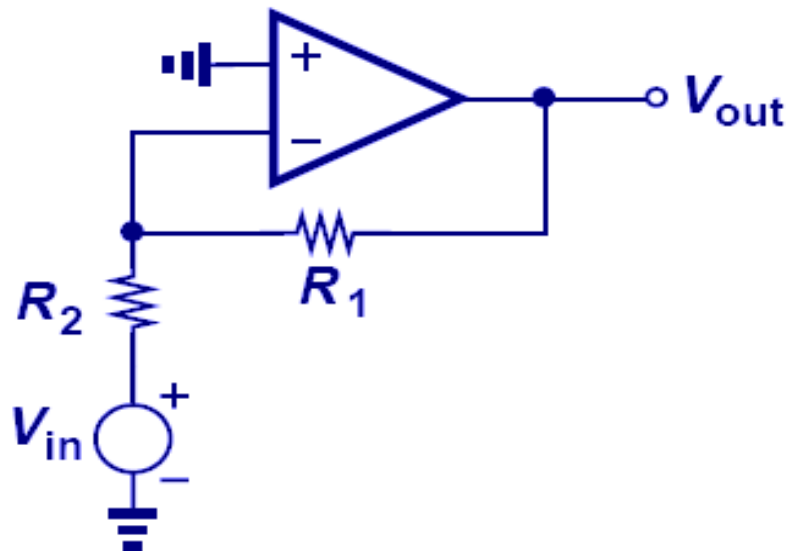
$$V^- \approx V^+$$

$$I_{in1} = I_{in2} \approx 0$$



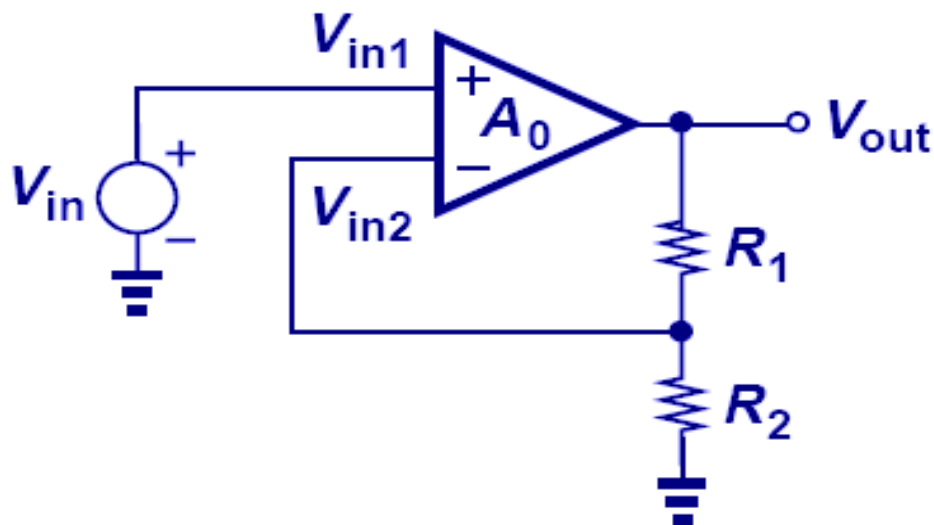
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## Another View of Inverting Amplifier



$$\frac{V_{out}}{V_{in}} = -\frac{R_1}{R_2}$$

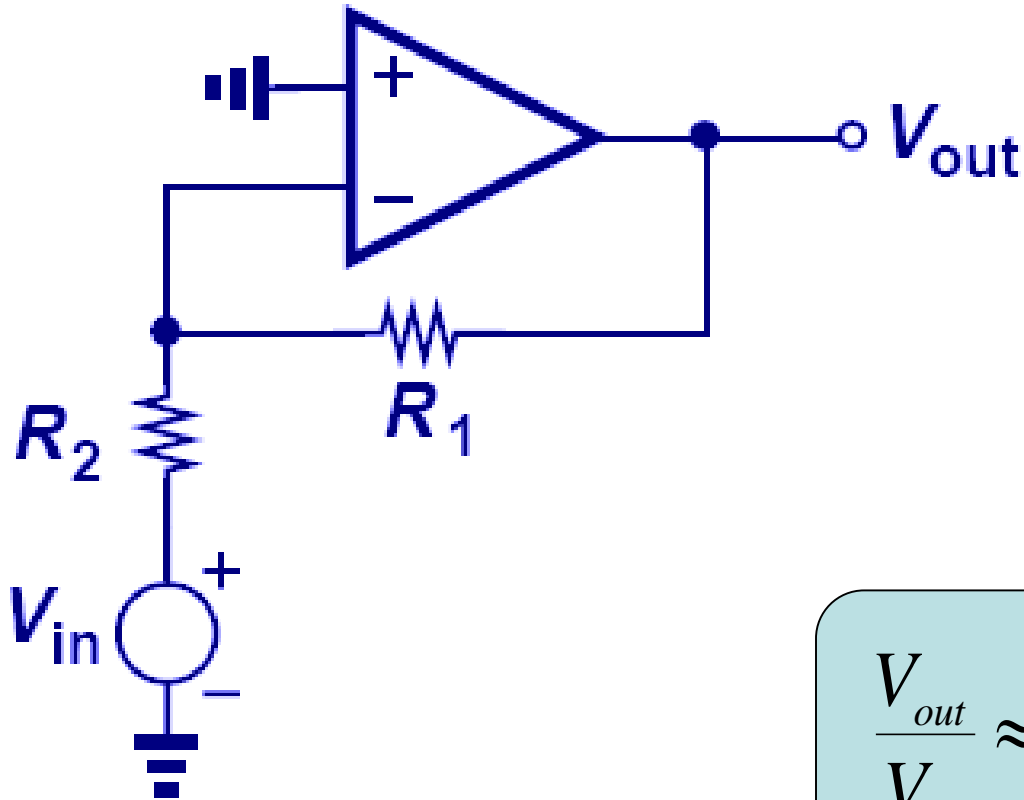
**Inverting**



$$\frac{V_{out}}{V_{in}} = 1 + \frac{R_1}{R_2}$$

**Noninverting**

## Gain Error Due to Finite $A_0$



$$V_{out} = A_0(V_{in1} - V_{in2})$$

$$= -A_0 V_X.$$

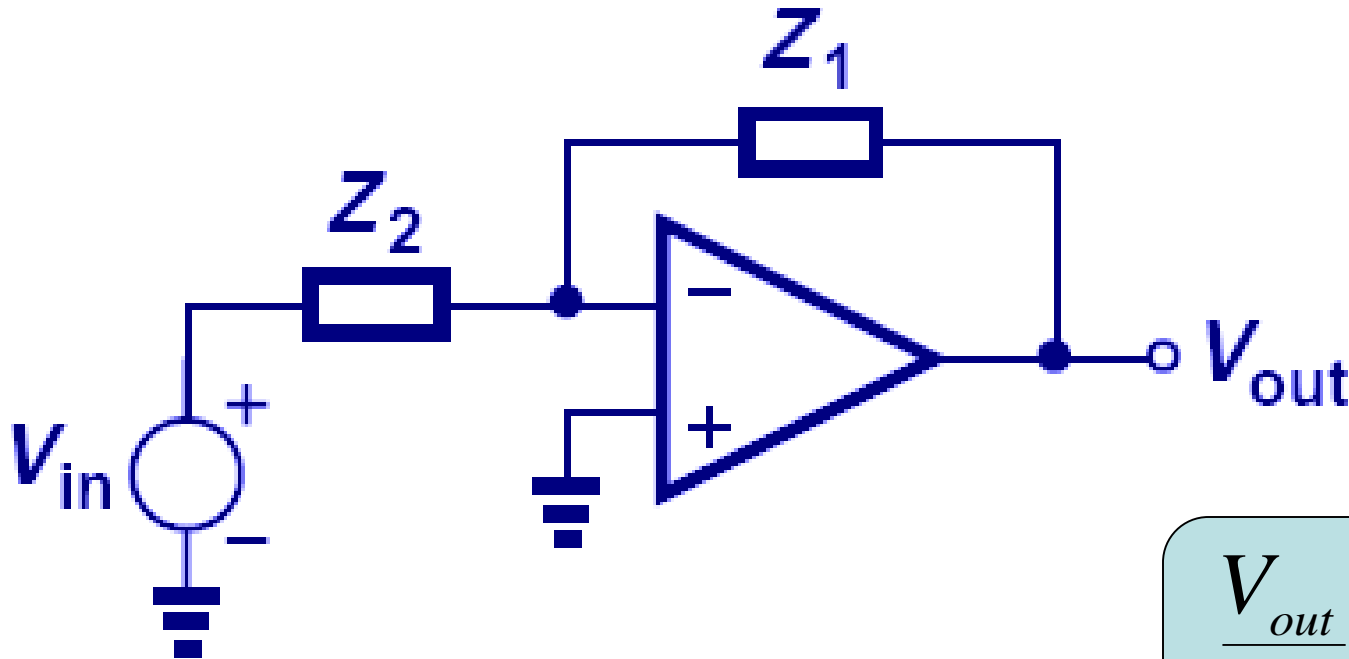
$$\frac{V_{out}}{V_{in}} = -\frac{1}{\frac{1}{A_0} + \frac{R_2}{R_1}\left(\frac{1}{A_0} + 1\right)}$$

$$= -\frac{1}{\frac{R_2}{R_1} + \frac{1}{A_0}\left(1 + \frac{R_2}{R_1}\right)}.$$

$$\frac{V_{out}}{V_{in}} \approx -\frac{R_1}{R_2} \left[ 1 - \frac{1}{A_0} \left( 1 + \frac{R_1}{R_2} \right) \right]$$

➤ The larger the closed loop gain, the more inaccurate the circuit is.

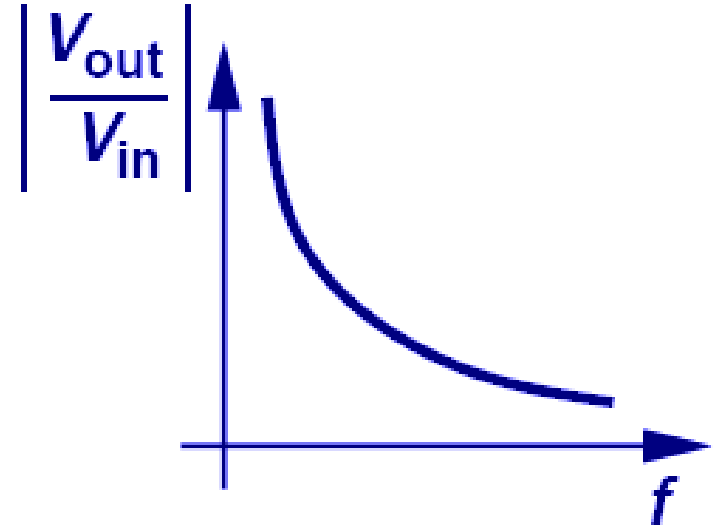
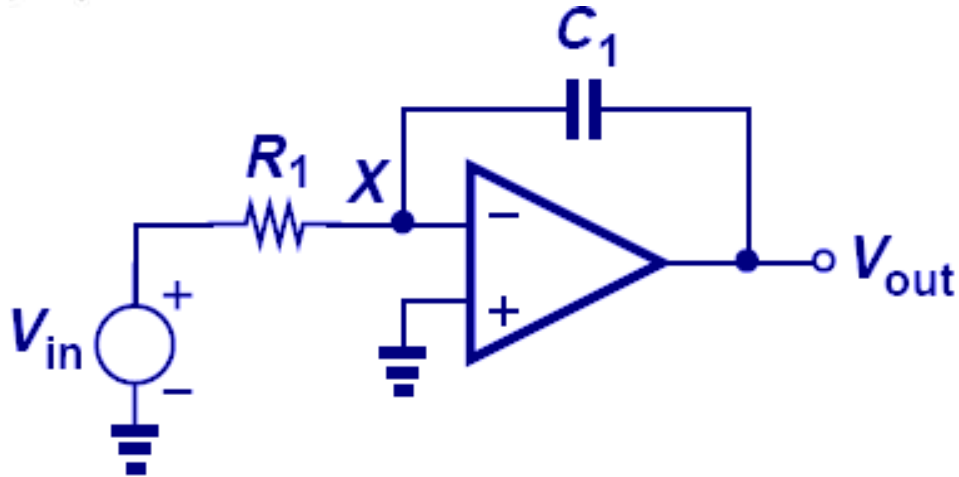
# Complex Impedances Around the Op Amp



$$\frac{V_{out}}{V_{in}} \approx -\frac{Z_1}{Z_2}$$

➤ The closed-loop gain is still equal to the ratio of two impedances.

# Integrator



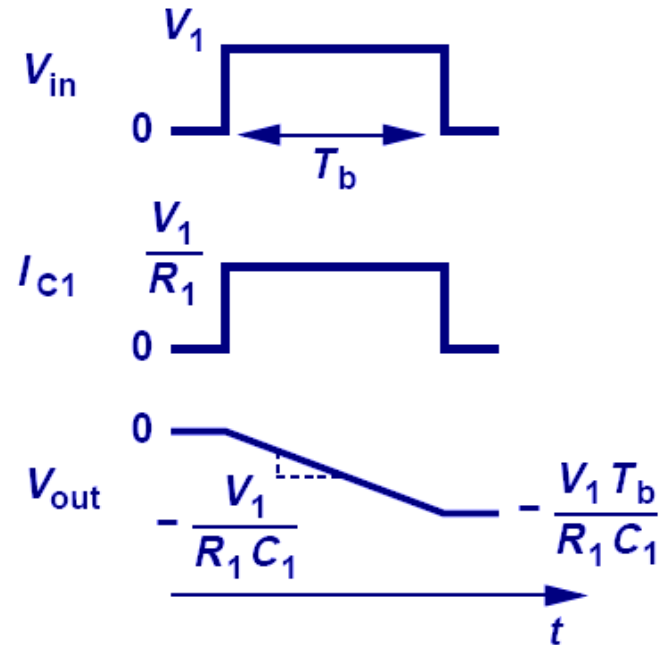
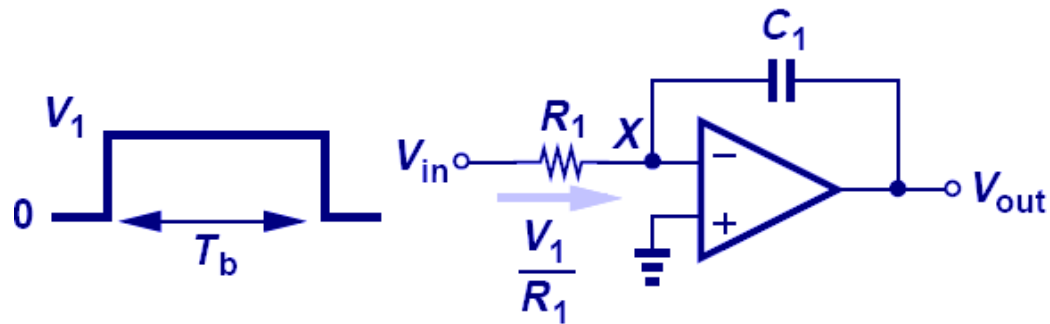
$$\frac{V_{out}}{V_{in}} = -\frac{1}{C_1 s R_1}$$

$$\frac{V_{in}}{R_1} = -C_1 \frac{dV_{out}}{dt}$$

$$\frac{V_{out}}{V_{in}} = -\frac{1}{R_1 C_1 s}$$

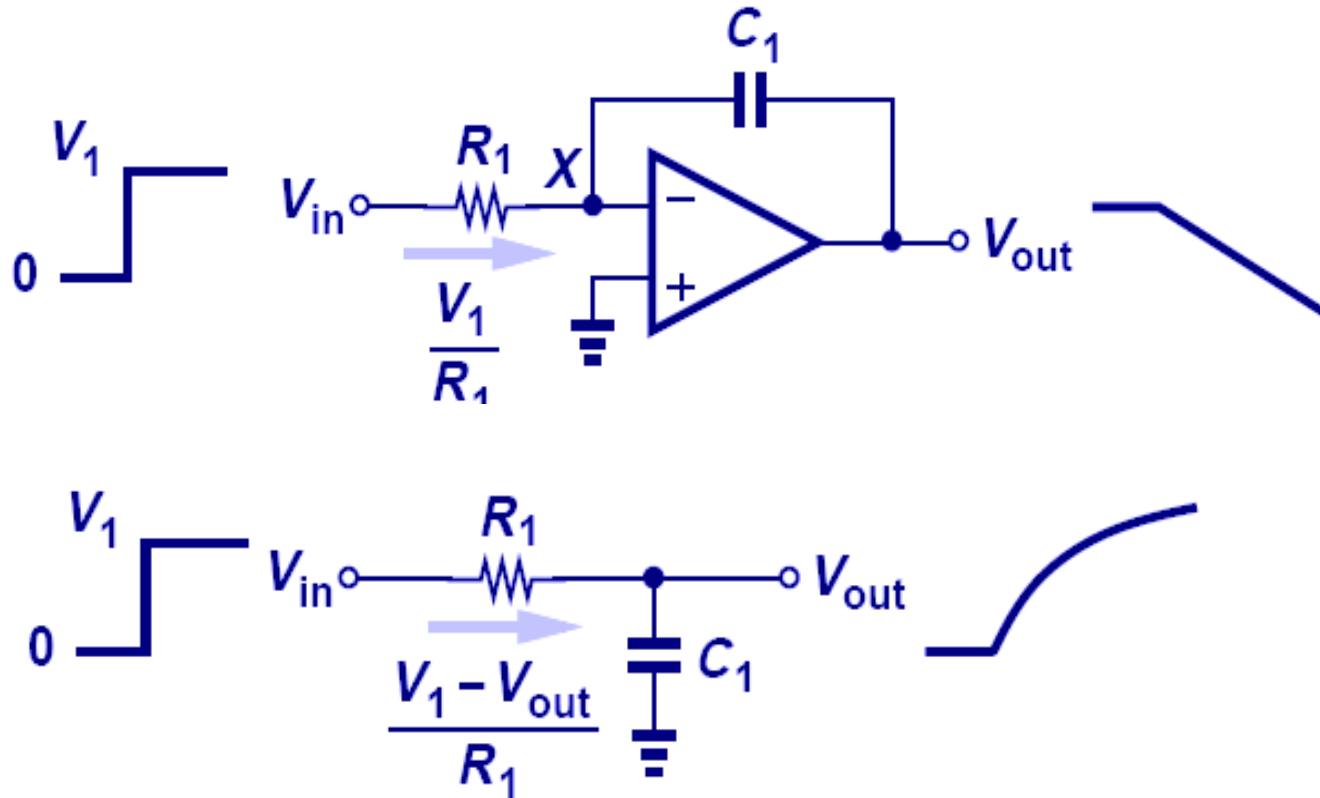
$$V_{out} = -\frac{1}{R_1 C_1} \int V_{in} dt$$

## Example 8.5: Integrator with Pulse Input



$$V_{out} = -\frac{1}{R_1 C_1} \int V_{in} dt = -\frac{V_1}{R_1 C_1} t \quad 0 < t < T_b$$

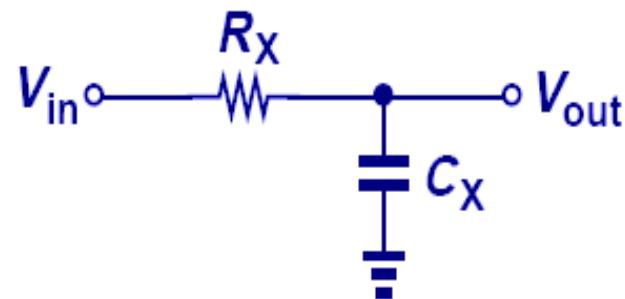
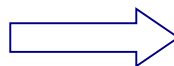
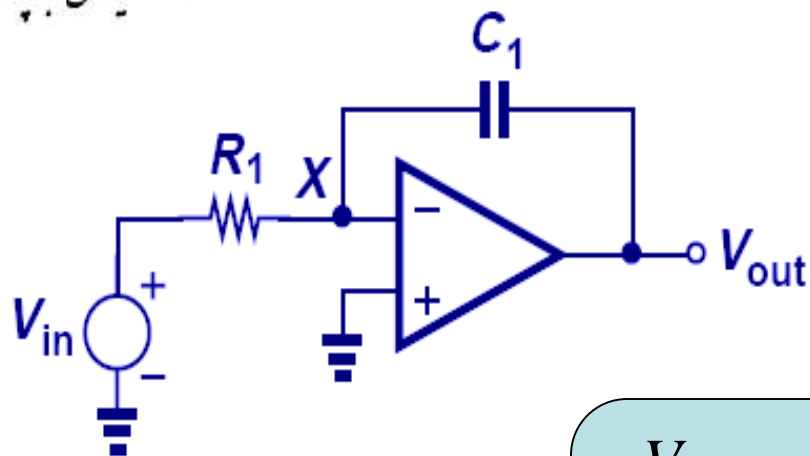
# Comparison of Integrator and RC Lowpass Filter



- The RC low-pass filter is actually a “passive” approximation to an integrator.
- With the RC time constant large enough, the RC filter output approaches a ramp.



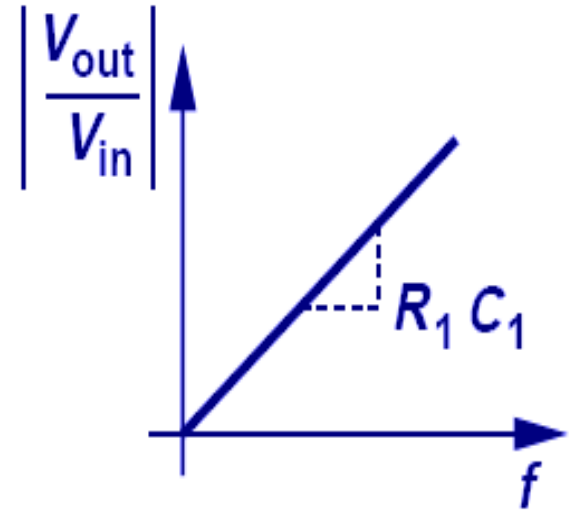
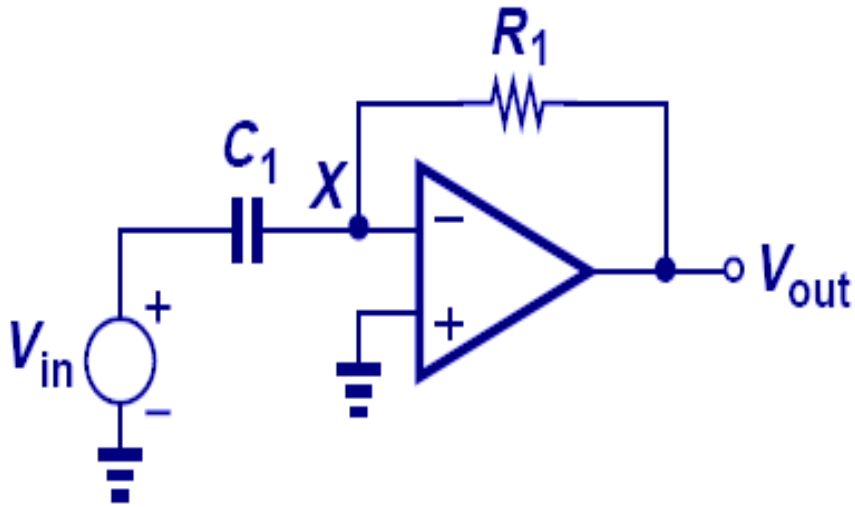
## Lossy Integrator



$$\frac{V_{out}}{V_{in}} = \frac{-1}{\frac{1}{A_0} + \left(1 + \frac{1}{A_0}\right) R_1 C_1 s}$$

- When finite op amp gain is considered, the integrator becomes lossy as the pole moves from the origin to  $-1/[(1+A_0)R_1C_1]$ .
- It can be approximated as an RC circuit with C boosted by a factor of  $A_0+1$ .

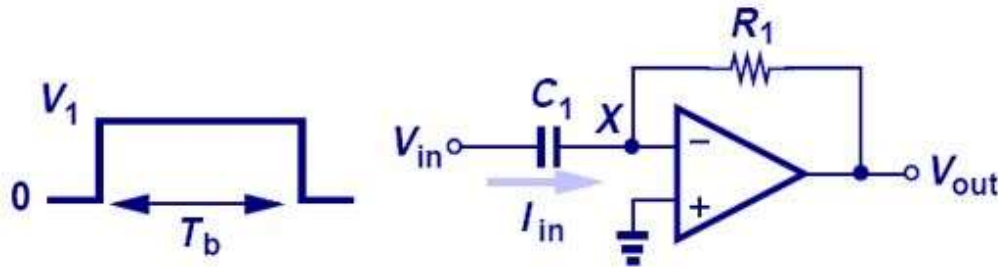
# Differentiator



$$V_{out} = -R_1 C_1 \frac{dV_{in}}{dt}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_1}{\frac{1}{C_1 s}} = -R_1 C_1 s$$

## Exaple 8.7: Differentiator with Pulse Input



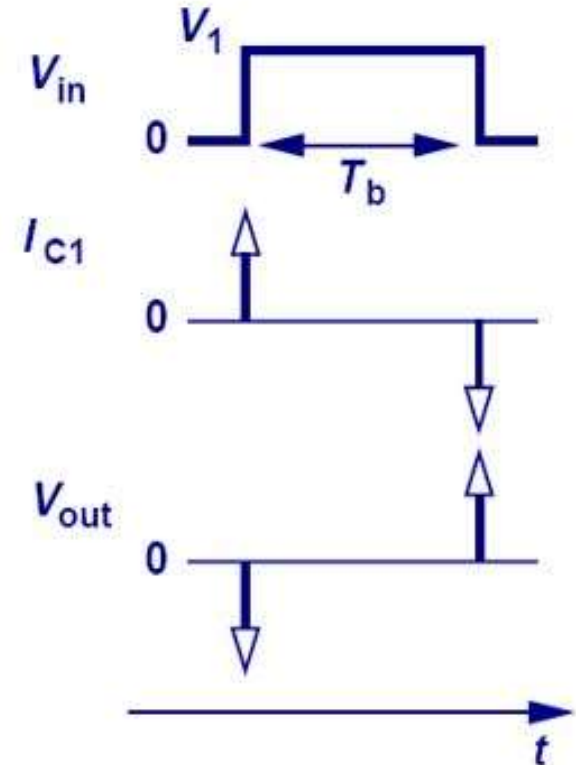
$$I_{in} = C_1 \frac{dV_{in}}{dt} = C_1 V_1 \delta(t).$$

$$\begin{aligned} V_{out} &= -I_{in} R_1 \\ &= -R_1 C_1 V_1 \delta(t). \end{aligned}$$

$$\begin{aligned} I_{in} &= C_1 \frac{dV_{in}}{dt} \\ &= C_1 V_1 \delta(t). \end{aligned}$$

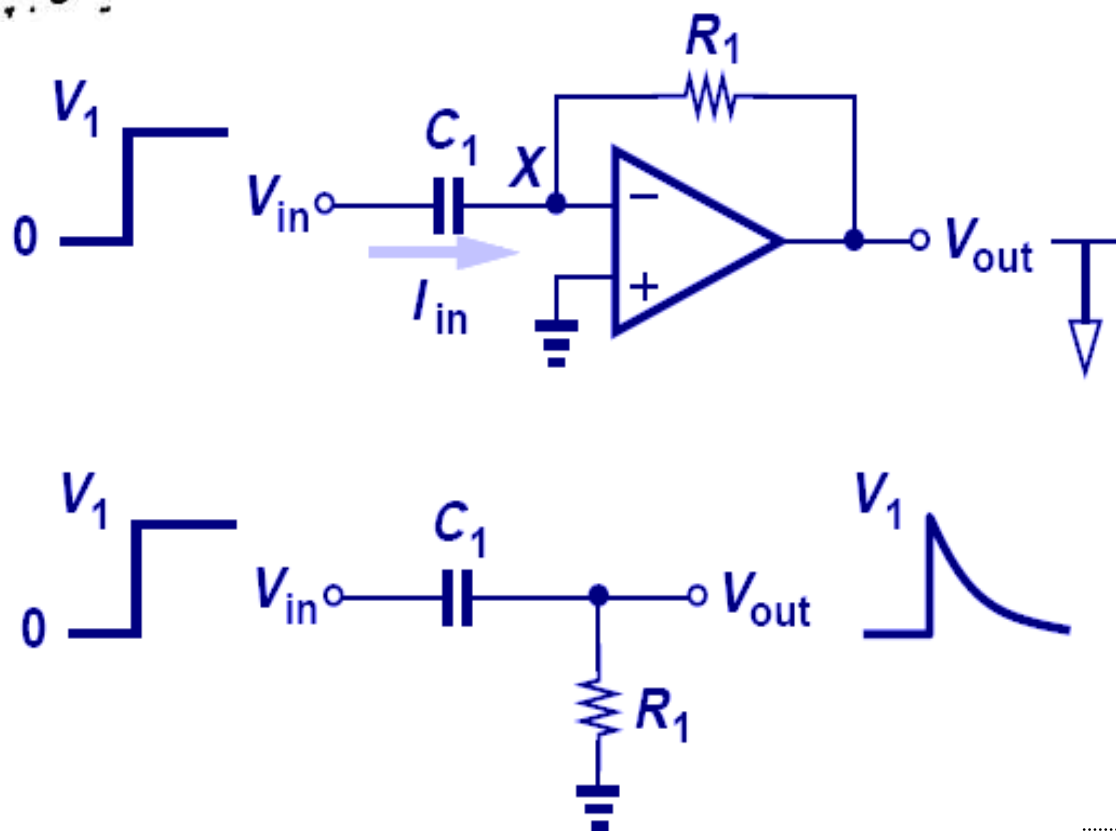
$$\begin{aligned} V_{out} &= -I_{in} R_1 \\ &= R_1 C_1 V_1 \delta(t). \end{aligned}$$

$$V_{out} = \mp R_1 C_1 V_1 \delta(t)$$





# Comparison of Differentiator and High-Pass Filter



$$\frac{V_{in} - V_X}{\frac{1}{C_1 s}} = \frac{V_X - V_{out}}{R_1}.$$

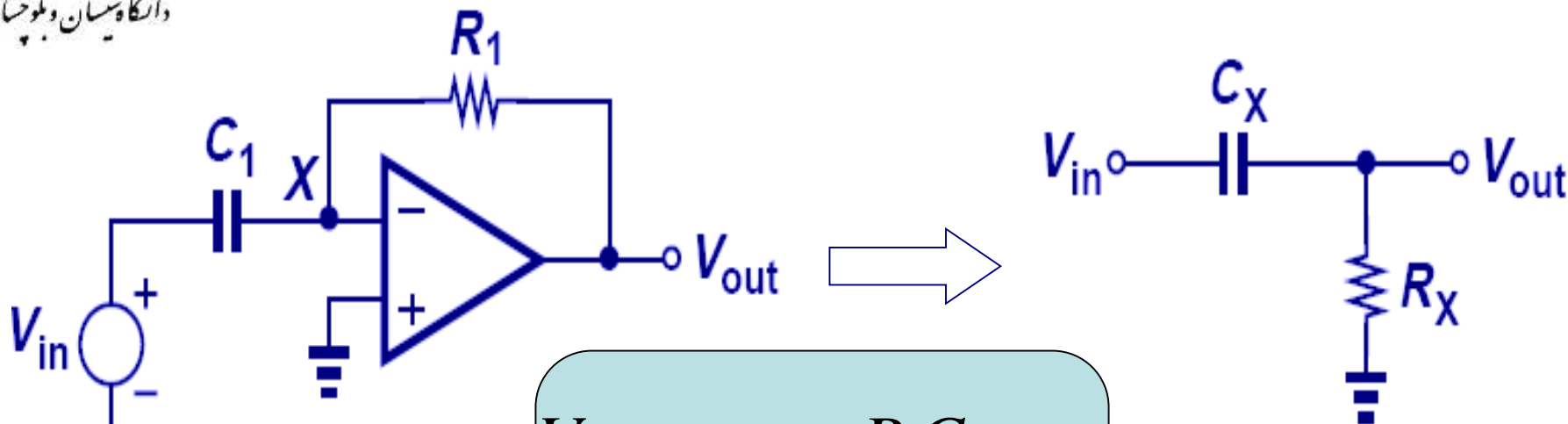
$$\frac{V_{out}}{V_{in}} = \frac{-R_1 C_1 s}{1 + \frac{1}{A_0} + \frac{R_1 C_1 s}{A_0}}.$$

$$s_p = -\frac{A_0 + 1}{R_1 C_1}.$$

- The RC high-pass filter is actually a passive approximation to the differentiator.
- When the RC time constant is small enough, the RC filter approximates a differentiator.



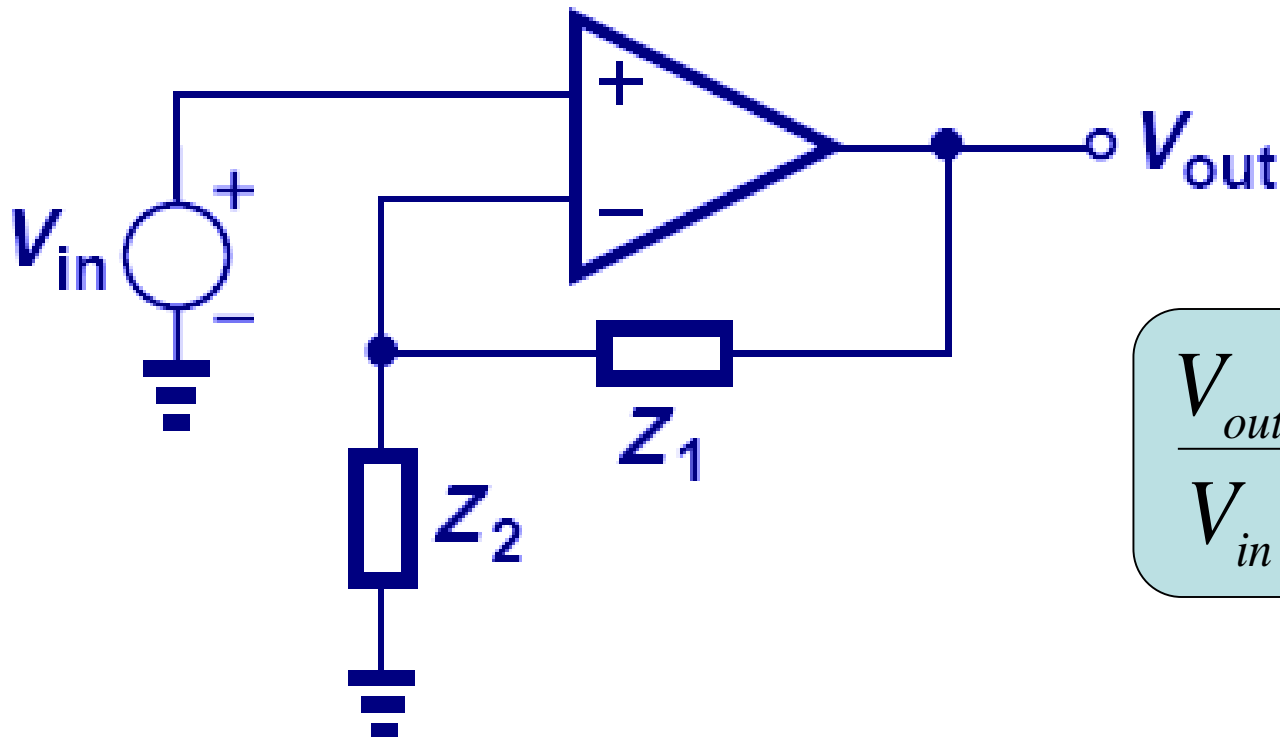
## Lossy Differentiator



$$\frac{V_{out}}{V_{in}} = \frac{-R_1 C_1 s}{1 + \frac{1}{A_0} + \frac{R_1 C_1 s}{A_0}}$$

- When finite op amp gain is considered, the differentiator becomes lossy as the zero moves from the origin to  $-(A_0+1)/R_1 C_1$ .
- It can be approximated as an RC circuit with R reduced by a factor of  $(A_0+1)$ .

# Op Amp with General Impedances

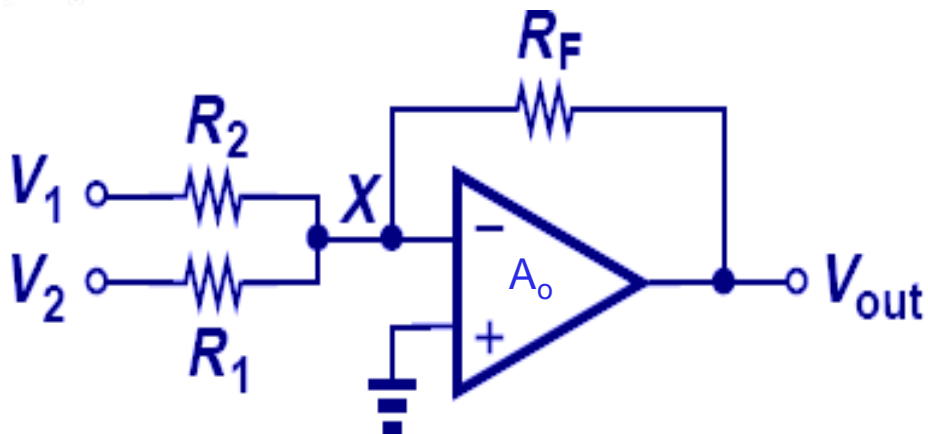


$$\frac{V_{out}}{V_{in}} = 1 + \frac{Z_1}{Z_2}$$

➤ This circuit cannot operate as ideal integrator or differentiator.



## Voltage Adder



$$V^- \approx V^+$$

$$I_{in1} = I_{in2} \approx 0$$

$$\frac{V_1}{R_1} + \frac{V_2}{R_2} = \frac{-V_{out}}{R_F}$$

$$V_{out} = -R_F \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} \right)$$

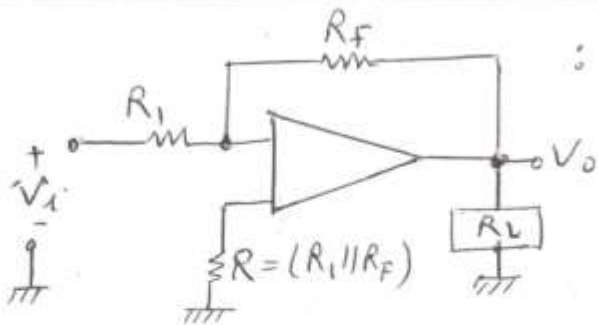
$$V_{out} = \frac{-R_F}{R} (V_1 + V_2)$$

$$\text{If } R_1 = R_2 = R$$

- If  $A_o$  is infinite, X is pinned at ground, currents proportional to  $V_1$  and  $V_2$  will flow to X and then across  $R_F$  to produce an output proportional to the sum of two voltages.

# بخش اول - کاربردهای « تقویت کننده عملیاتی » - وارونگر - غیر وارونگر

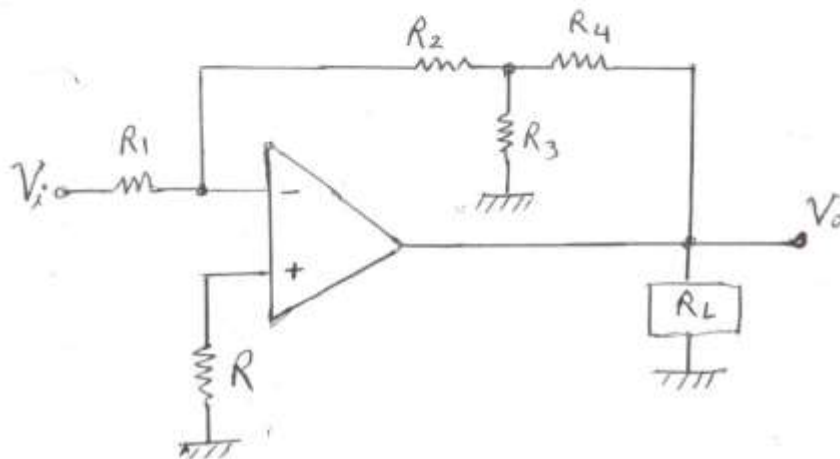
۱ - تقویت کننده وارونگر (inverting Ampl.) :



$$V_o = -\frac{R_F}{R_1} V_i \Rightarrow \frac{V_o}{V_i} = -\frac{R_F}{R_i}$$

$$R_i = \frac{V_i}{I_i} = R_1$$

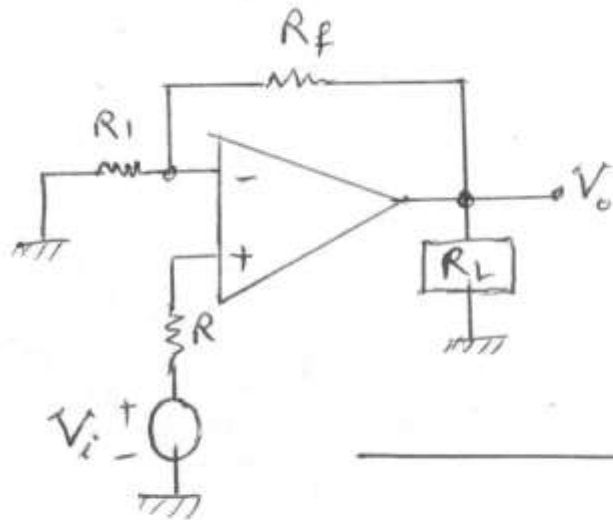
- برای افزایش بهره بدون استفاده از مقاومت های بزرگ (استفاده از شبکه T می باشد) :



$$\frac{V_o}{V_i} = -\frac{R_2}{R_1} \left( 1 + \frac{R_4}{R_2} + \frac{R_4}{R_3} \right)$$

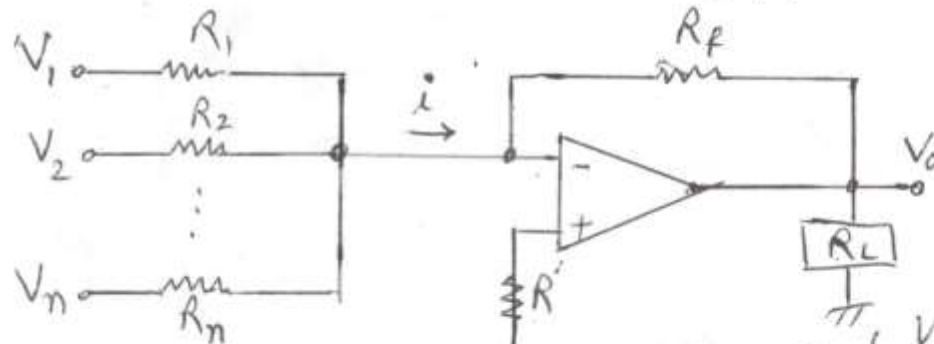
برای حصول بهترین نتیجه لازم از مقاومت هایی با توانش ۱٪ مورد استفاده قرار می گیرند.

۲- تریس کنده غیر وارونگر (Non inverting) :



$$\frac{V_o}{V_i} = \left(1 + \frac{R_f}{R_1}\right)$$

۳- مدار جمع کننده وارونگر (Inverting summing) :



$$\begin{cases} i = \frac{V_1}{R_1} + \frac{V_2}{R_2} + \dots + \frac{V_n}{R_n} \\ V_o = -i R_f \end{cases}$$

$$\Rightarrow V_o = -R_f \left( \frac{V_1}{R_1} + \frac{V_2}{R_2} + \dots + \frac{V_n}{R_n} \right)$$

✓ ۱:  $R_1 = R_2 = \dots = R_n = R \Rightarrow V_o = -\frac{R_f}{R} (V_1 + V_2 + \dots + V_n)$

بخش اول - کاربردهای تقویت کننده عملیاتی - جمع کننده - بافر - مبدلگر

۴ - تقویت کننده متوسط گیر وارونگر :

در مدار جمع کننده وارونگر :

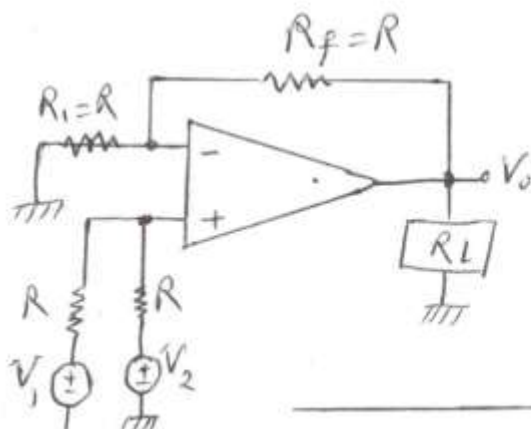
$$R_f = \frac{R}{n} \rightarrow \text{تعداد ورودی ها}$$

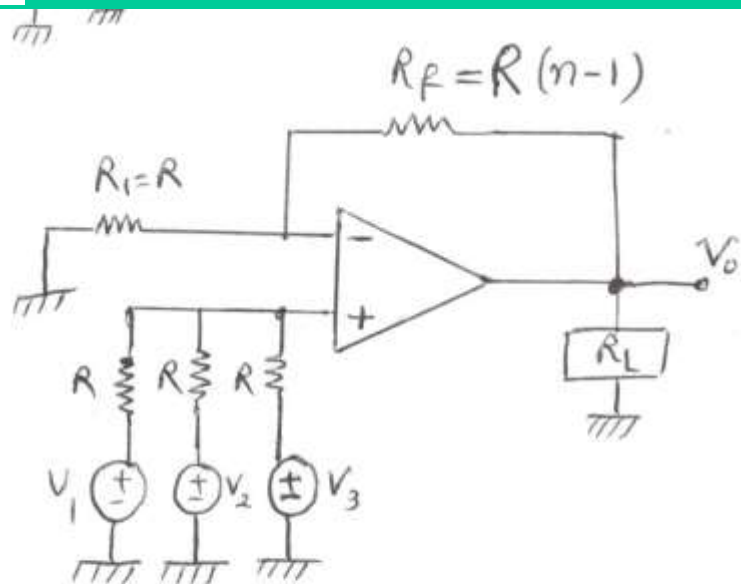
$$\Rightarrow V_o = - \left( \frac{V_1 + V_2 + \dots + V_n}{n} \right)$$

۵ - مدار جمع کننده ناوارونگر (بازو ورودی)

$$\begin{cases} V^+ = \frac{V_1 + V_2}{2} \\ V^- = V^+ \end{cases} \Rightarrow V_o = \left( 1 + \frac{R}{R} \right) V^+$$

$$\Rightarrow V_o = 2 \left( \frac{V_1 + V_2}{2} \right) = V_1 + V_2$$

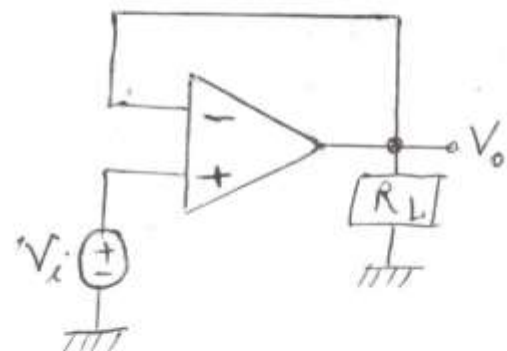




۶- مدار جمع کننده نفاذی با  $n$  ورودی :

$$V_o = V_1 + V_2 + V_3$$

تقریب :  $V^+ \equiv \frac{1}{3} (V_1 + V_2 + V_3)$



۷- دنبال کننده ولتاژ (Voltage follower)

- منبع (Source)

- تقویت کننده با بهره واحد (Unity gain Amp.)

- میانگیر (بافت)

- جداساز (Isolation Amp.)

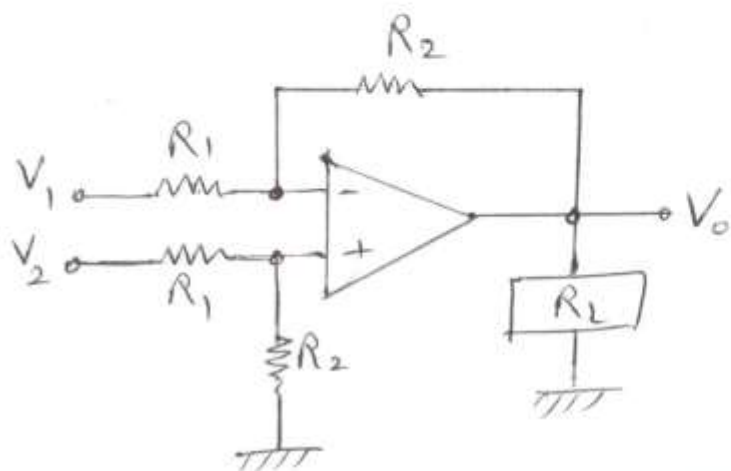
$$V_o = V_i$$

$$\left\{ \begin{array}{l} R_i \uparrow, \text{ Gain} \approx 1 \\ R_o \downarrow \end{array} \right\}$$



۳ بخش اول کاربردهای تقویت کننده عملیاتی - تفاضلی و ابزار دقیق

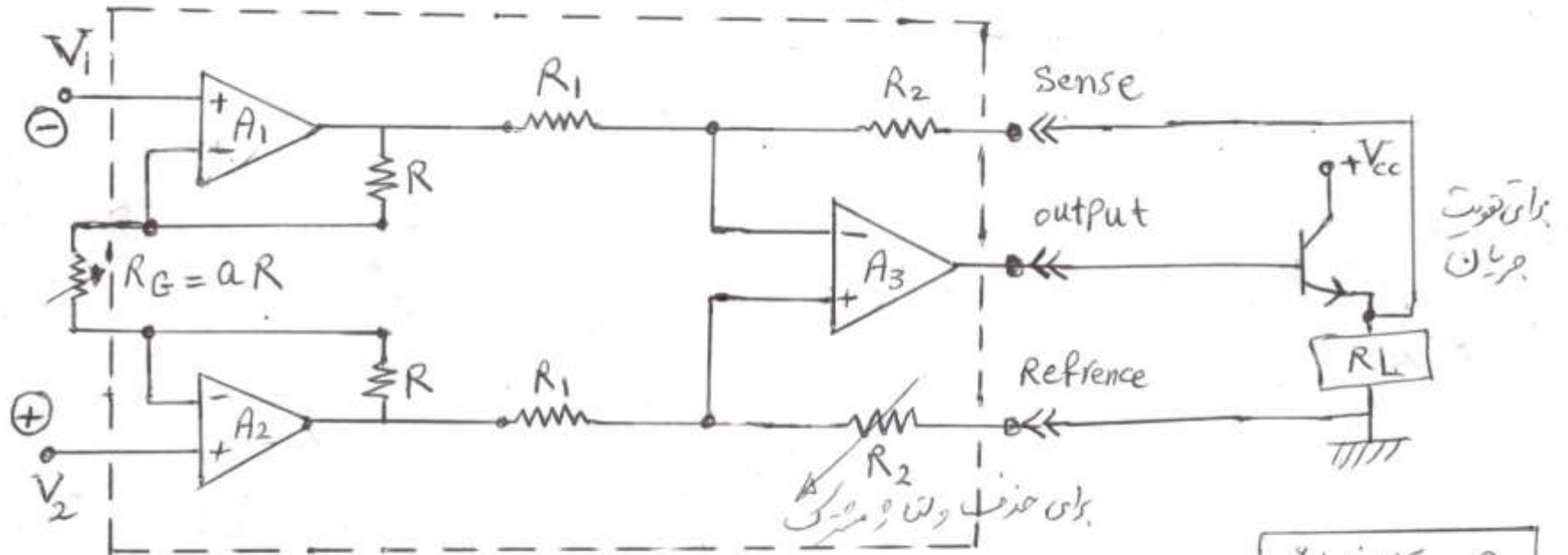
۸ - تقویت کننده تفاضلی (تفاضلی) :



$$V_o = \left( \frac{R_2}{R_1} \right) (V_2 - V_1)$$

اثبات : (بهترین و کوتاه ترین راه، استفاده از جمع آمار منهای)

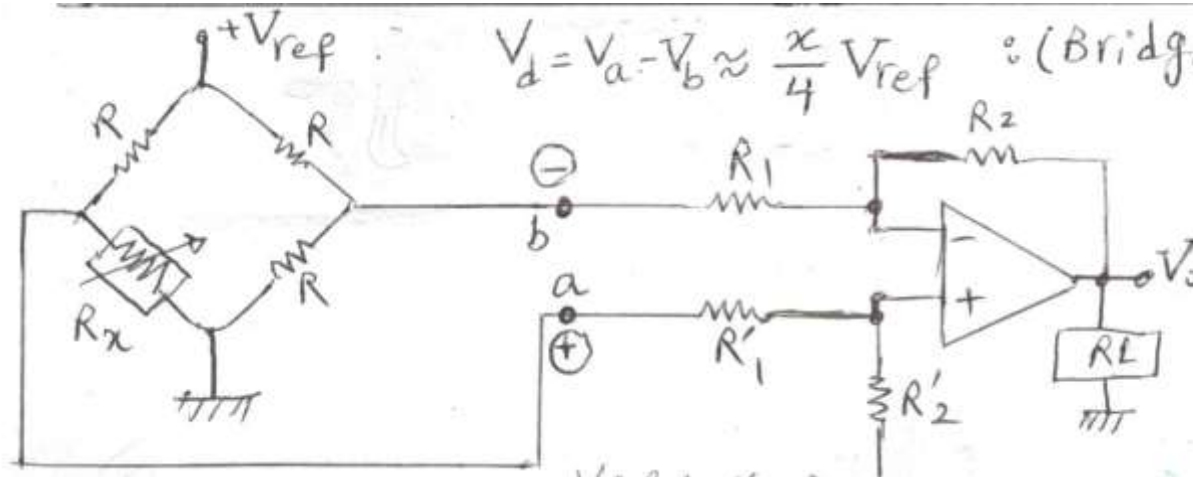
۹- تقویت کننده ابزار دقیق (تفاضلی با فروردی) (Instrumentation Amp.)  
 (AD524, AD624)



$$V_o = \left(1 + \frac{2R}{R_G}\right) \left(\frac{R_2}{R_1}\right) (V_2 - V_1) = \left(1 + \frac{2}{\alpha}\right) V_d$$

$$\left( \text{اگر: } R_2 = R_1, R_G = aR, V_d = V_2 - V_1 \right)$$

$R_x$  می تواند نامیده  
 مشهور و یا ترانس دیرین  
 باشد که در یک بل قرار  
 گرفته است.



$V_d = V_a - V_b \approx \frac{x}{4} V_{ref}$  : (Bridge) ۱-۱۰

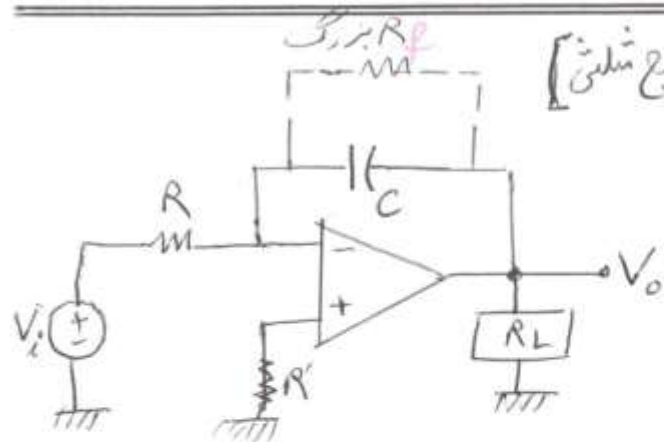
$$R_x = R \pm \Delta R = R \left(1 \pm \frac{\Delta R}{R}\right) = R(1+x)$$

$$\begin{cases} V_b = \frac{V_{ref}}{2} \\ V_a = \frac{1+x}{1+\frac{x}{2}} \cdot \frac{V_{ref}}{2} \end{cases}$$

بخش اول - کاربردهای تقویت کننده عملیاتی - اینترال گری و مشتق گری

۱۱- مدار اینترال گری (وایولگری) : [تبدیل موج مربعی به موج مثلثی]

(فیلتر پایین گذر با فرکانس قطع صفر)



$$\frac{V_o}{V_i} = \frac{-1}{sCR} = \frac{-1}{j\omega CR}$$

\* برای اینترال گری مناسب، RC باید خیلی بزرگتر از دوره تناوب سیگنال ورودی باشد.

$$V_o(t) = V_c - \frac{1}{RC} \int_0^t V_i(t) dt$$

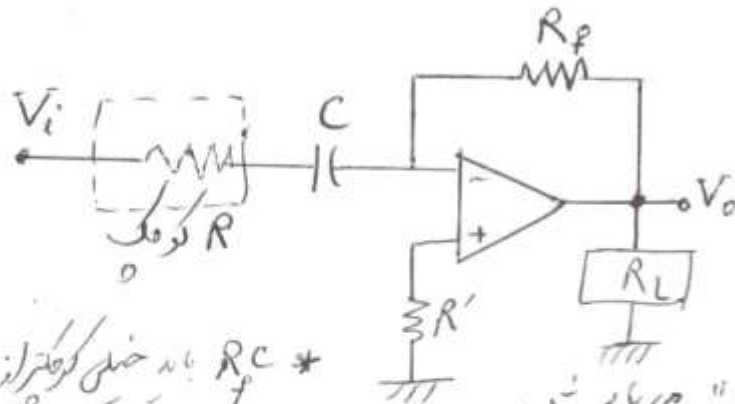
چون در فرکانس صفر (dc) خازن مدار باز عمل می کند، لذا بهره حلقه بسته بی نهایت خواهد شد.

برای اصلاح مدار اینترال گری: با موازی کردن مقاومت بزرگ با خازن اینترال گری

امپدانس را می توان انجام داد.

(مقاومت امپدانس اینترال گری را غیر ایده آل می کنند).

## ۱۲ - مدار مشتق گیر (نظیر بالاگذر با ضریب کسین قطع نامحدود)



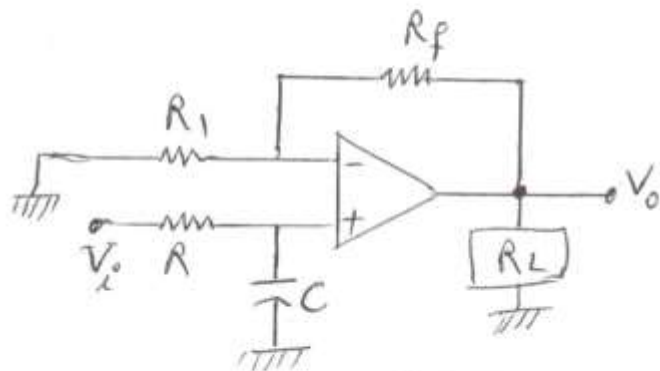
$$\frac{V_o}{V_i} = -sCR_f = -j\omega CR_f$$

$$\therefore V_o(t) = -R_f C \frac{dV_i}{dt}$$

- \* خصوصیات ذاتی مدار مشتق گیر به "بزرگ کننده فوئر" می باشد.
- \*  $RC$  باید خیلی کوچکتر از دوره تناوب سیگنال ورودی باشد.
- \* هر زمان که تغییر ناگهانی در  $V_i(t)$  بوجود آید، در خروجی جهشی ایجاد می شود.
- \* در عمل از مدارهای مشتق گیر اجتناب می شود، و اگر استفاده شود، معمولاً لازم است مطابق شکل، مقاومت کومکی با خازن سری شود.

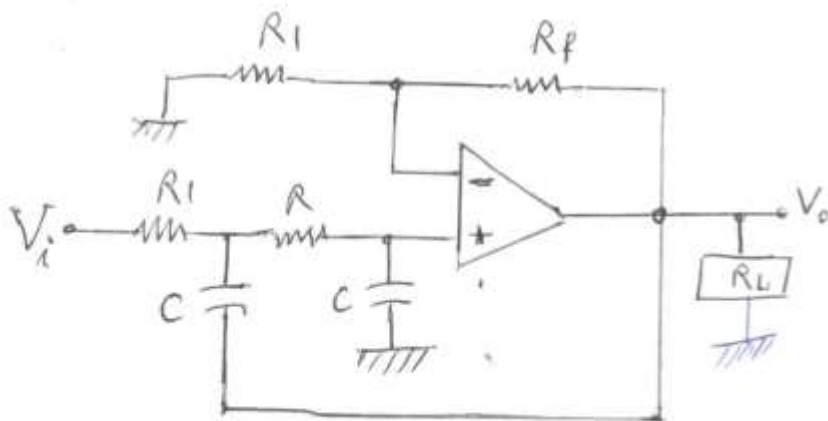
بخش اول - کاربردهای تقویت کننده عملیاتی - فیلترهای فعال (active filter)

۱۳ - فیلتر پایین گذر درجه یک :



$$A_V(s) = \frac{V_o}{V_i} = \frac{R_1 + R_f}{R_1} \cdot \frac{1}{1 + sCR}$$

۱۴ - فیلتر پایین گذر درجه دوم :



$$A_{V_0} \triangleq 1 + \frac{R_f}{R_1}$$

$$A_V(s) = \frac{V_o}{V_i} = \frac{A_{V_0}}{(sCR)^2 + (3 - A_{V_0})sCR + 1}$$



۱۵- فیلتر پاس باند گذر دوم را با هم Cascade کنیم. فیلتر درجه دوم

بدست می آید و اگر از سه طبقه استفاده شود، درجه ششم بدست می آید و ...

۱۶- فیلتر پاس باند گذر دوم قرار دهیم. اگر یک فیلتر درجه یک با یک فیلتر درجه دو با هم Cascade کنیم،

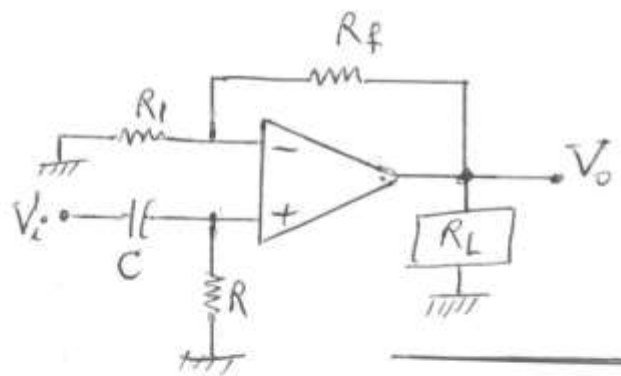
فیلتر درجه سوم و اگر یک فیلتر درجه یک با دو فیلتر درجه دو Cascade

شود فیلتر درجه پنجم بدست می آید و ...

۱۷- فیلتر بالاگذر (درجه یک)

اگر بجای خازن و مقاومت را در مدار قرار دهیم (۱۳) عوض کنیم

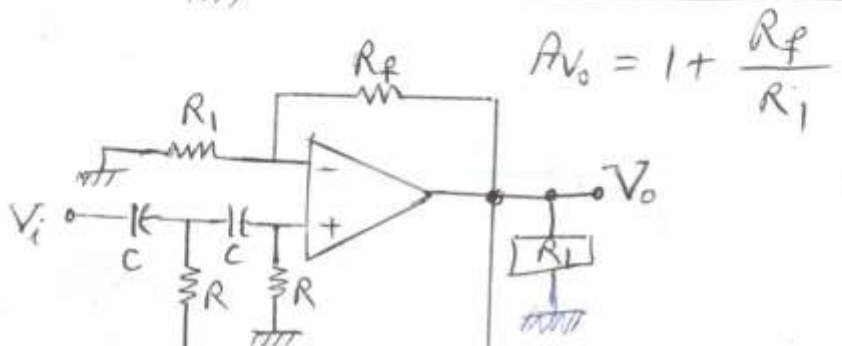
تبدیل به فیلتر بالاگذر می شود.



$$A_V(s) = \frac{V_o}{V_i} = \left(1 + \frac{R_f}{R_1}\right) \frac{sCR}{1 + sCR}$$

۱۸- فیلتر بالاگذر درجه دو

$A_{V_0}$



$$A_{V_0} = 1 + \frac{R_f}{R_1}$$

$$A_V(s) = \frac{A_{V_0}}{\left(\frac{1}{sCR}\right)^2 + (3 - A_{V_0})\left(\frac{1}{sCR}\right) + 1}$$





دانشگاه سیستان و بلوچستان

# Fundamentals of Microelectronics

## الکترونیک ۲

### فصل ۸ – تقویت کننده عملیاتی (آپ امپ) قسمت دوم – کاربردهای غیرخطی

**Mohammad Ali Mansouri- Birjandi**

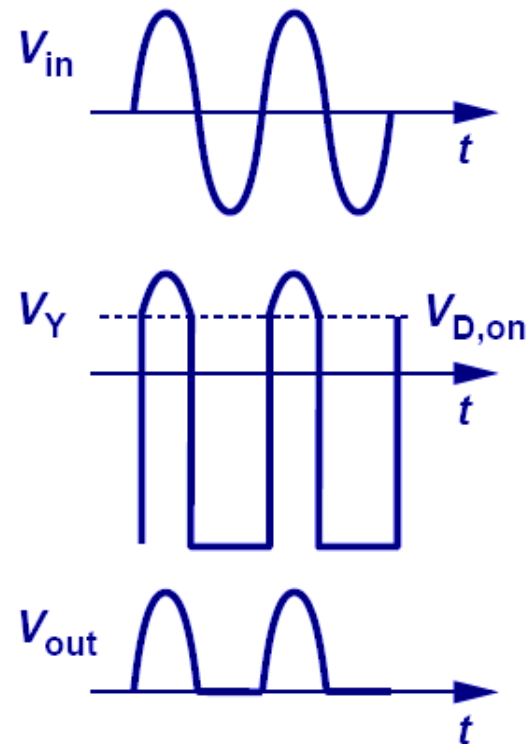
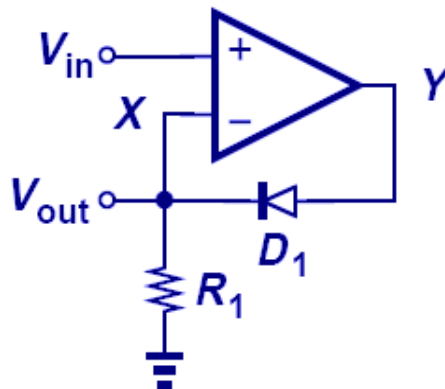
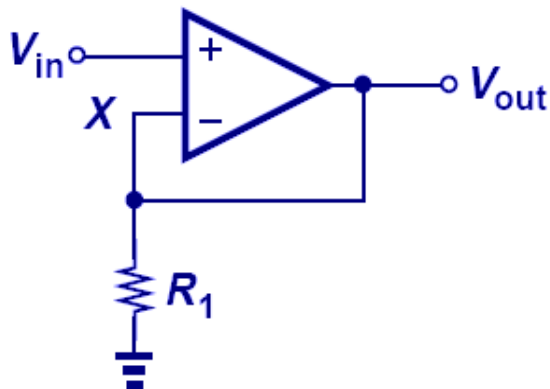
**Majid Ghadrddan**

**Faculty of Electrical and Computer Engineering  
University of Sistan and Baluchestan (USB)**

**[mansouri@ece.usb.ac.ir](mailto:mansouri@ece.usb.ac.ir) ,  
[mamansouri@yahoo.com](mailto:mamansouri@yahoo.com)**



# Precision Rectifier



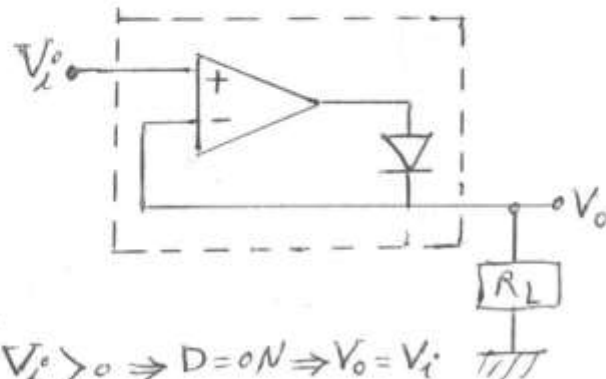
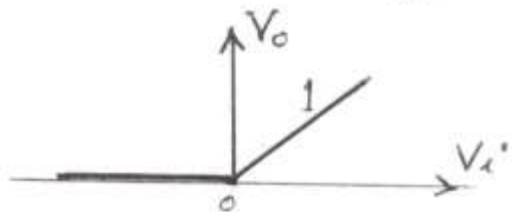
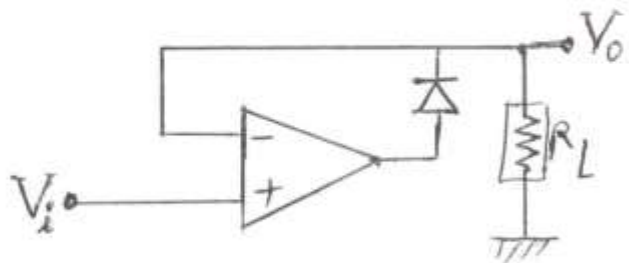
$$V^- \approx V^+$$
$$I_{in1} = I_{in2} \approx 0$$

فقط وقتی که دیود روشن هست ، فیدبک برقرار است و میتوان از این فرضیات استفاده نمود.

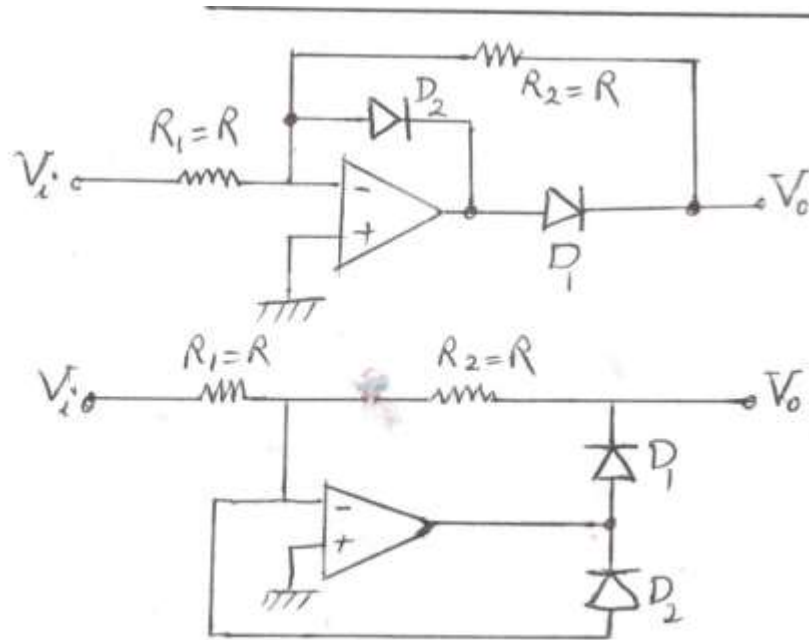
- When  $V_{in}$  is positive, the circuit in b) behaves like that in a), so the output follows input.
- When  $V_{in}$  is negative, the diode opens, and the output drops to zero. Thus performing rectification.

## بخش اول - کاربردهای تقویت کننده عملیاتی - میکسر کننده ها

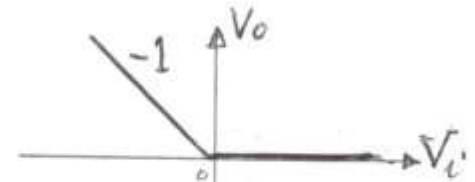
۱۹ - میکس ساز نیم موج رفتی :



$$\begin{cases}
 V_i > 0 \Rightarrow D = \text{on} \Rightarrow V_o = V_i \\
 V_i < 0 \Rightarrow D = \text{off} \Rightarrow V_o = 0
 \end{cases}$$



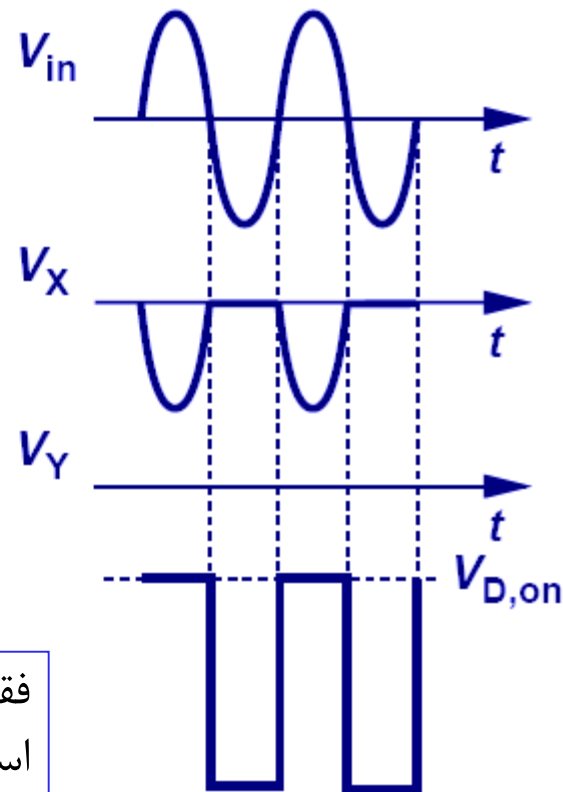
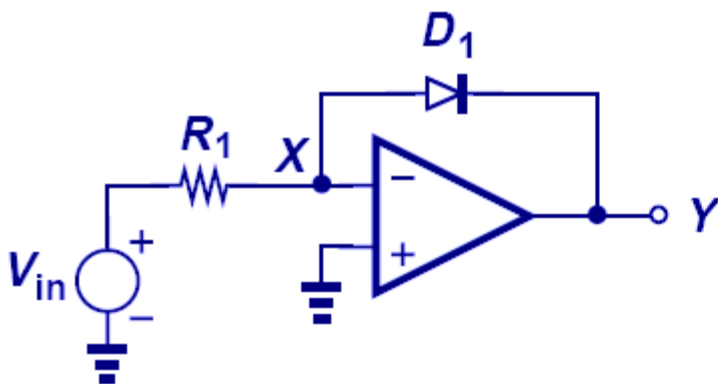
۲۰ - یکسو ساز نیم موج دقیق اصلاح شده :



$$\begin{aligned}
 V_i > 0 &\Rightarrow \begin{cases} D_1 = \text{OFF} \\ D_2 = \text{ON} \end{cases} \Rightarrow V_o = 0 \\
 V_i < 0 &\Rightarrow \begin{cases} D_1 = \text{ON} \\ D_2 = \text{OFF} \end{cases} \Rightarrow V_o = -V_i
 \end{aligned}$$



## Inverting Precision Rectifier



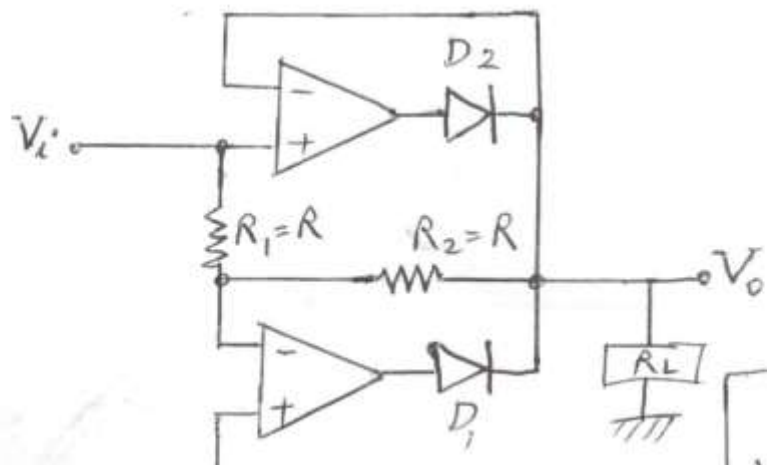
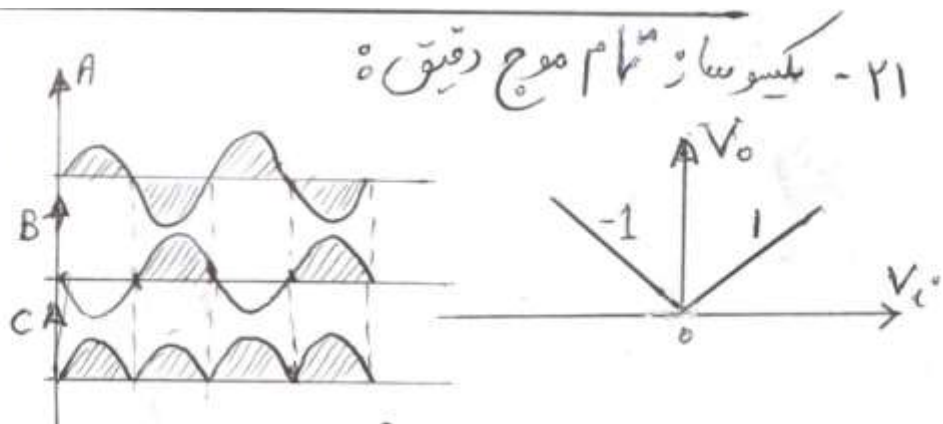
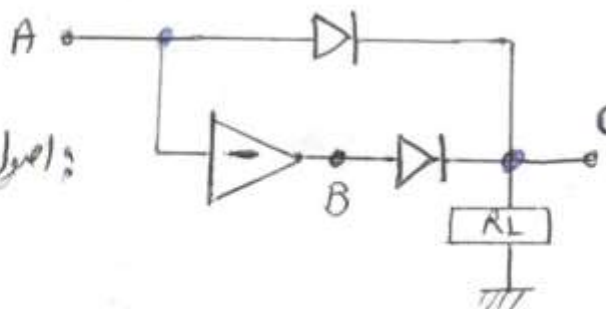
$$V^- \approx V^+$$

$$I_{in1} = I_{in2} \approx 0$$

فقط وقتی که دیود روشن هست ، فیدبک برقرار است و میتوان از این فرضیات استفاده نمود.

- When  $V_{in}$  is positive, the diode is on,  $V_Y$  is pinned around  $V_{D,on}$ , and  $V_x$  at virtual ground.
- When  $V_{in}$  is negative, the diode is off,  $V_Y$  goes extremely negative, and  $V_x$  becomes equal to  $V_{in}$ .

اصول میکروسیاری



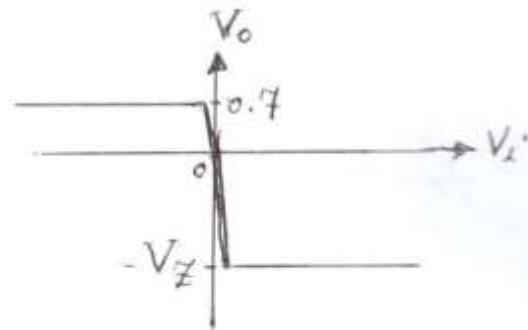
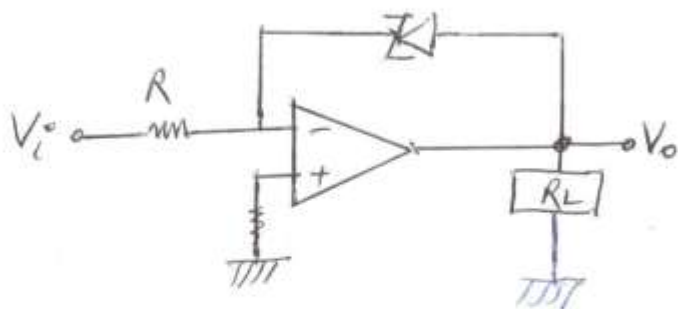
$$V_i > 0 \Rightarrow \begin{cases} D_2 = ON \\ D_1 = OFF \end{cases} \Rightarrow V_o = V_i$$

$$V_i < 0 \Rightarrow \begin{cases} D_1 = ON \\ D_2 = OFF \end{cases} \Rightarrow V_o = -V_i$$

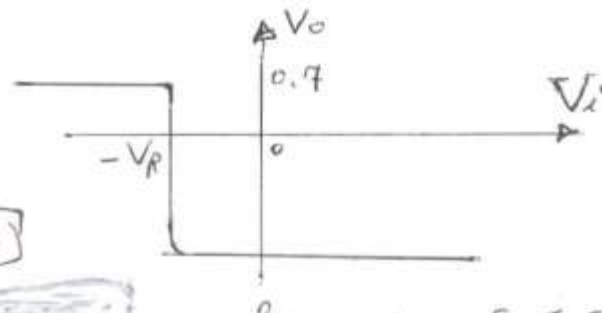
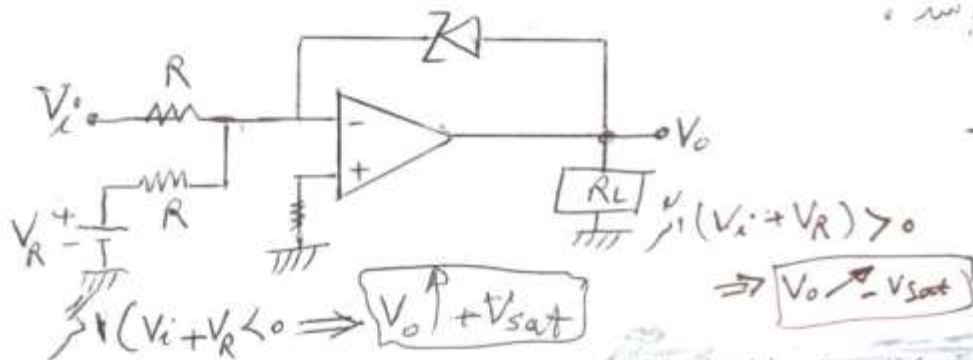


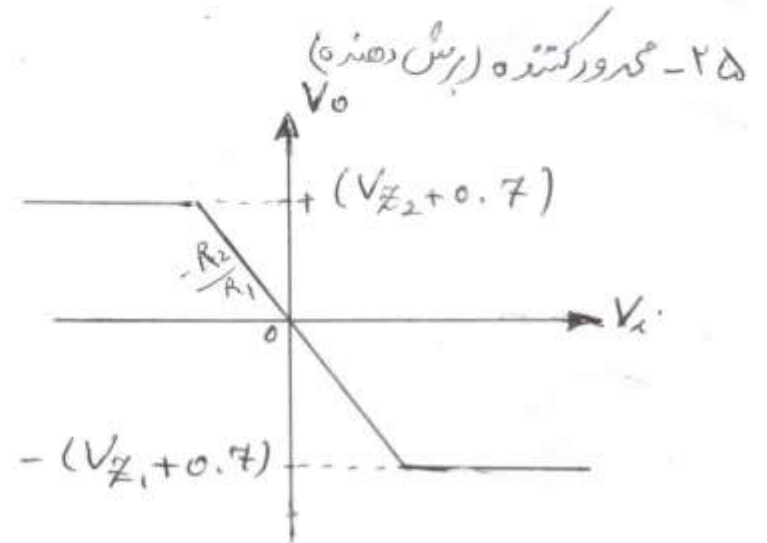
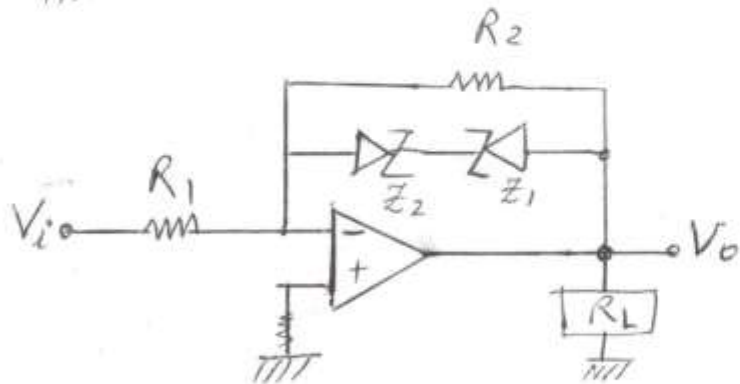
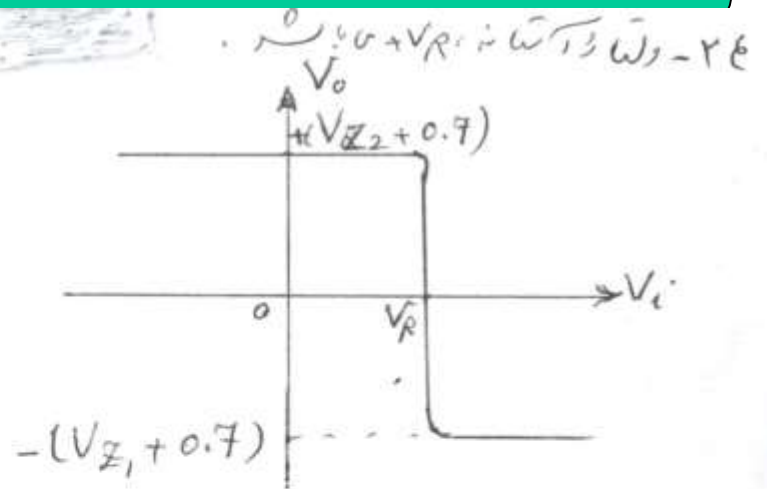
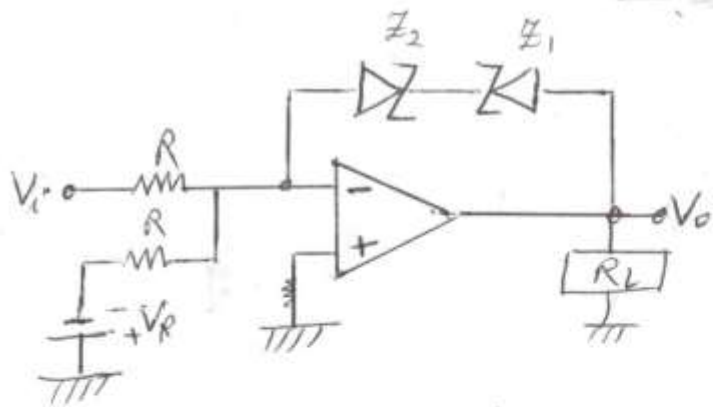
بخش اول - کاربردهای تقویت کننده عملیاتی - مقایسه کننده ها و مبرور کننده ها

۲۲ - ولتاژ استانه (مقایسه) ، همفر ولت می باشد.



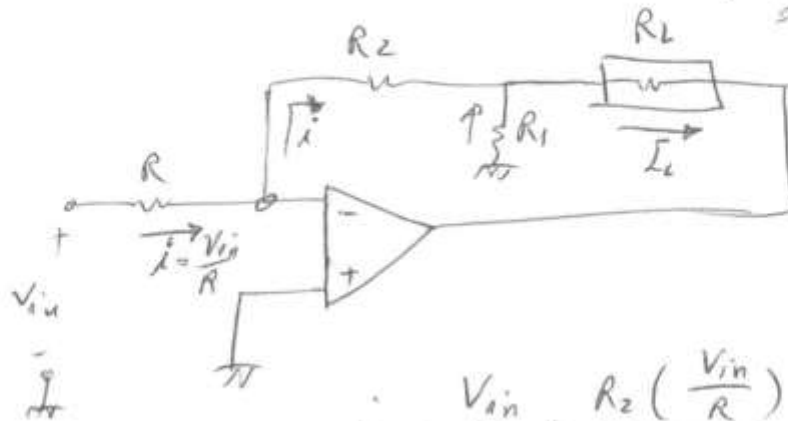
۲۳ - ولتاژ استانه (مقایسه) -  $V_R$  می باشد.





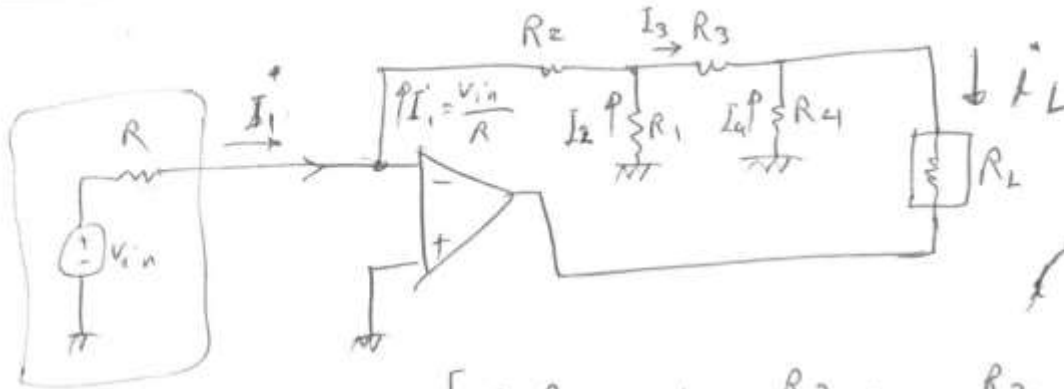
بخش دوم - کاربرد مدارات مجتمع خطی - مدل ولتاژ به جریان  
 V-I-C

استفاده از شبکه T برای تقویت جریانها کوچک :



$$I_L = \frac{V_{in}}{R} \left( 1 + \frac{R_2}{R_1} \right)$$

$$I_L = \frac{V_{in}}{R} + \frac{R_2 \left( \frac{V_{in}}{R} \right)}{R_1} = \frac{V_{in}}{R} \left[ \frac{R_1 + R_2}{R_1} \right] = \frac{V_{in}}{R} \left( 1 + \frac{R_2}{R_1} \right)$$



(L)

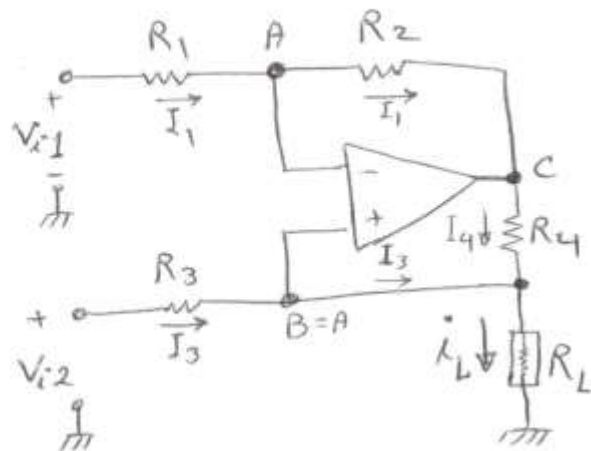
$$I_L = \frac{V_{in}}{R} \left[ \left( \frac{R_2}{R_4} \right) \left( 1 + \frac{R_3}{R_1} \right) + \frac{R_2}{R_1} + \frac{R_3}{R_4} + 1 \right]$$

$\therefore I_1 = \frac{V_{in}}{R}$

$$I_2 = \frac{I_1 R_2}{R_1} \rightarrow I_3 = I_1 + I_2 = I_1 \left( 1 + \frac{R_2}{R_1} \right)$$

$$I_4 = \frac{R_3 I_3 + R_2 I_1}{R_4} = \frac{(R_3 (1 + \frac{R_2}{R_1}) + R_2) I_1}{R_4}$$

$$I_L = I_3 + I_4 = I_1 \left( \left( 1 + \frac{R_2}{R_1} \right) + \frac{R_2}{R_4} + \left( \frac{R_3 (1 + \frac{R_2}{R_1})}{R_4} \right) \right) = \dots$$



۱. مبدل ولتاژ به جریان Howland :

با شرط :  $\frac{R_4}{R_3} = \frac{R_2}{R_1}$

$I_L = \frac{V_{i2} - V_{i1}}{R_3}$

$R_o = \frac{R_4}{\frac{R_2}{R_1} - \frac{R_4}{R_3}} = \infty$

اثبات :

$$I_1 = \frac{V_{i1} - V_A}{R_1} = \frac{V_A - V_C}{R_2} \rightarrow V_A - V_C = \frac{R_2}{R_1} (V_{i1} - V_A)$$

$$I_3 = \frac{V_{i2} - V_A}{R_3}, \quad I_4 = \frac{V_C - V_A}{R_4}$$

$$I_L = I_3 + I_4 = \frac{V_{i2} - V_A}{R_3} + \frac{V_C - V_A}{R_4} = \frac{R_2}{R_1 R_4} (V_A - V_{i1}) + \frac{V_{i2} - V_A}{R_3} = \frac{V_A}{R_L}$$

$$\Rightarrow V_A \left[ \frac{R_2}{R_1 R_4} - \frac{1}{R_3} - \frac{1}{R_L} \right] = V_{i1} \left( \frac{R_2}{R_1 R_4} \right) - V_{i2} \left( \frac{1}{R_3} \right)$$

$$\Rightarrow V_A = \frac{V_{i2} \left( \frac{1}{R_3} \right) - V_{i1} \left( \frac{R_2}{R_1 R_4} \right)}{\frac{1}{R_3} + \frac{1}{R_L} - \frac{R_2}{R_1 R_4}} = [ \quad ]$$

$R_o = R_L$

$$\Rightarrow V_A = \frac{V_{i2} \left( \frac{1}{R_3} \right) - V_{i1} \left( \frac{R_2}{R_1 R_4} \right)}{\frac{1}{R_3} + \frac{1}{R_L} - \frac{R_2}{R_1 R_4}} = [ \text{ " } ]$$

$$i_L = \frac{V_A}{R_L} = \frac{1}{R_L} [ \text{ " } ] \Rightarrow \text{مخرج مشترک} = \left( \frac{R_L}{R_3} + 1 - \frac{R_2 R_L}{R_1 R_4} \right)$$

برای آنکه خروجی  $i_L$  متغیر از  $R_L$  نباشد باید شرط زیر برقرار باشد:

$$\frac{1}{R_3} = \frac{R_2}{R_1 R_4} \rightarrow \boxed{\frac{R_4}{R_3} = \frac{R_2}{R_1}}$$

$$i_L = V_{i2} \left( \frac{1}{R_3} \right) - V_{i1} \left( \frac{R_2}{R_1 R_4} \right) \Rightarrow \boxed{i_L = \frac{V_{i2} - V_{i1}}{R_3}}$$

$\left( \frac{1}{R_3} \right)$

---

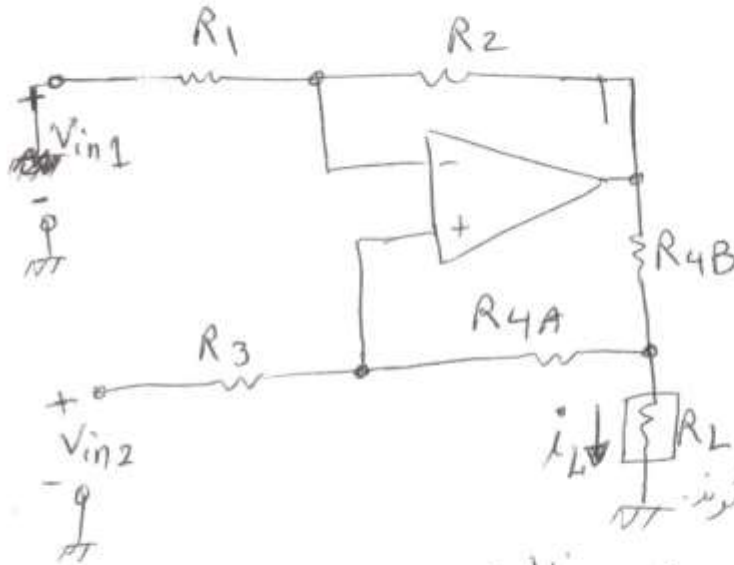
② حالت Howland inverting :  $\boxed{V_{i2} = 0}$   $\Rightarrow \boxed{i_L = \frac{-V_{i1}}{R_3}}$

③ حالت Howland noninverting :  $\boxed{V_{i1} = 0}$   $\Rightarrow \boxed{i_L = \frac{V_{i2}}{R_3}}$

V-I-c

محسین لوی - کاربرد مدارات مجتمع خطی - مبدل ولتاژ به جریان

"Howland Improved"



با شرط :

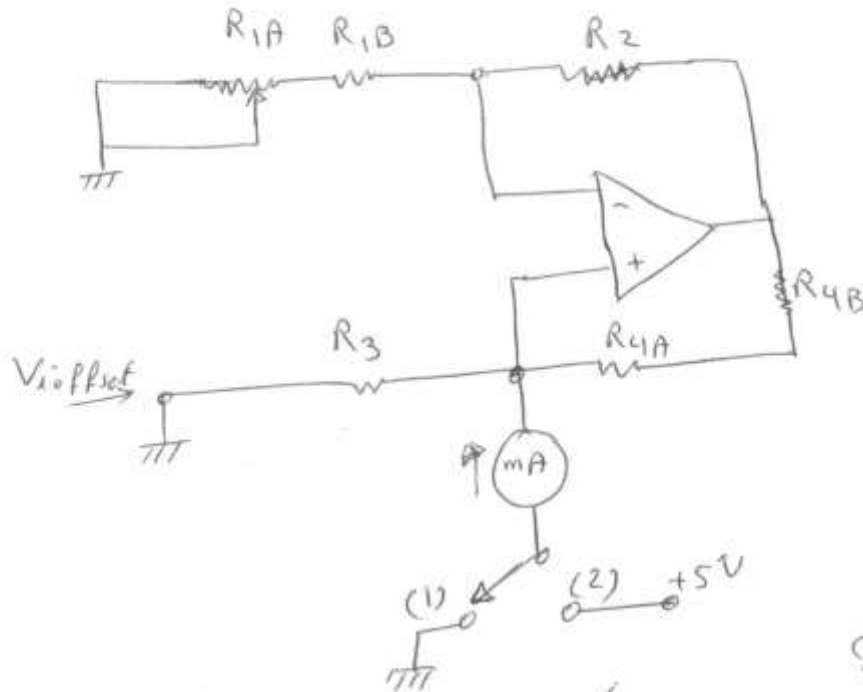
$$\frac{R_{4A} + R_{4B}}{R_3} = \frac{R_2}{R_1}$$

$$I_L = (V_{i2} - V_{i1}) \left( \frac{R_2}{R_1 R_{4B}} \right)$$

$R_1, R_2, R_3, R_4$  بزرگ انتخاب می شوند.  
 $R_{4B}$  تا حد ممکن کوچک انتخاب می شود. (بر دو منظور):

- ۱- حساسیت (تابع انتقال) مدار زیاد شود.
- ۲- فاصله  $V_L$  تا  $V_{com}$  و  $V_L$  از  $V_L$  کوچکتر شود.

(۵) مدار گایبر کردن (Improved V-I-C) :



برای گایبر کردن باید :

$$\frac{R_1}{R_3} = \frac{R_2}{R_4}$$

$$(R_{1A} + R_{1B} = R_1)$$

$R_{1A}$  باید میزان خطای نامعبر بودن مقاومتها را کم کند .

روش گایبر کردن :

$R_{1A}$  را آنقدر تغییر می دهیم تا در حالتیکه

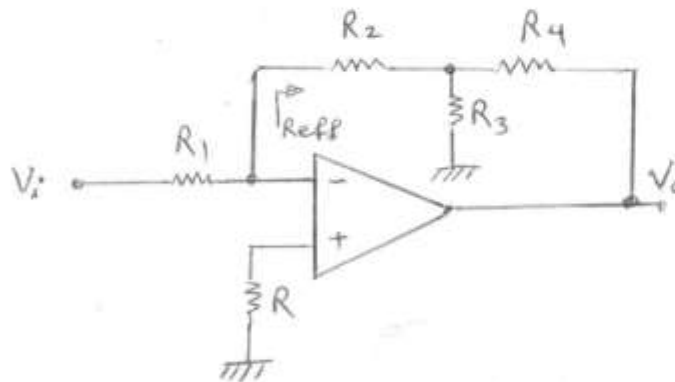
$V_i = 0$  تغییر در نسبت کمپ از حالت (۱) به (۲) و بالعکس هیچ جریان از آمپرمتر عبور نکند .

در این حالت :  $R_o = R_3 \parallel (-R_3) = \infty$  خواهد شد .

محبوب سوم - کاربرد مدارات مجتمع خطی

فصل دوازدهم: پترنگ کردن و مشابہ سازی قطعات پیسو الکترونیکی توسط IC  
(۱۲-۱) افزایش مقاومت (برای دستیابی به بهره بیشتر توسط مقادیرهای کوچک):

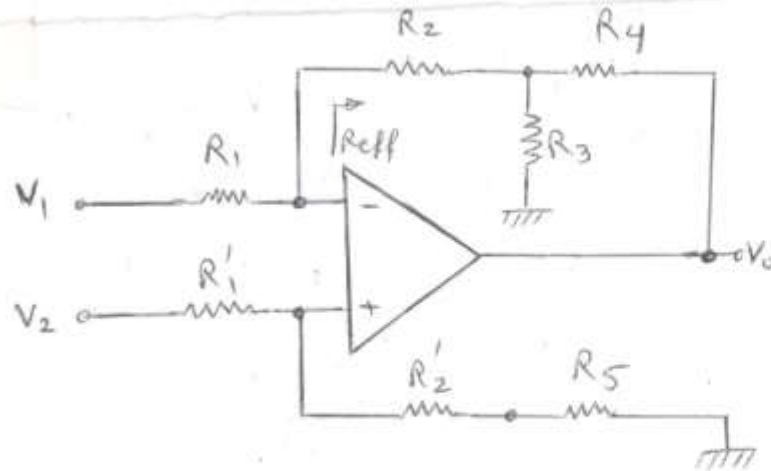
\* استفاده از شبکه T



$$R_{eff} = R_2 + R_4 + \frac{R_2 R_4}{R_3}$$

$$V_o = -\text{Gain} \cdot V_i$$

$$\text{Gain} = \frac{R_{eff}}{R_1}$$



\* در حالت تعادل:

$$R_1 = R'_1$$

$$R_2 = R'_2$$

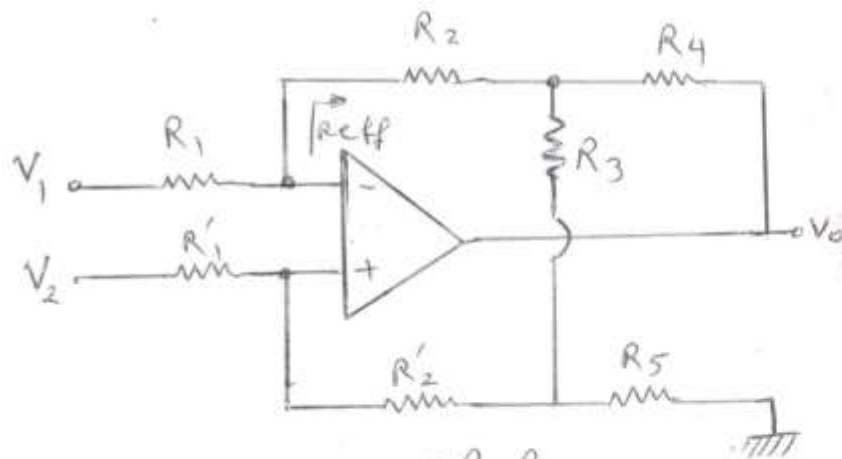
$$R_5 = R_4 \parallel R_3$$

بافتن

$$R_{eff} = R_2 + R_4 + \frac{R_2 R_4}{R_3}$$

$$V_o = (V_2 - V_1) \text{Gain}$$

$$\text{Gain} = \frac{R_{eff}}{R_1}$$



\* مدار بهتر برای حالت تعادل:

$$R_1 = R'_1$$

$$R_2 = R'_2$$

$$R_5 = R_4$$

بافتن

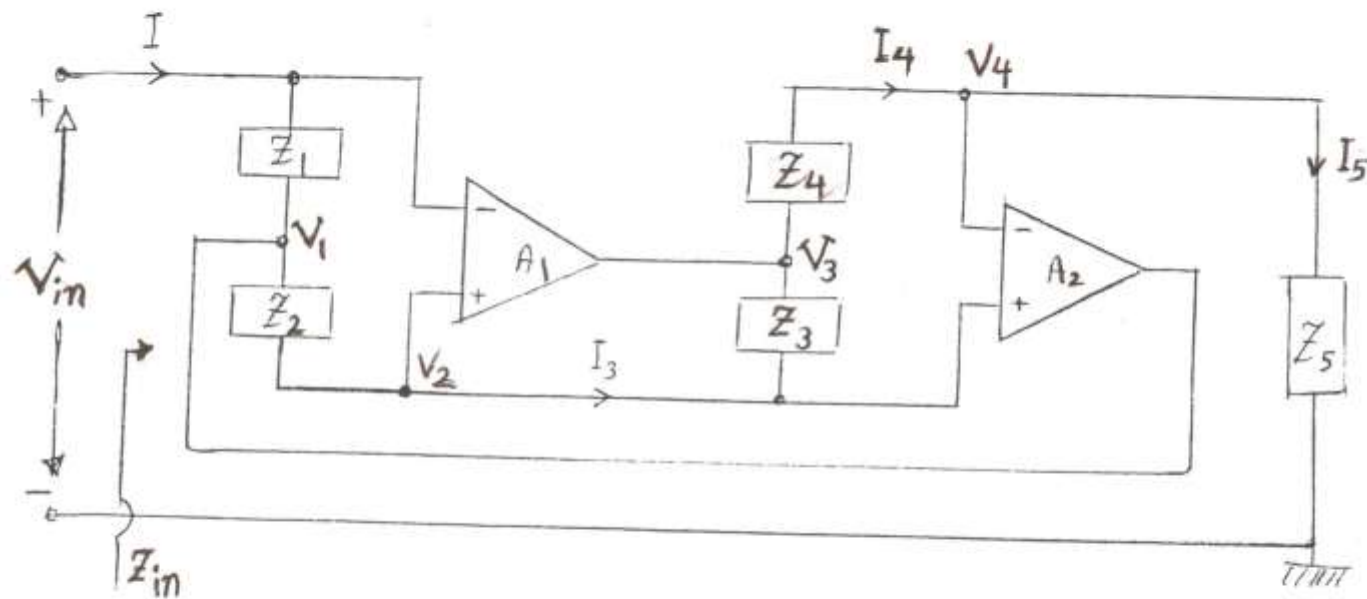
$$R_{eff} = R_2 + R_4 + \frac{2R_2 R_4}{R_3}$$

$$V_o = (V_2 - V_1) \text{Gain}$$

$$\text{Gain} = \frac{R_{eff}}{R_1}$$

محبت سوم - کاربرد مدارات بیس حقیقی

مدار کلی تبدیل امپدانس (GIC) : (General Impedance Converter)



با توجه به قوانین OP-Amp داریم :

$$V_{in} = V_2 = V_4, \quad I_4 = I_5 = \frac{V_4}{Z_5}$$

$$V_3 = V_4 + I_4 Z_4, \quad I_3 = \frac{V_2 - V_3}{Z_3} = -V_{in} \frac{Z_4}{Z_3 Z_5}$$

$$I = \frac{V_{in} - V_1}{Z_1} = V_{in} \frac{Z_4 Z_2}{Z_1 Z_3 Z_5} \Rightarrow \boxed{Z_{in} = \frac{V_{in}}{I} = \frac{Z_1 Z_3 Z_5}{Z_2 Z_4}}$$



$$I = \frac{V_{in} - V_1}{Z_1} = V_{in} \frac{Z_4 Z_2}{Z_1 Z_3 Z_5} \Rightarrow \boxed{Z_{in} = \frac{V_{in}}{I} = \frac{Z_1 Z_3 Z_5}{Z_2 Z_4}}$$

(I) \* حال اگر در این رابطه  $Z_2$  و یا  $Z_4$  خازن باشند (و بقیه مقاومست) داریم:

$$Z_{in} = \frac{R_1 R_3 R_5}{\frac{1}{j\omega C_2} \cdot R_4} = j\omega C_2 \frac{R_1 R_3 R_5}{R_4}$$

$$L = C_2 \frac{R_1 R_3 R_5}{R_4}$$

«کل مدار مثل یک سلف عمل می‌کند»

که در آن داریم:

$$C_{in} = C_1 \frac{R_2 R_4}{R_3 R_5}$$

(II) اگر  $Z_1$  و یا  $Z_3$  و یا  $Z_5$  خازن باشند در آن صورت:

مثال عددی ①: اگر در مدار فوق داشته باشیم:

$$R_1 = R_3 = R_5 = R_4 = 10K, C_2 = 1nF$$

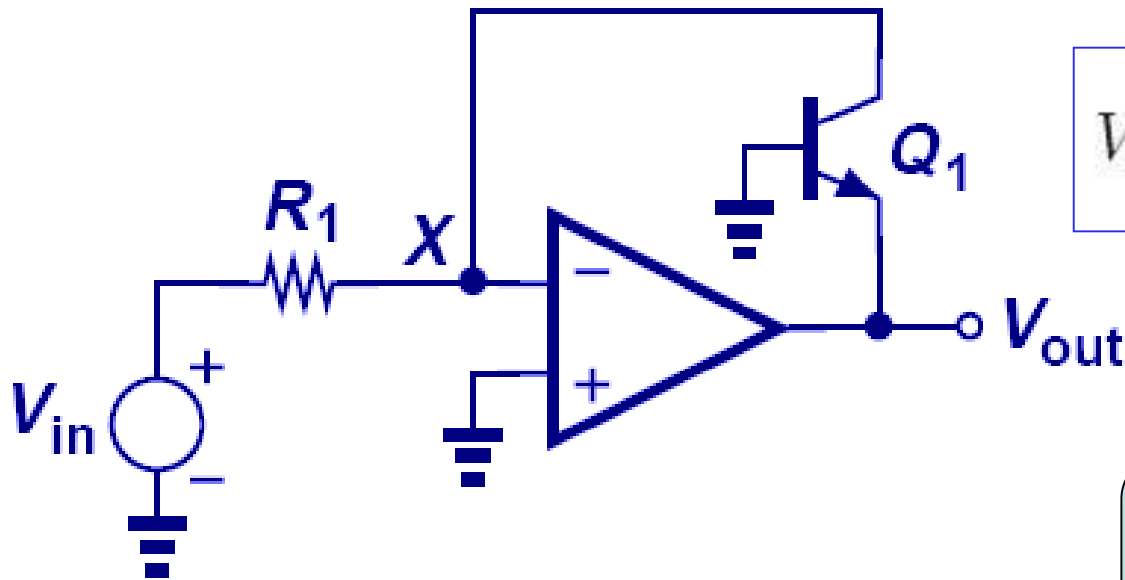
$$\Rightarrow L = 0.1H$$

(توجه: سلف این مدار را می‌توانستیم با سلف تعریف ساخت)

$$\boxed{Z_{in} = 116 + j\omega 0.16}$$

$$\leftarrow \begin{matrix} Z_1 = Z_3 = Z_5 = 2K\Omega, \\ Z_2 = 1K\Omega, \\ Z_4 = 0.02\mu F \parallel 69K\Omega \end{matrix}$$

# Logarithmic Amplifier



$$V_{BE} = V_T \ln \frac{V_{in} / R_1}{I_S}$$

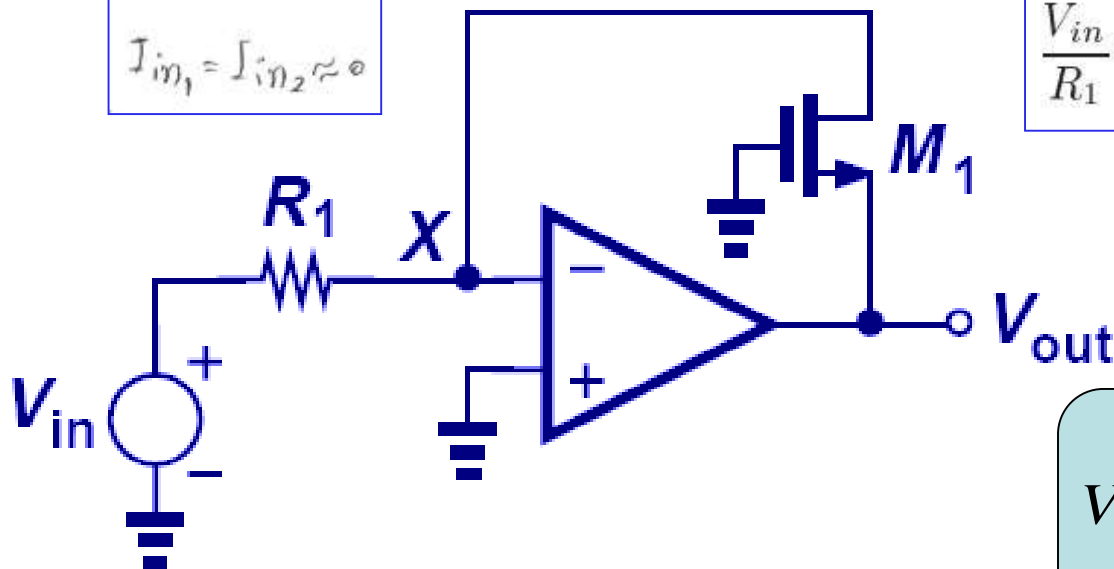
$$V_{out} = -V_T \ln \frac{V_{in}}{R_1 I_S}$$

- By inserting a bipolar transistor in the loop, an amplifier with logarithmic characteristic can be constructed.
- This is because the current to voltage conversion of a bipolar transistor is a natural logarithm.



## Square-Root Amplifier

$$V^- \approx V^+ \\ I_{in1} = I_{in2} \approx 0$$

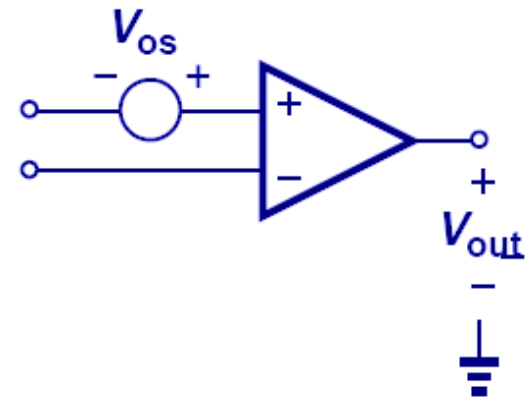
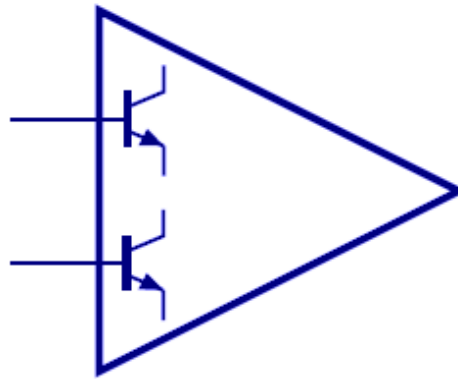
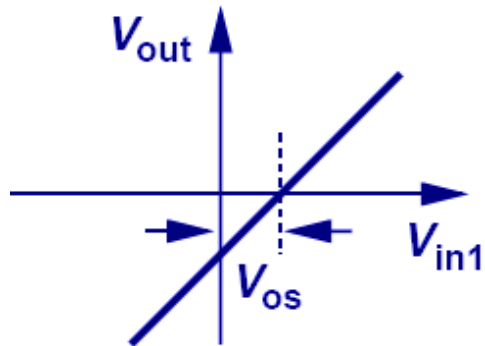


$$\frac{V_{in}}{R_1} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2.$$

$$V_{out} = - \sqrt{\frac{2V_{in}}{\mu_n C_{ox} \frac{W}{L} R_1}} - V_{TH}$$

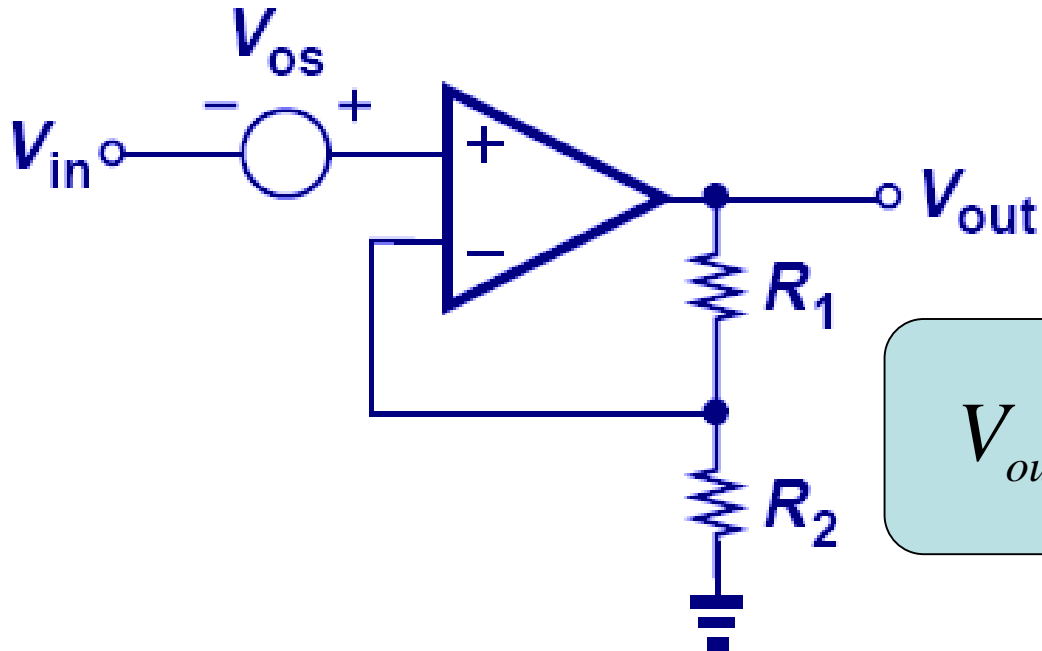
- By replacing the bipolar transistor with a MOSFET, an amplifier with a square-root characteristic can be built.
- This is because the current to voltage conversion of a MOSFET is square-root.

# Op Amp Nonidealities: DC Offsets



- Offsets in an op amp that arise from input stage mismatch cause the input-output characteristic to shift in either the positive or negative direction (the plot displays positive direction).

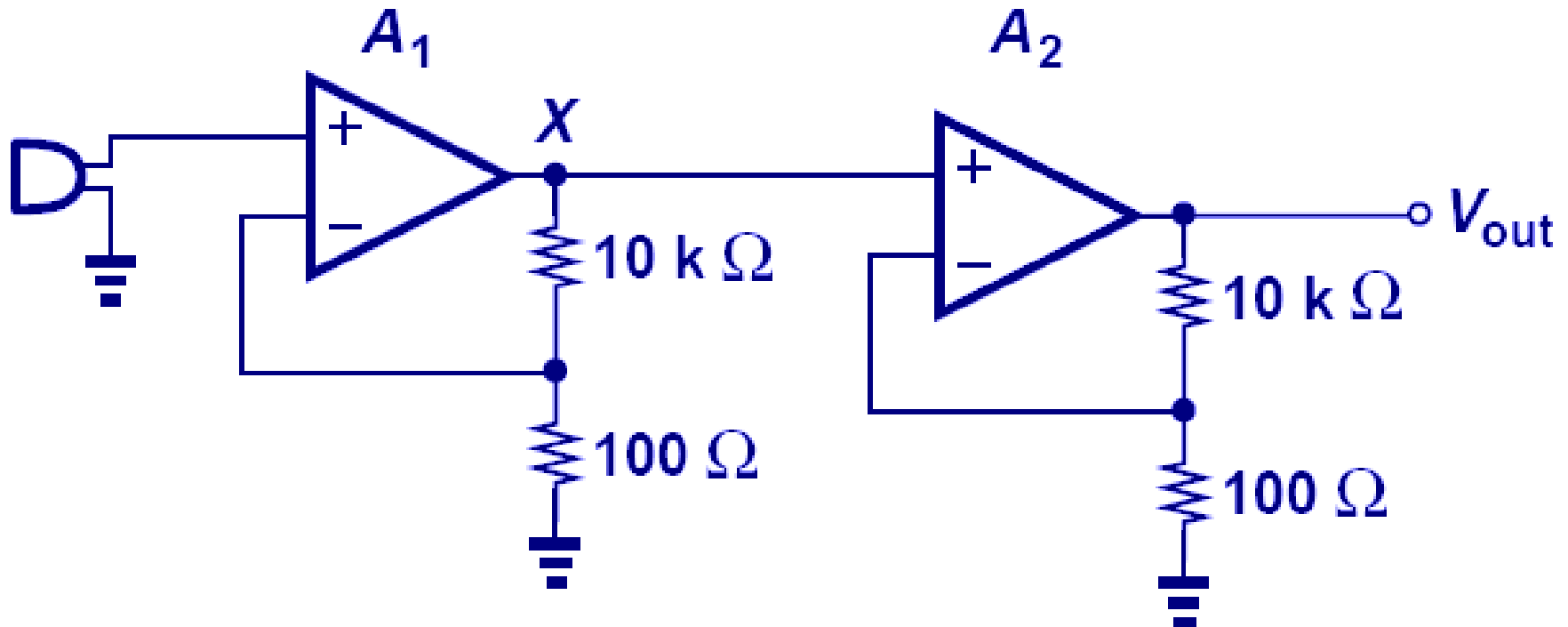
## Effects of DC Offsets



$$V_{out} = \left( 1 + \frac{R_1}{R_2} \right) (V_{in} + V_{os})$$

➤ As it can be seen, the op amp amplifies the input as well as the offset, thus creating errors.

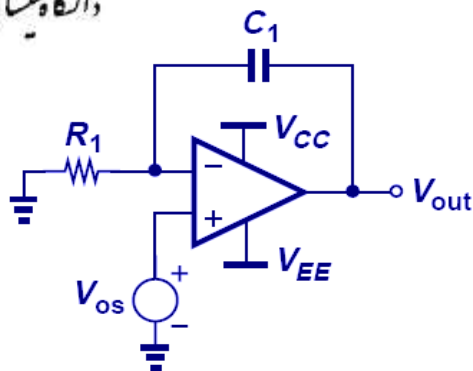
## Saturation Due to DC Offsets



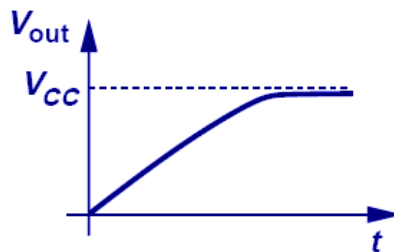
- Since the offset will be amplified just like the input signal, output of the first stage may drive the second stage into saturation.



# Offset in Integrator

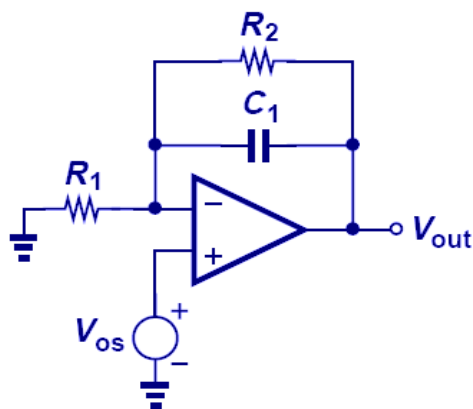


(a)

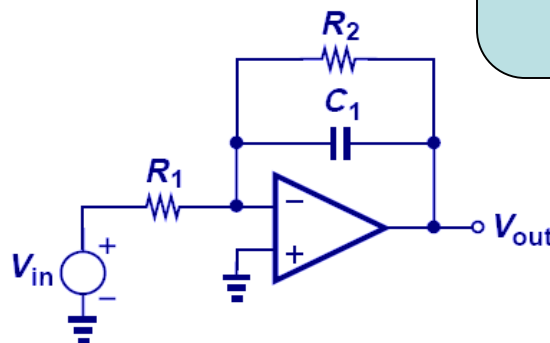


(b)

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1} \frac{1}{R_2 C_1 s + 1}$$



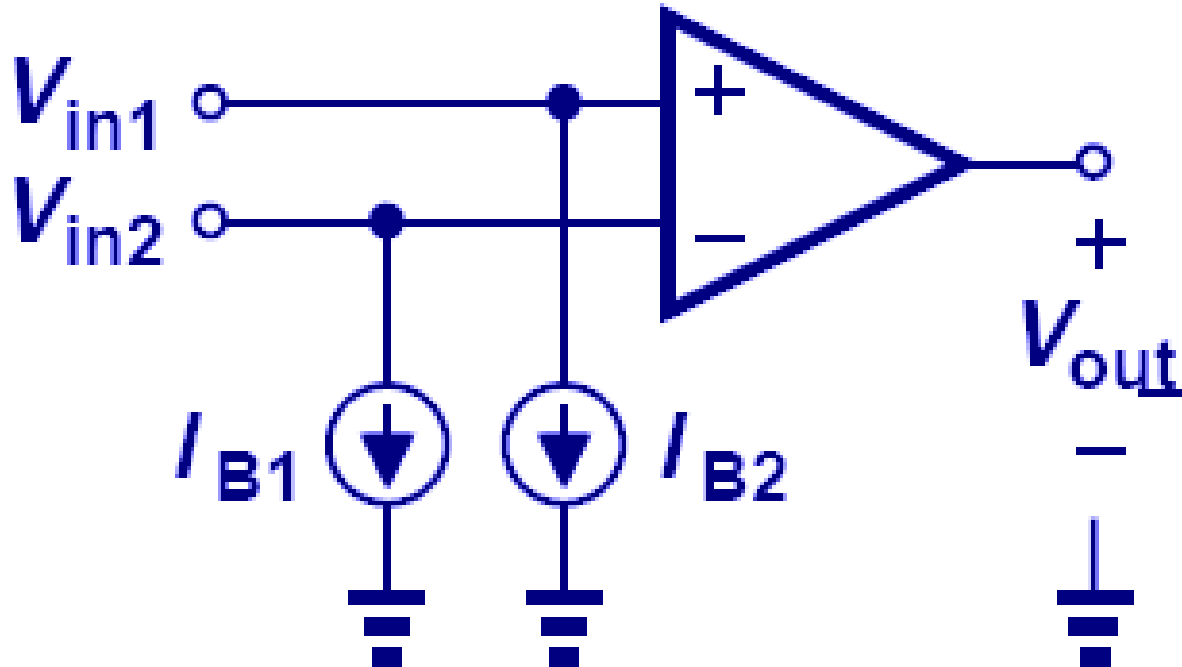
(c)



(d)

- A resistor can be placed in parallel with the capacitor to “absorb” the offset. However, this means the closed-loop transfer function no longer has a pole at origin.

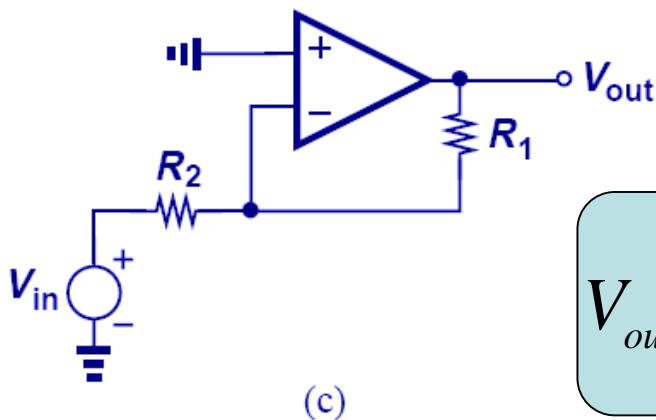
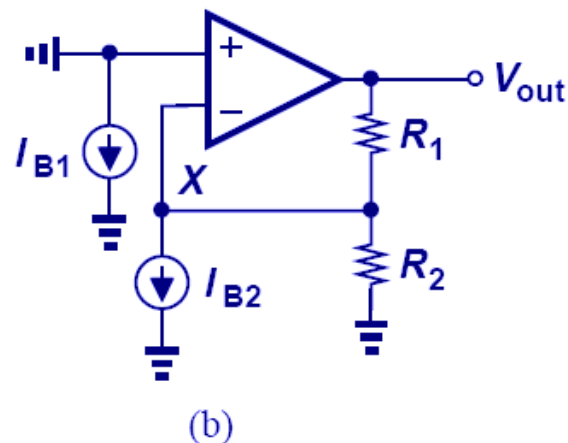
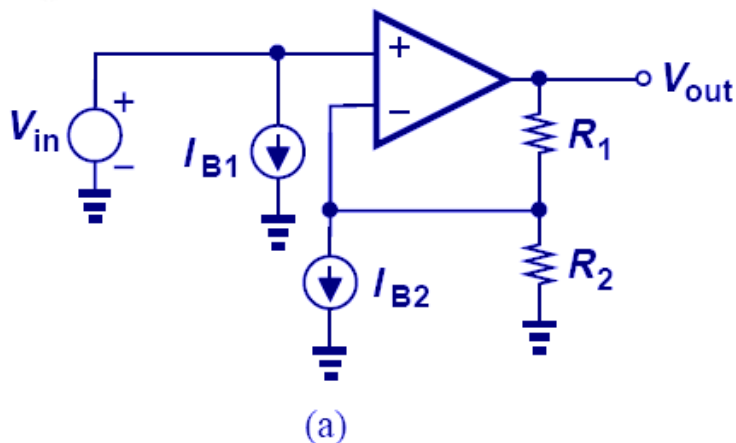
# Input Bias Current



- The effect of bipolar base currents can be modeled as current sources tied from the input to ground.



## Effects of Input Bias Current on Noninverting Amplifier

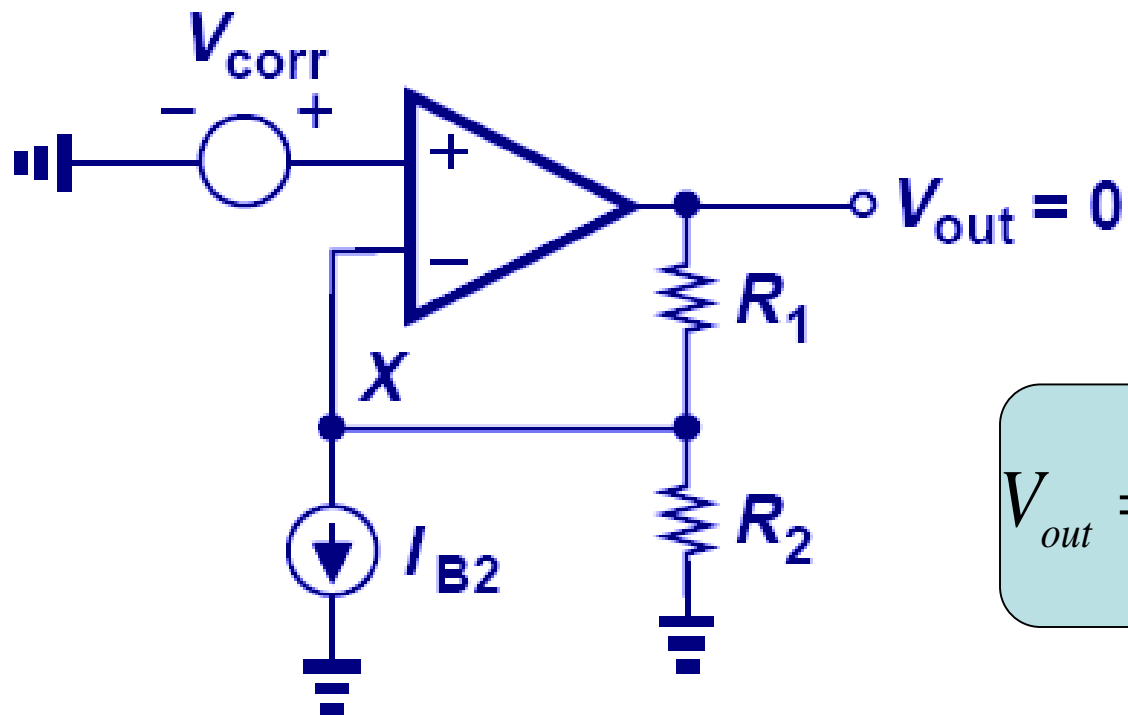


$$V_{out} = -R_2 I_{B2} \left( -\frac{R_1}{R_2} \right) = R_1 I_{B2}$$

➤ It turns out that  $I_{B1}$  has no effect on the output and  $I_{B2}$  affects the output by producing a voltage drop across  $R_1$ .



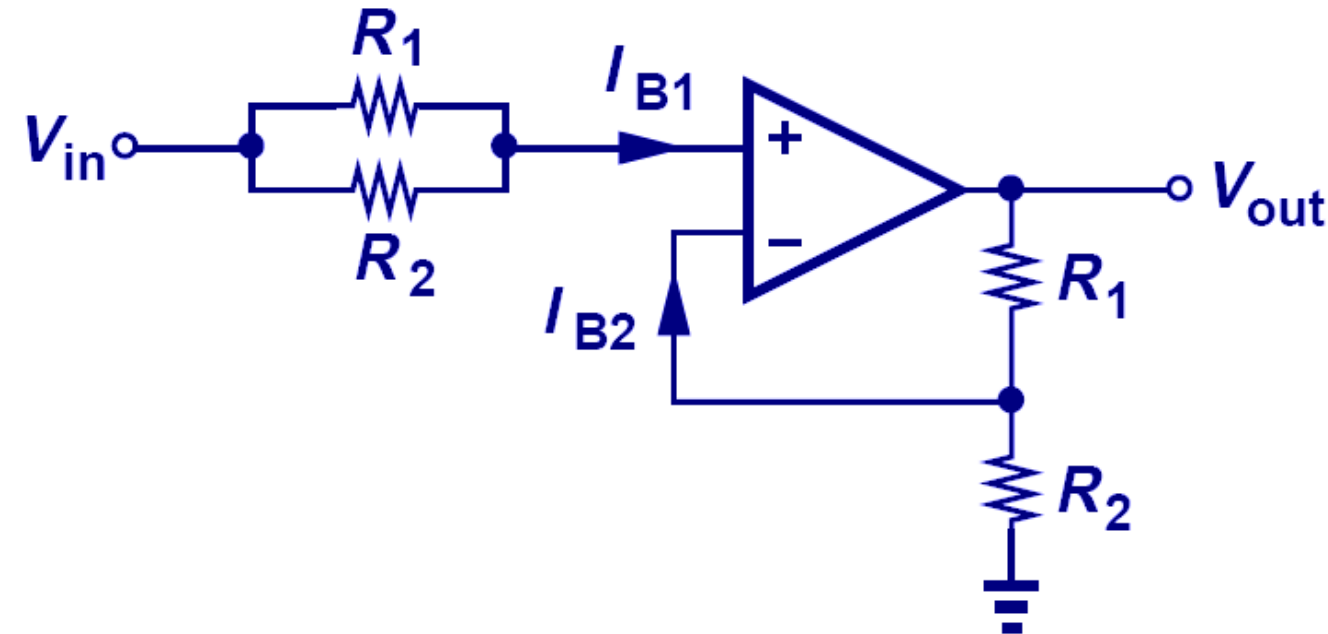
# Input Bias Current Cancellation



$$V_{out} = V_{corr} \left( 1 + \frac{R_1}{R_2} \right) + I_{B2} R_1$$

- We can cancel the effect of input bias current by inserting a correction voltage in series with the positive terminal.
- In order to produce a zero output,  $V_{corr} = -I_{B2}(R_1 || R_2)$ .

## Correction for $\beta$ Variation

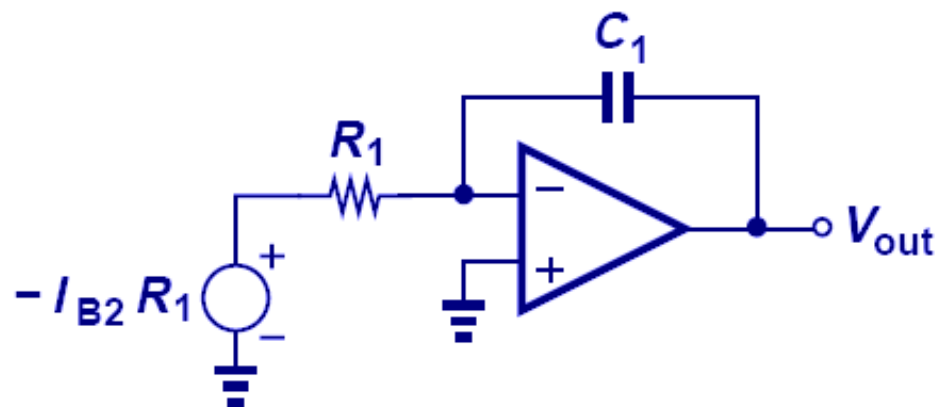
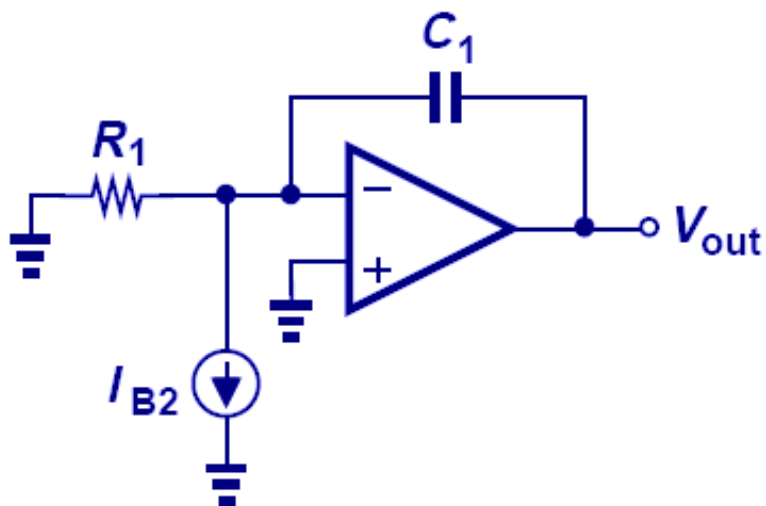


$$I_{B1} = I_{B2}$$

- Since the correction voltage is dependent upon  $\beta$ , and  $\beta$  varies with process, we insert a parallel resistor combination in series with the positive input. As long as  $I_{B1} = I_{B2}$ , the correction voltage can track the  $\beta$  variation.



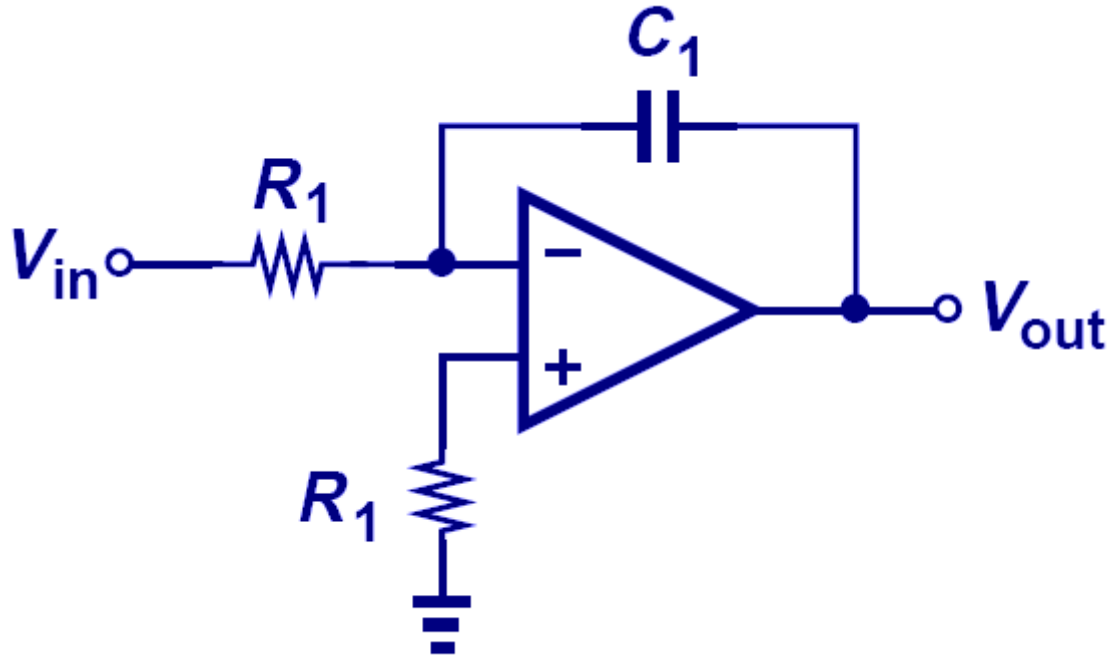
## Effects of Input Bias Currents on Integrator



$$V_{out} = -\frac{1}{R_1 C_1} \int (-I_{B2} R_1) dt$$

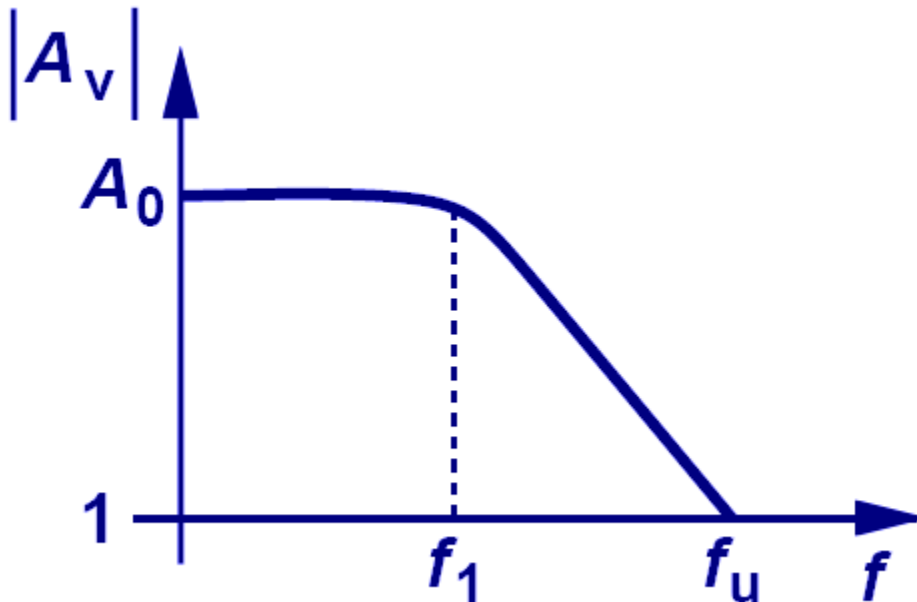
- Input bias current will be integrated by the integrator and eventually saturate the amplifier.

## Integrator's Input Bias Current Cancellation



- By placing a resistor in series with the positive input, integrator input bias current can be cancelled.
- However, the output still saturates due to other effects such as input mismatch, etc.

# Speed Limitation

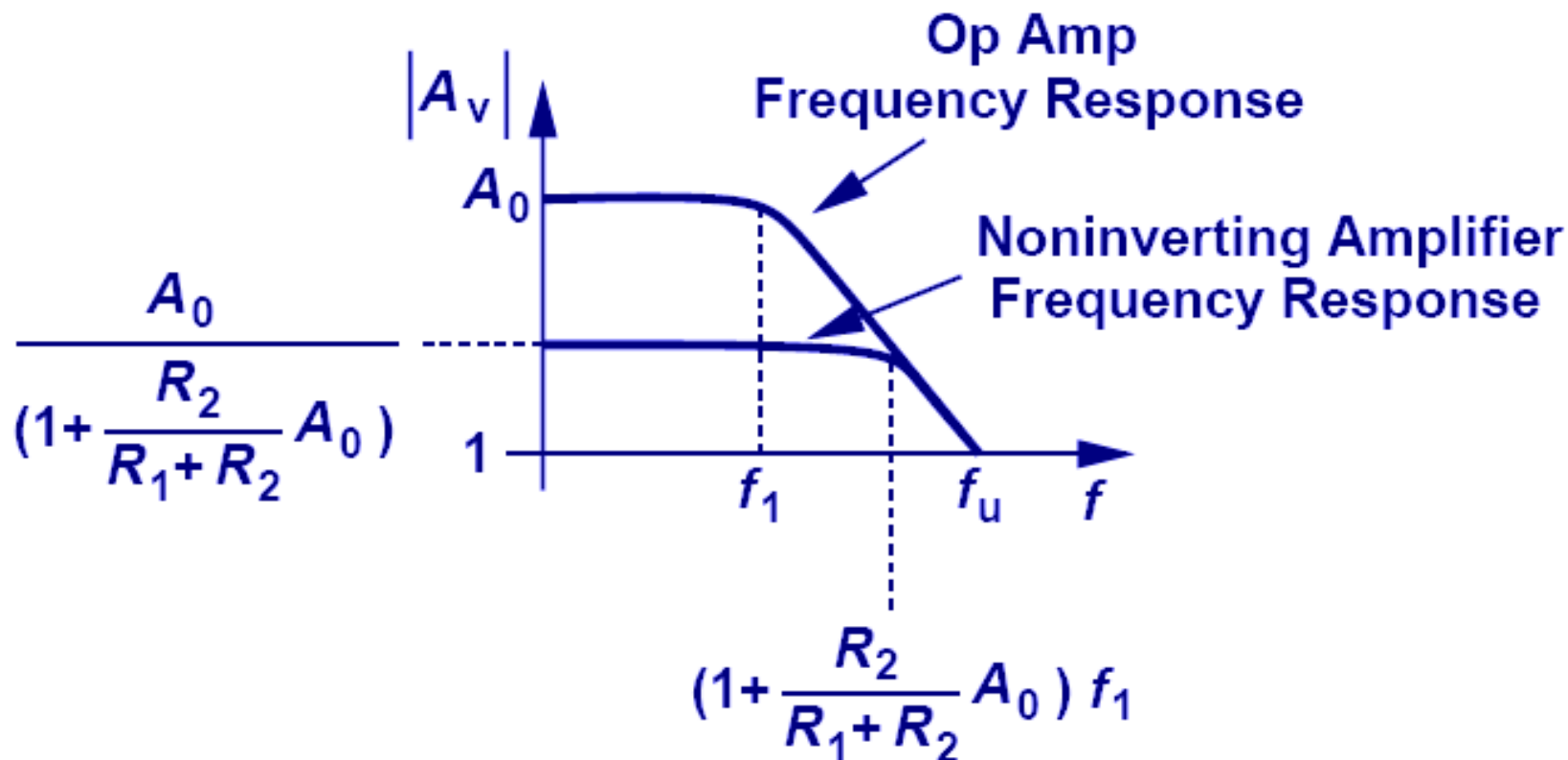


$$\frac{V_{out}}{V_{in1} - V_{in2}}(s) = \frac{A_0}{1 + \frac{s}{\omega_1}}$$

- Due to internal capacitances, the gain of op amps begins to roll off.

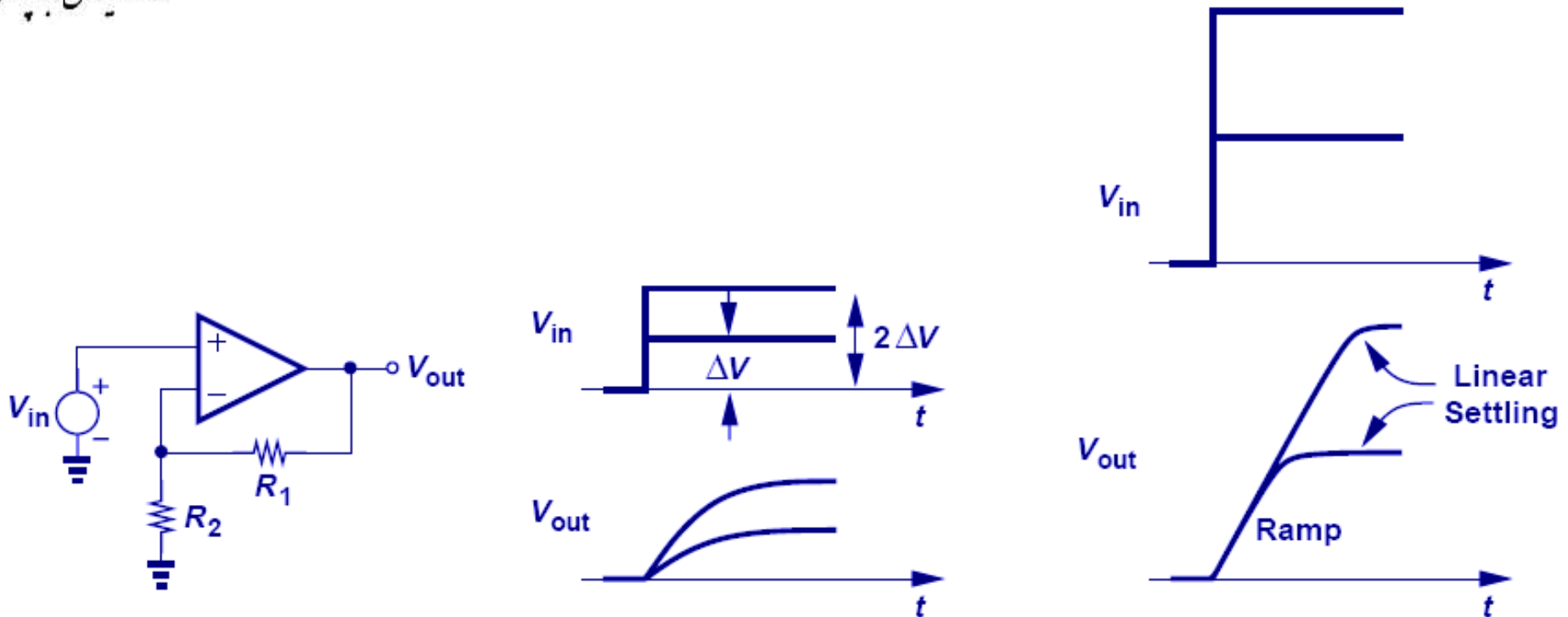


## Bandwidth and Gain Tradeoff



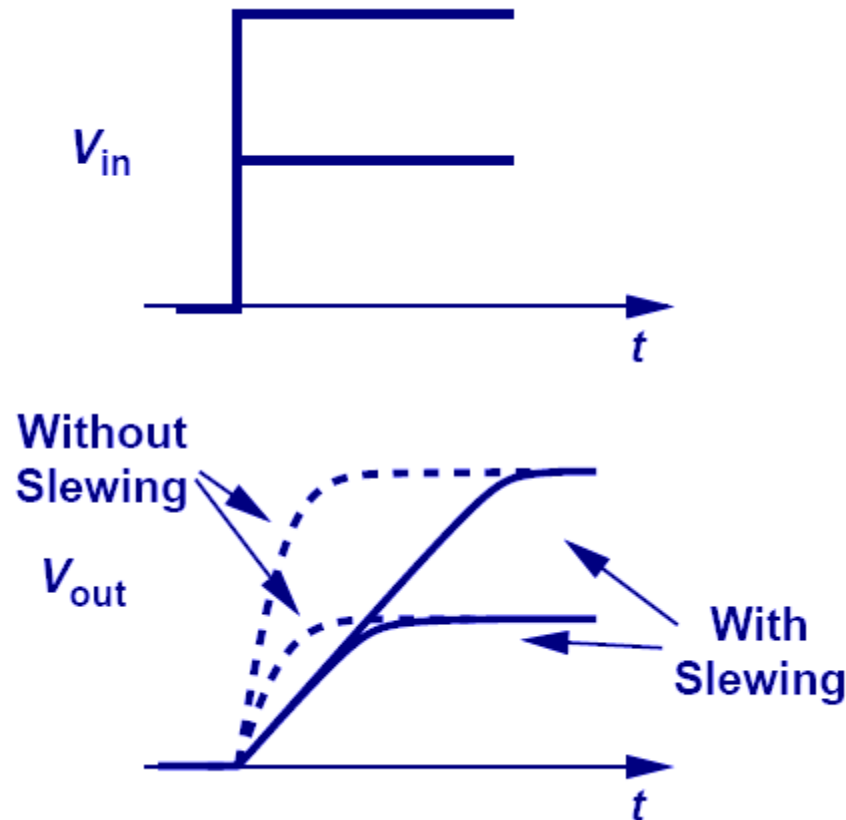
- Having a loop around the op amp (inverting, noninverting, etc) helps to increase its bandwidth. However, it also decreases the low frequency gain.

# Slew Rate of Op Amp



- In the linear region, when the input doubles, the output and the output slope also double. However, when the input is large, the op amp slews so the output slope is fixed by a constant current source charging a capacitor.
- This further limits the speed of the op amp.

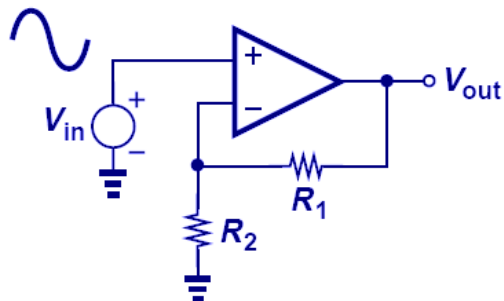
## Comparison of Settling with and without Slew Rate



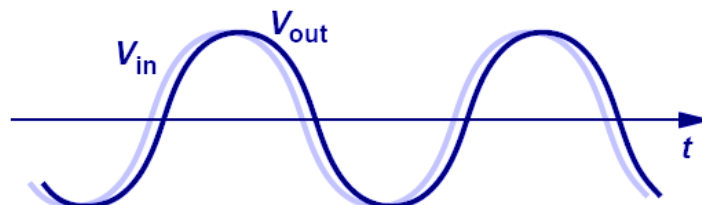
- As it can be seen, the settling speed is faster without slew rate (as determined by the closed-loop time constant).



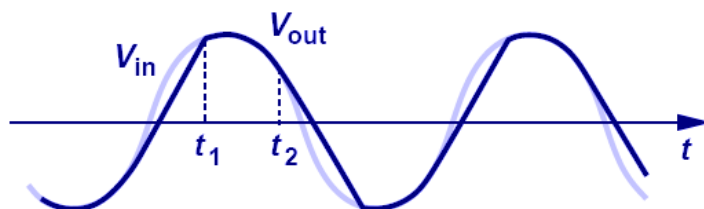
## Slew Rate Limit on Sinusoidal Signals



(a)



(b)

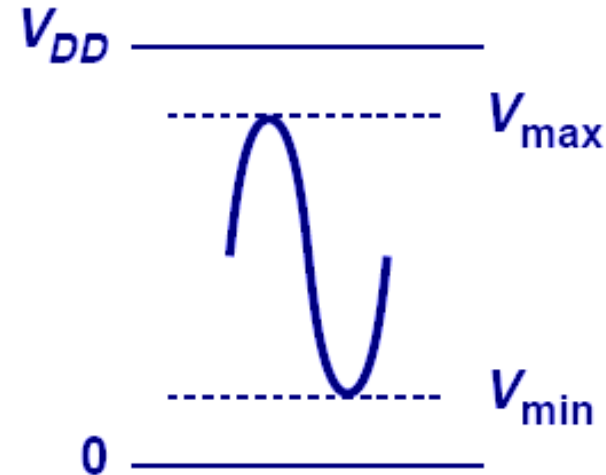
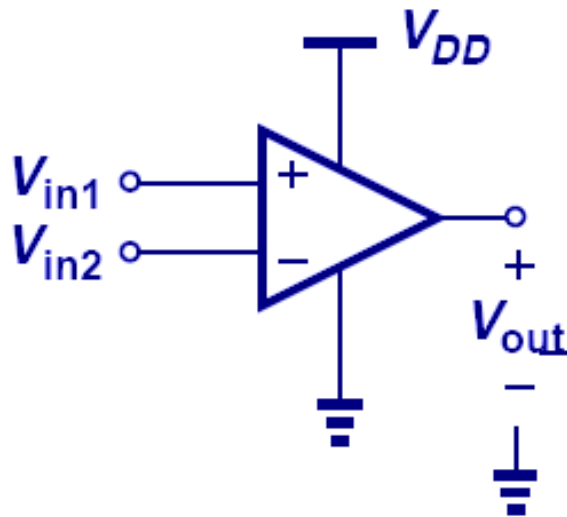


(c)

$$\frac{dV_{out}}{dt} = V_0 \left( 1 + \frac{R_1}{R_2} \right) \omega \cos \omega t$$

- As long as the output slope is less than the slew rate, the op amp can avoid slewing.
- However, as operating frequency and/or amplitude is increased, the slew rate becomes insufficient and the output becomes distorted.

# Maximum Op Amp Swing

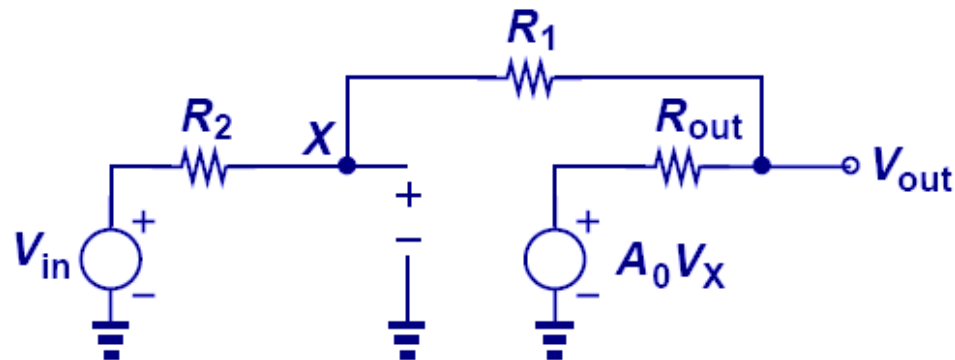
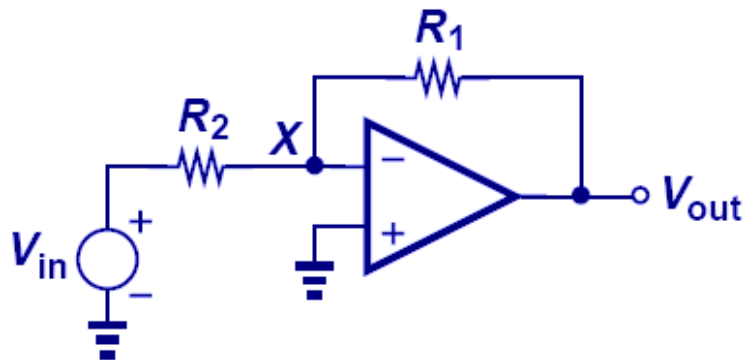


$$V_{out} = \frac{V_{max} - V_{min}}{2} \sin \omega t + \frac{V_{max} + V_{min}}{2} \quad \omega_{FP} = \frac{SR}{\frac{V_{max} - V_{min}}{2}}$$

- To determine the maximum frequency before op amp slews, first determine the maximum swing the op amp can have and divide the slew rate by it.



## Nonzero Output Resistance



$$\frac{v_{out}}{v_{in}} = -\frac{R_1}{R_2} \frac{A_0 - \frac{R_{out}}{R_1}}{1 + \frac{R_{out}}{R_2} + A_0 + \frac{R_1}{R_2}}$$

- In practical op amps, the output resistance is not zero.
- It can be seen from the closed loop gain that the nonzero output resistance increases the gain error.

## Design Examples

- **Many design problems are presented at the end of the chapter to study the effects of finite loop gain, restrictions on peak to peak swing to avoid slewing, and how to design for a certain gain error.**

