



Fundamentals of Microelectronics II

فصل ۹- طبقه کاسکود و آیینه های جریان

(قسمت دوم- آیینه جریان)

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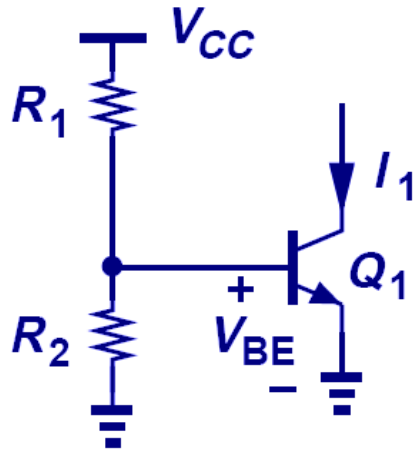
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➤ 9.2 Current Mirrors

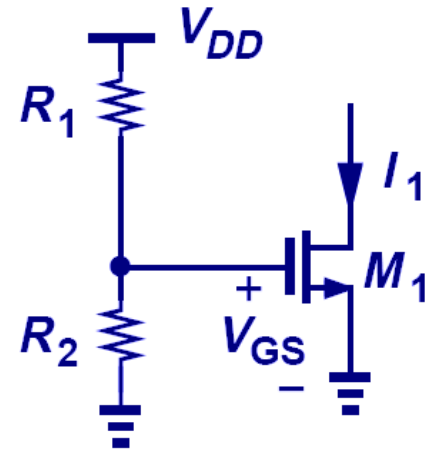


دانشگاه پشاور

Temperature and Supply Dependence of Bias Current



(a)



(b)

$$V_{BE} = V_T \ln \frac{I_C}{I_S}$$

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$R_2 V_{CC} / (R_1 + R_2) = V_T \ln(I_1 / I_S)$$

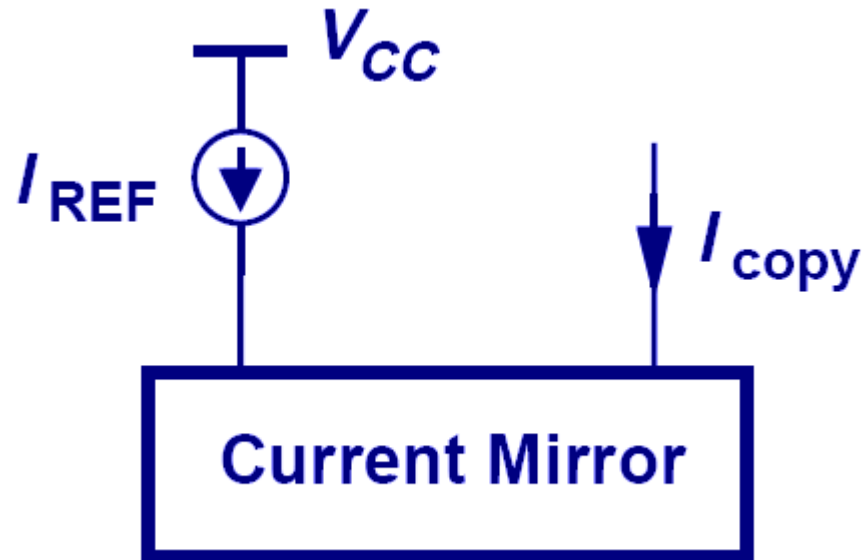
$$I_1 = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} \left(\frac{R_2}{R_1 + R_2} V_{DD} - V_{TH} \right)^2$$

➤ Since V_T , I_S , μ_n , and V_{TH} all depend on temperature, I_1 for both bipolar and MOS depends on temperature and supply.



دانشگاه بلوچستان

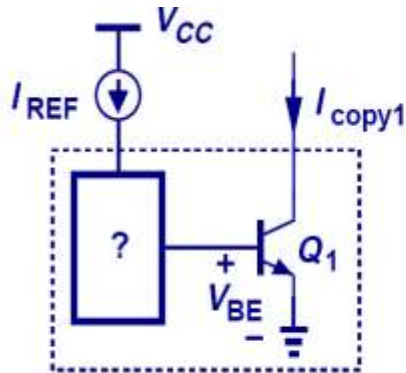
Concept of Current Mirror



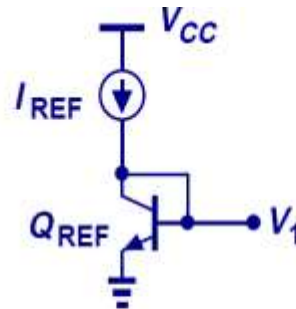
- The motivation behind a **current mirror** is to sense the current from a “**golden current source**” and **duplicate** this “golden current” to other locations.



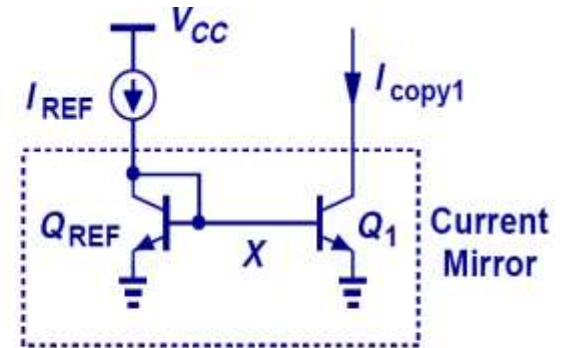
Bipolar Current Mirror Circuitry



(a)



(b)



(c)

$$I_C = I_S \exp \frac{V_{BE}}{V_T}$$

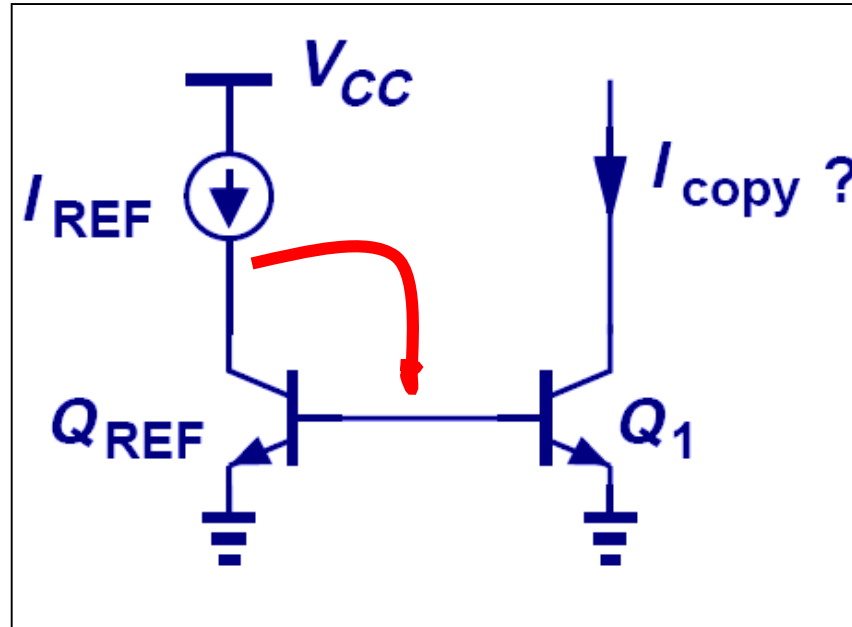
$$V_{BE} = V_T \ln \frac{I_C}{I_S}$$

$$I_{copy} = \frac{I_{S1}}{I_{S,REF}} I_{REF}$$

➤ The diode-connected Q_{REF} produces an output voltage V_1 that forces $I_{copy1} = I_{REF}$, if $Q_1 = Q_{REF}$.



Bad Current Mirror (Example I)

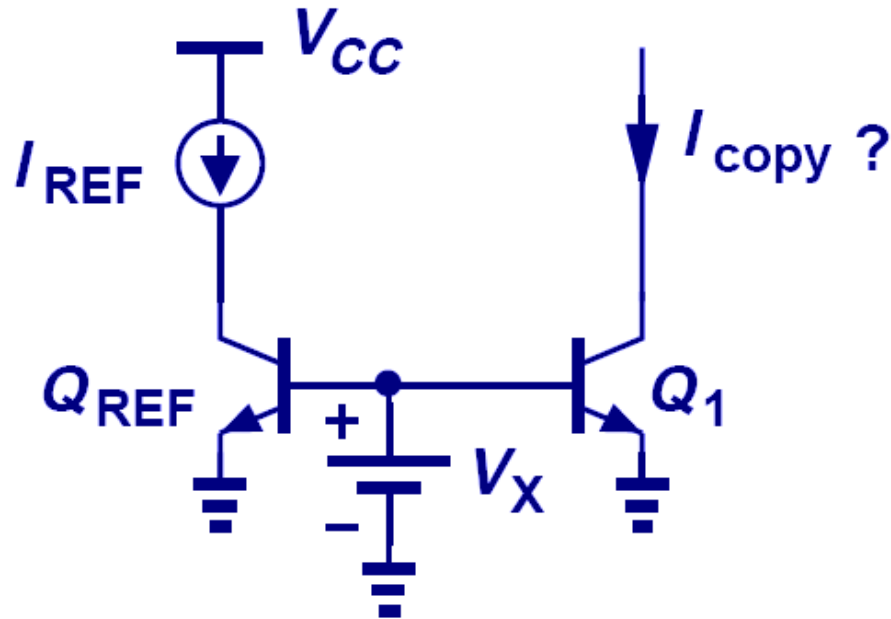


$$I_{copy} = 0 ???$$

- Without shorting the collector and base of Q_{REF} together, there will not be a path for the **base currents** to flow, therefore, **I_{copy} is zero.**



Bad Current Mirror (Example II)

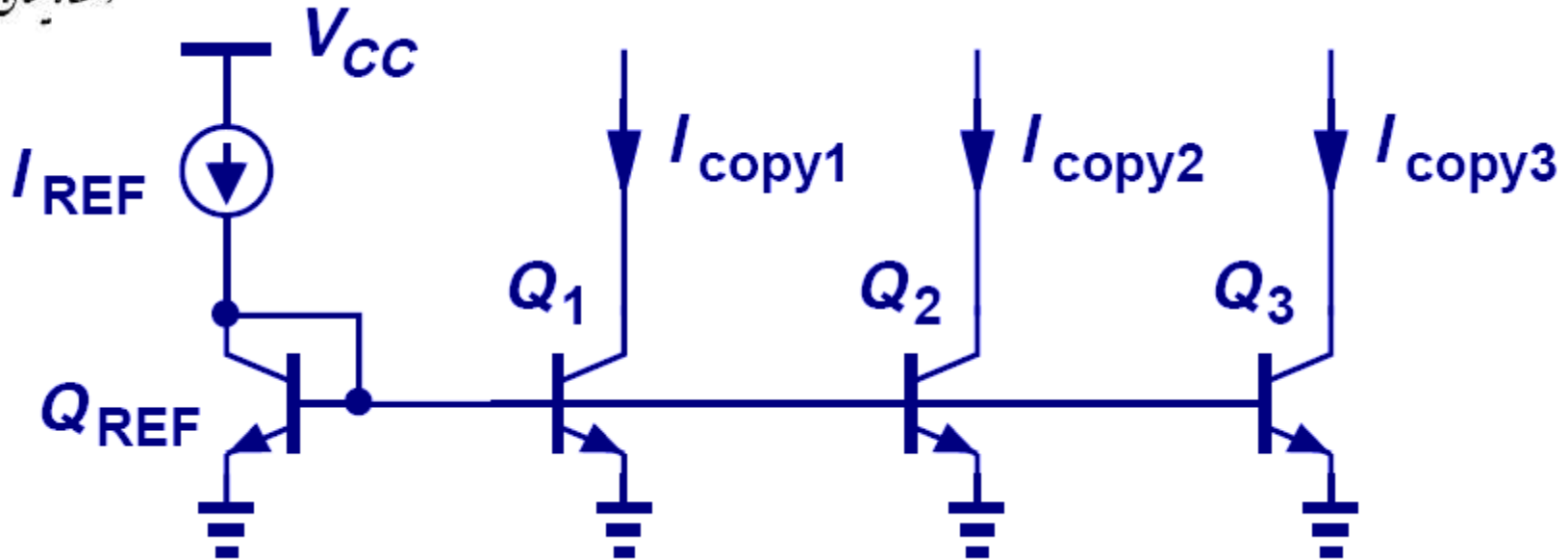


$$I_{Copy} = I_{S1} \exp \frac{V_X}{V_T}$$

- Although a path for base currents exists, this technique of biasing is **no better than resistive divider**.



Multiple Copies of I_{REF}



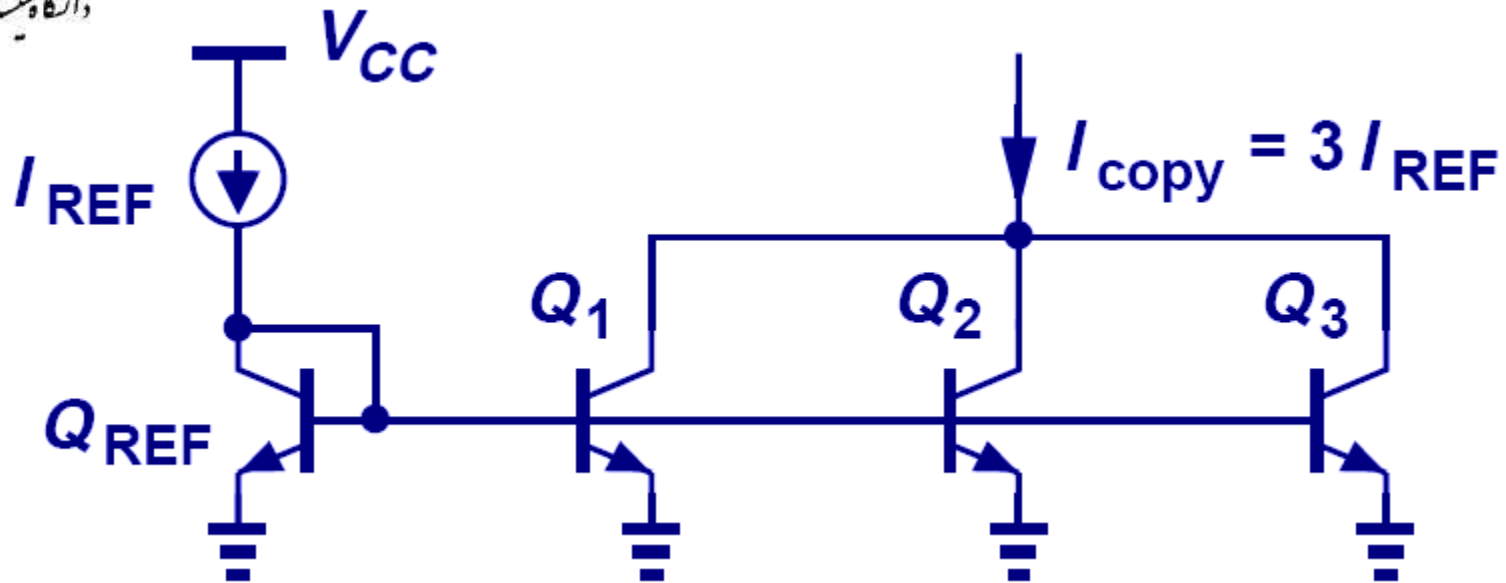
$$I_{copy,j} = \frac{I_{S,j}}{I_{S,REF}} I_{REF}$$

- Multiple copies of I_{REF} can be generated at different locations by simply applying the idea of current mirror to more transistors.



دانشگاه پشاور

Current Scaling



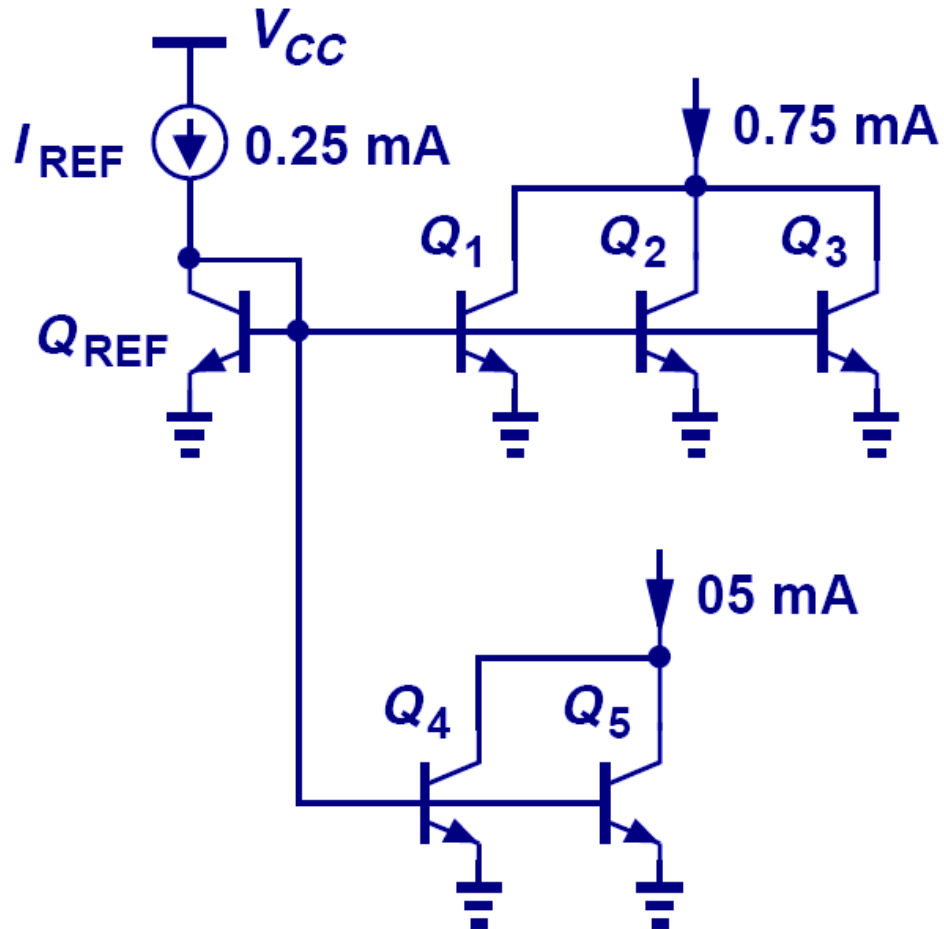
$$I_{copy,j} = n I_{REF}$$

- By scaling the emitter area of Q_j n times with respect to Q_{REF} , $I_{copy,j}$ is also n times **larger** than I_{REF} . This is equivalent to placing n unit-size transistors in parallel.



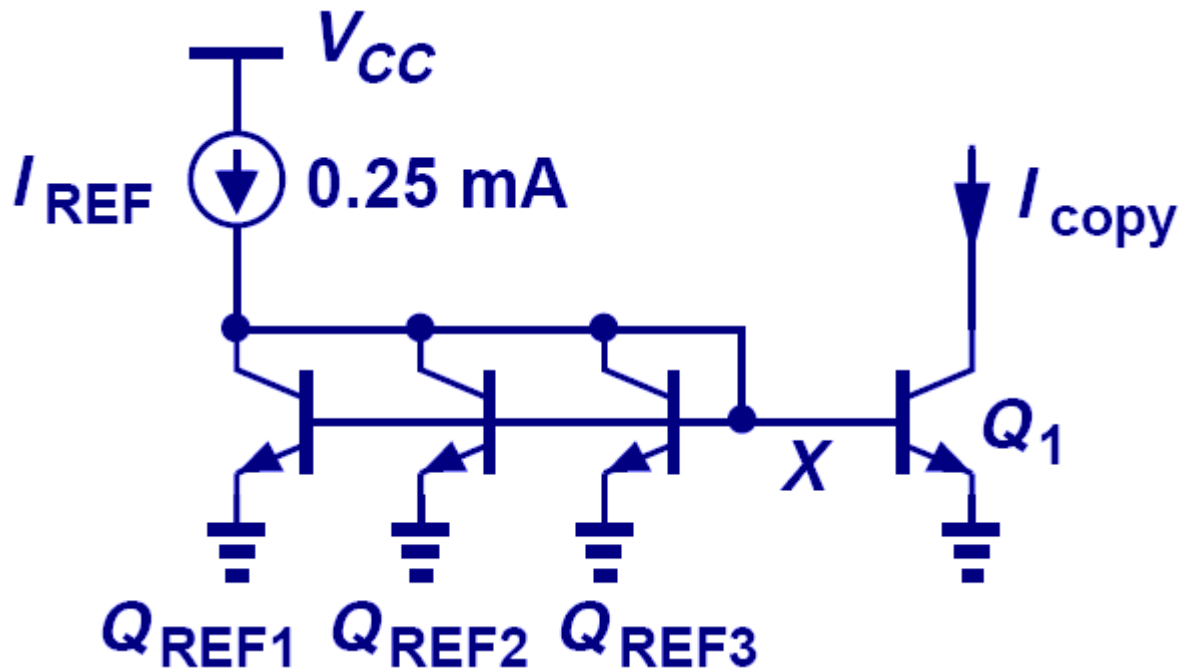
دانشگاه بلوچستان

Example: Scaled Current





Fractional Scaling



$$I_{copy} = \frac{1}{3} I_{REF}$$

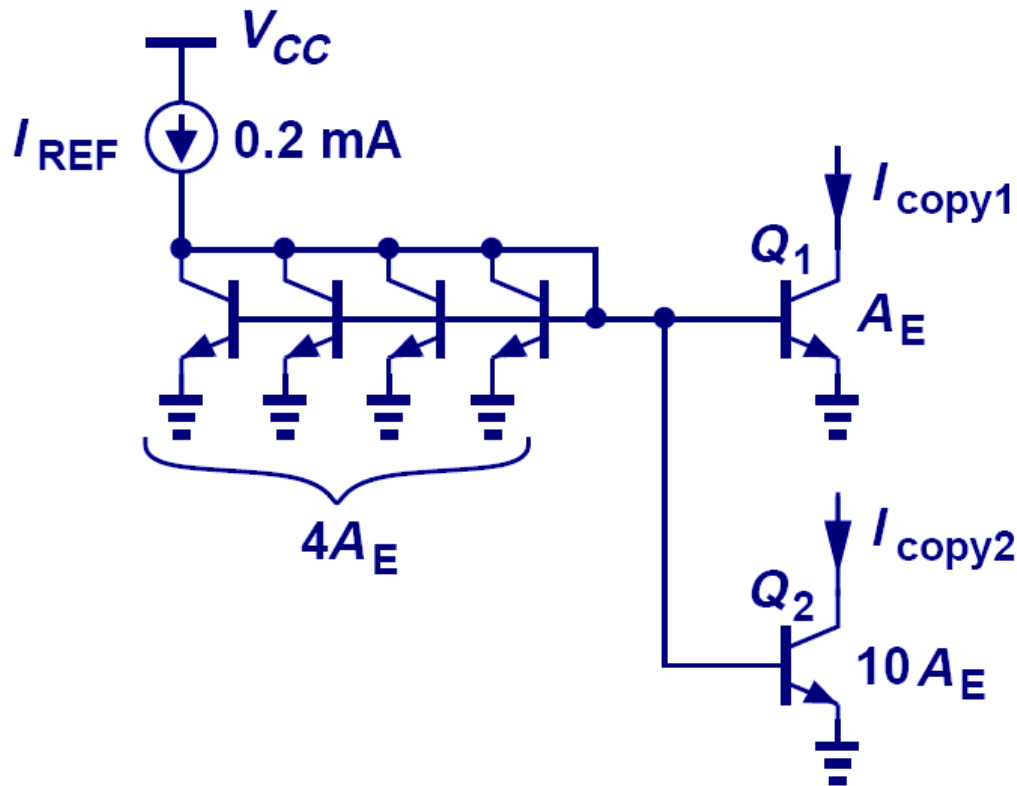
- A fraction of I_{REF} can be created on Q_1 by scaling up the emitter area of Q_{REF} .

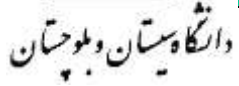


دانشگاه بلوچستان

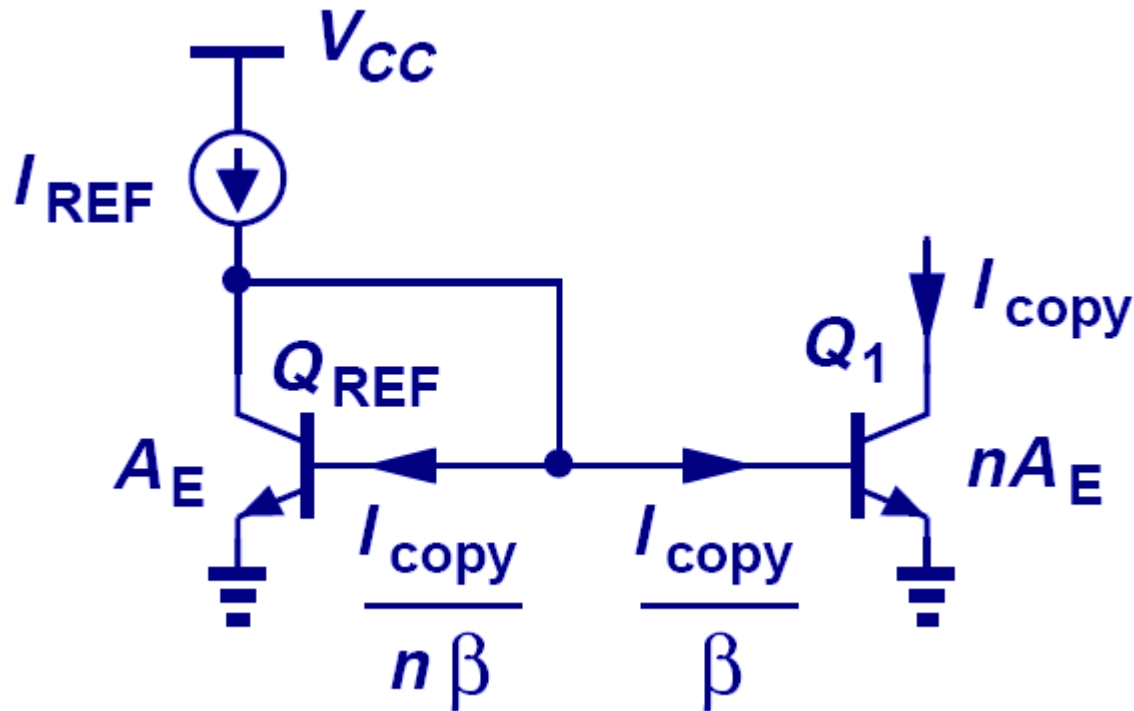
Example: Different Mirroring Ratio

- Using the idea of current scaling and fractional scaling, I_{copy2} is 0.5mA and I_{copy1} is 0.05mA respectively.
- All coming from a source of 0.2mA.





Mirroring Error Due to Base Currents

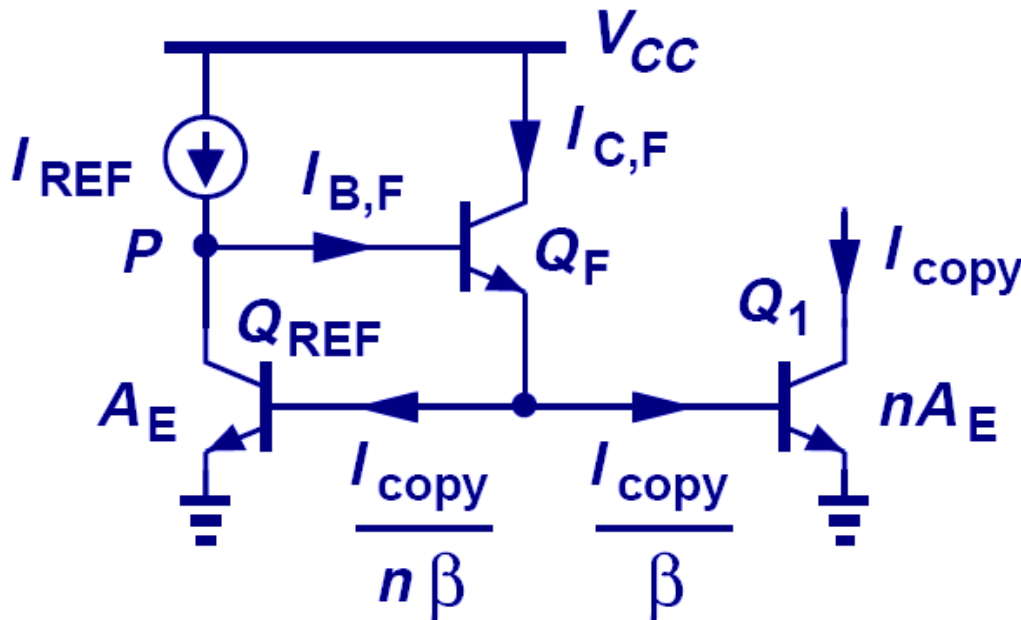


$$I_{copy} = nI_{C,REF}$$

$$I_{copy} = \frac{nI_{REF}}{1 + \frac{1}{\beta}(n+1)}$$



Improved Mirroring Accuracy



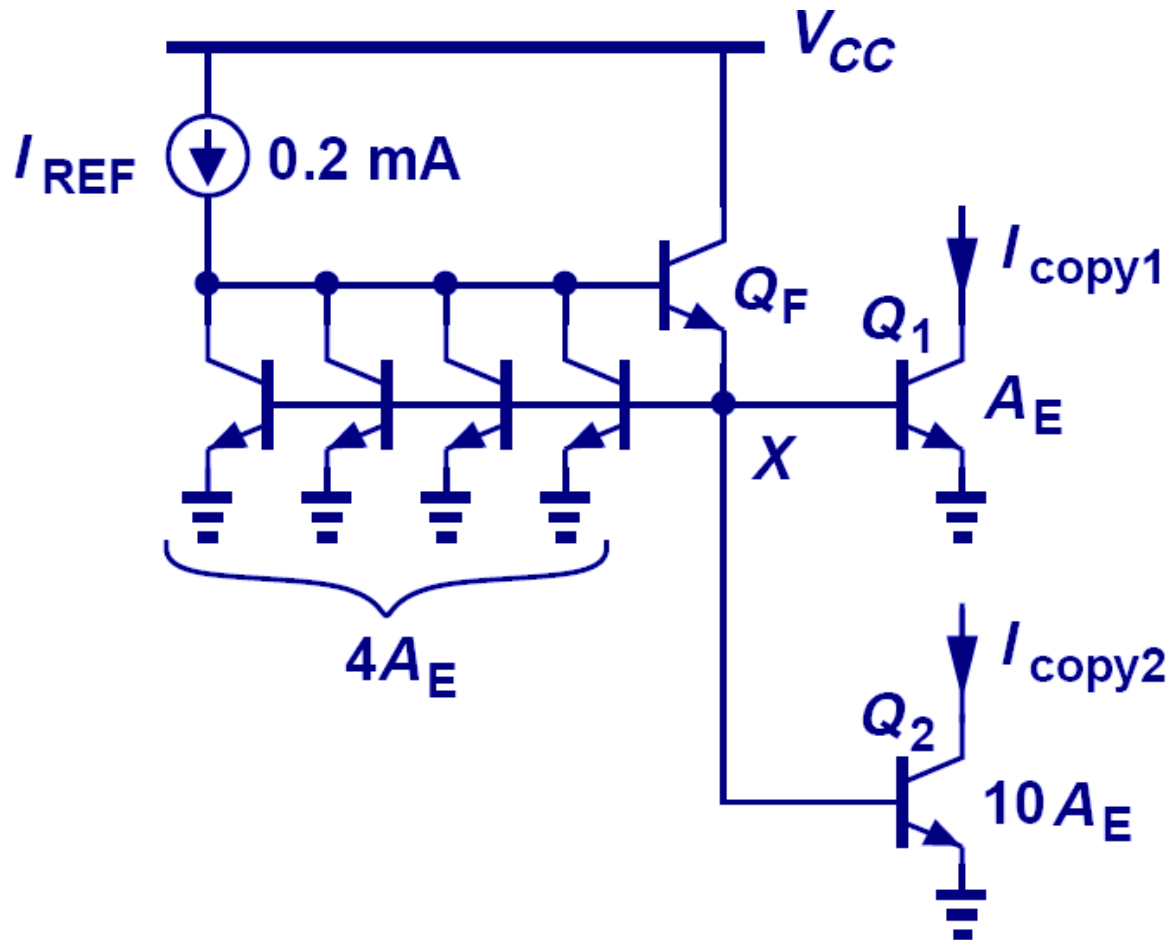
$$I_{copy} = \frac{nI_{REF}}{1 + \frac{1}{\beta^2}(n+1)}$$

- Because of Q_F , the base currents of Q_{REF} and Q_1 are mostly supplied by Q_F rather than I_{REF} . Mirroring error is reduced β times.



دانشگاه موهج

Example: Different Mirroring Ratio Accuracy



$$I_{copy,2} = 10I_{copy,1}$$

$$I_{C,REF} = 4I_{copy1}$$

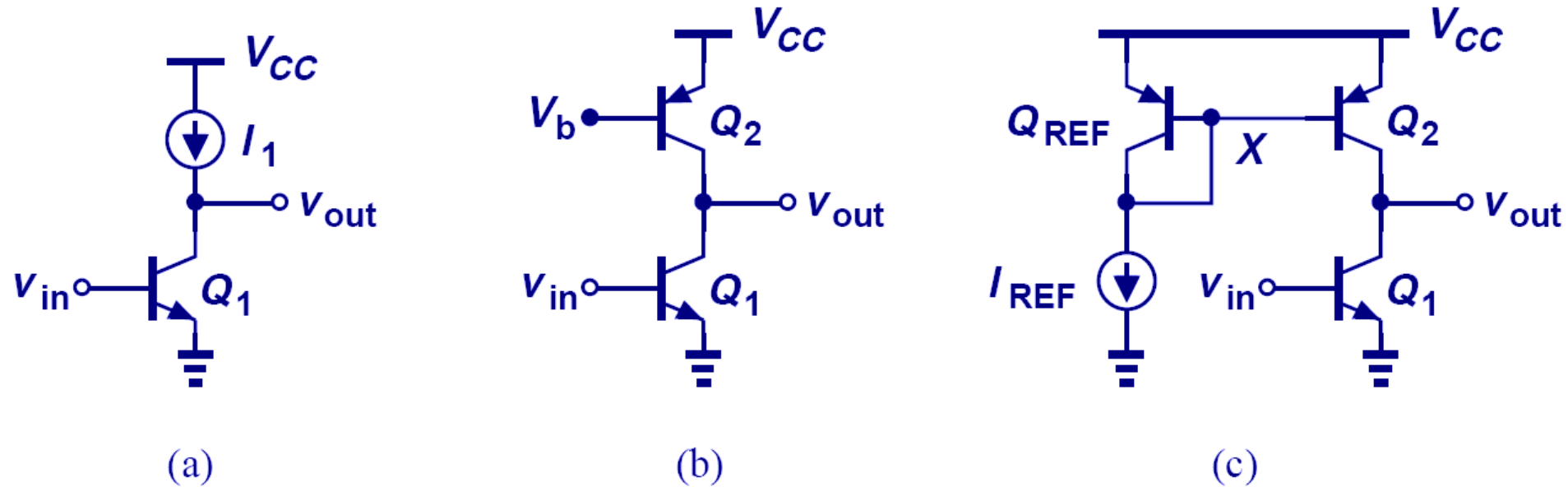
$$I_{copy1} = \frac{I_{REF}}{4 + \frac{15}{\beta^2}}$$

$$I_{copy2} = \frac{10I_{REF}}{4 + \frac{15}{\beta^2}}$$



دانشگاه پشاور
University of Peshawar

PNP Current Mirror

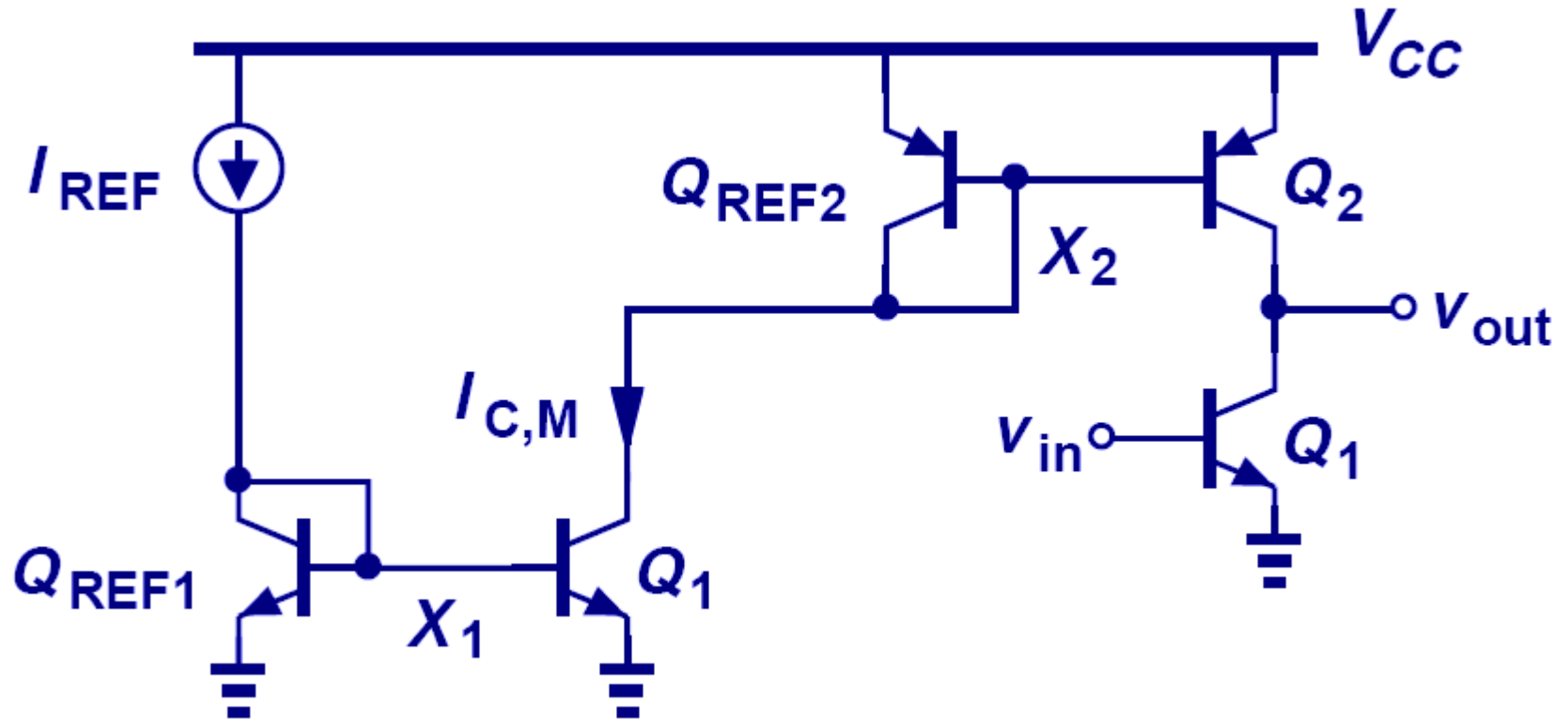


➤ PNP current mirror is used as a current source load to an NPN amplifier stage.



دانشگاه موهج

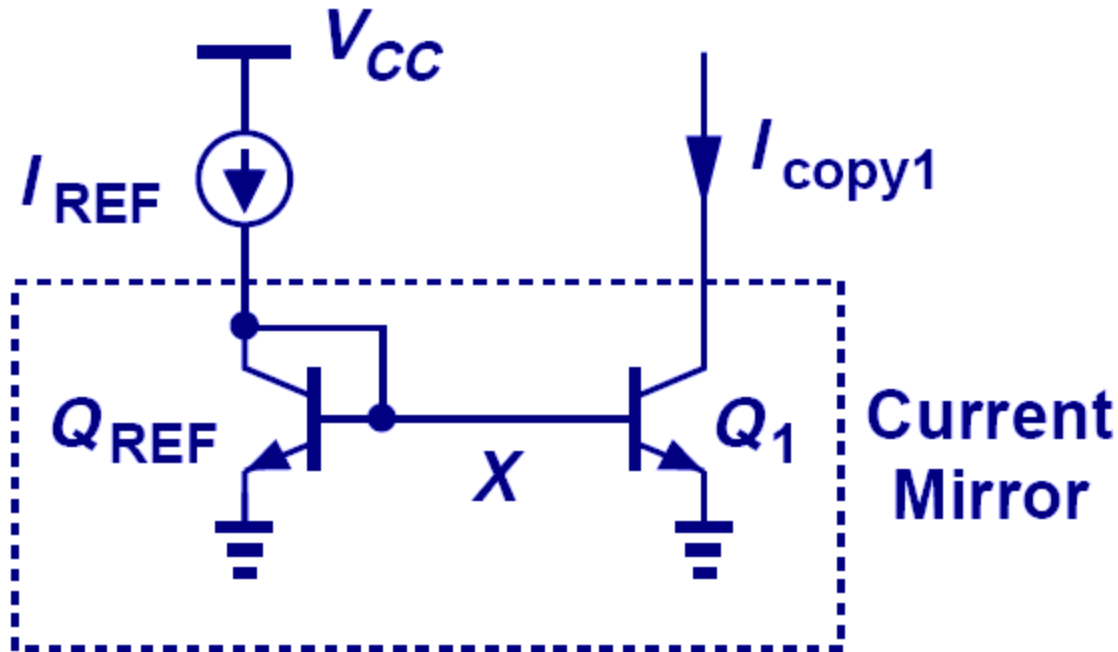
Generation of I_{REF} for PNP Current Mirror





دانشگاه گجرات

Example: Current Mirror with Discrete Devices

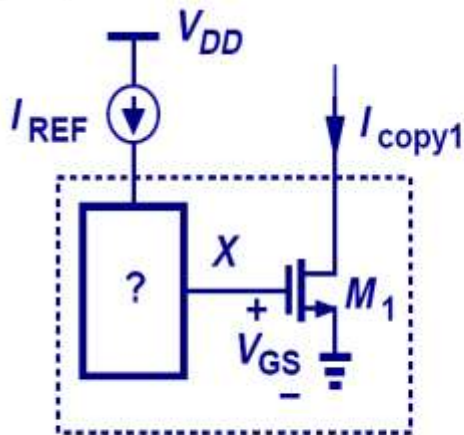


- Let Q_{REF} and Q_1 be **discrete NPN devices**.
- I_{REF} and I_{copy1} can vary in large magnitude due to **I_S mismatch**.

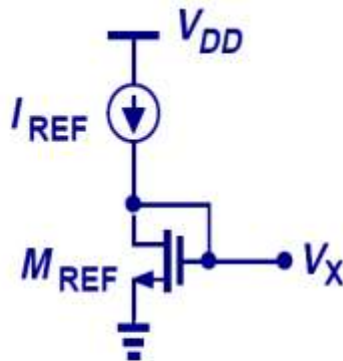


دانشگاه پشاور

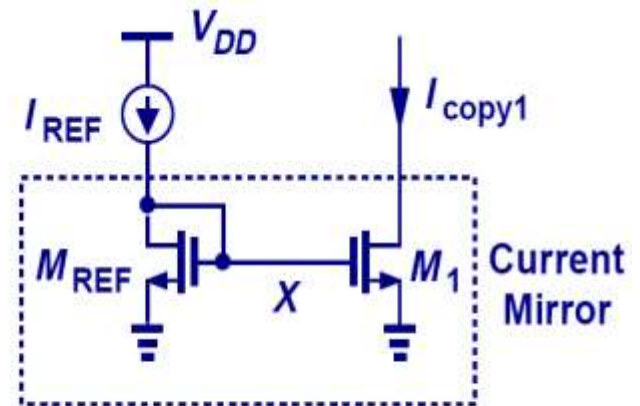
MOS Current Mirror



(a)



(b)



(c)

$$I_{D,REF} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right)_{REF} (V_X - V_{TH})^2$$
$$I_{copy} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L} \right)_1 (V_X - V_{TH})^2,$$

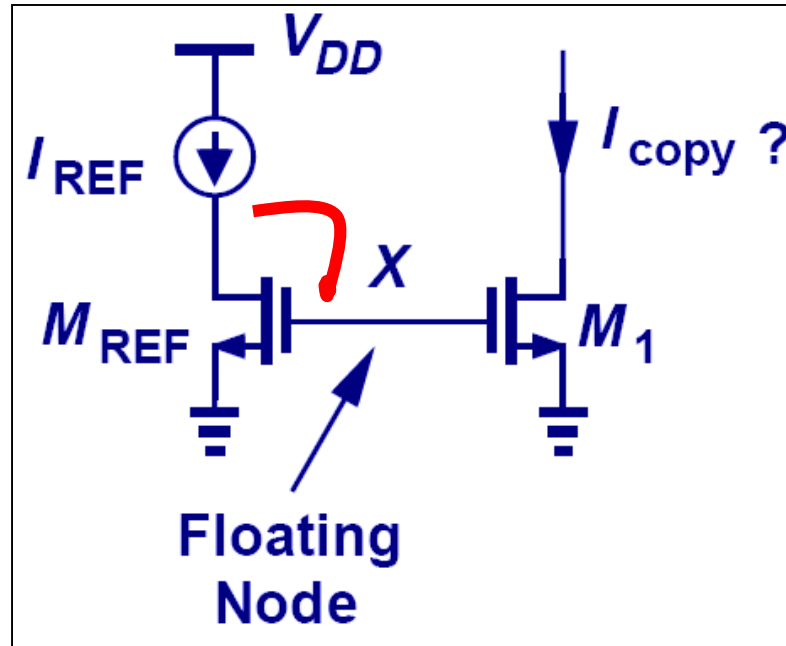
$$I_{copy} = \frac{\left(\frac{W}{L} \right)_1}{\left(\frac{W}{L} \right)_{REF}} I_{REF},$$

➤ The same concept of current mirror can be applied to MOS transistors as well.



دانشگاه پشاور

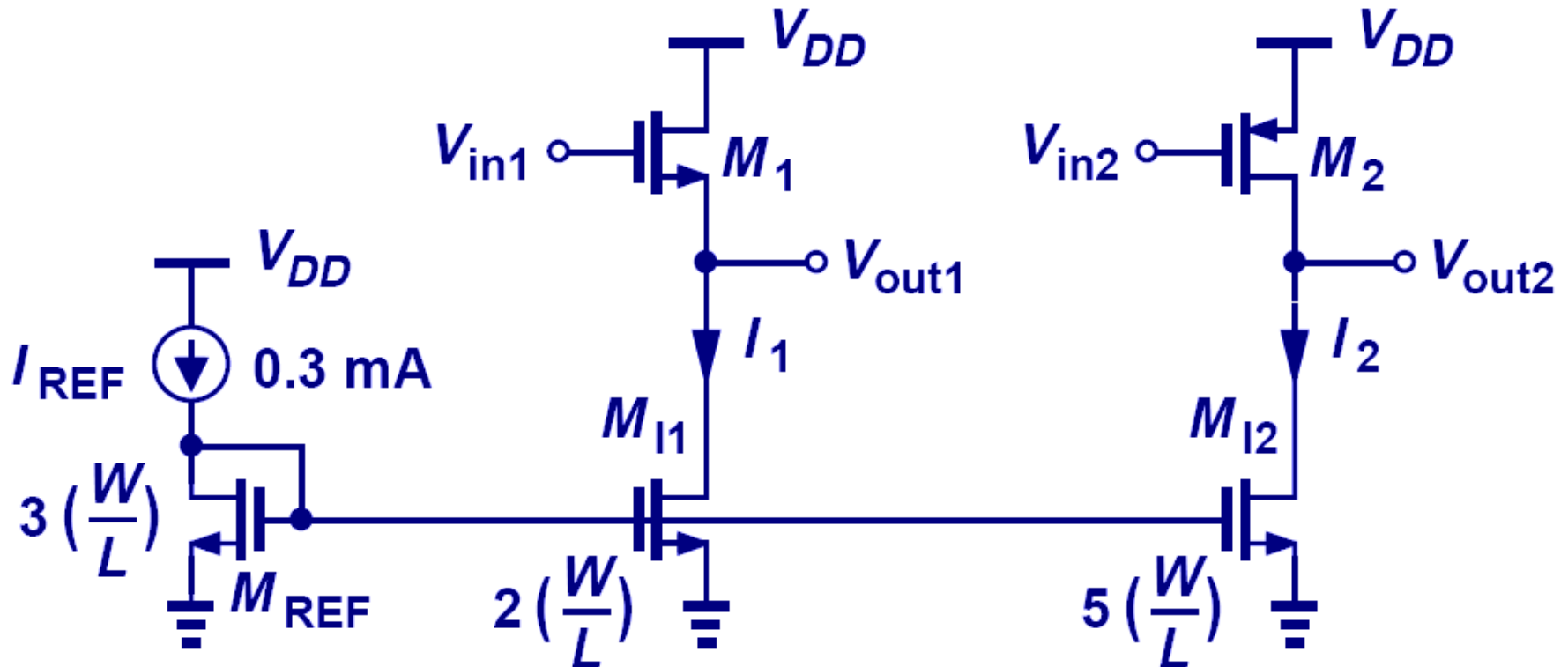
Bad MOS Current Mirror Example



- This **is not** a current mirror since the relationship between V_X and I_{REF} is not clearly defined.
- The only way to clearly define V_X with I_{REF} is to use a diode-connected MOS since it provides square-law I-V relationship.



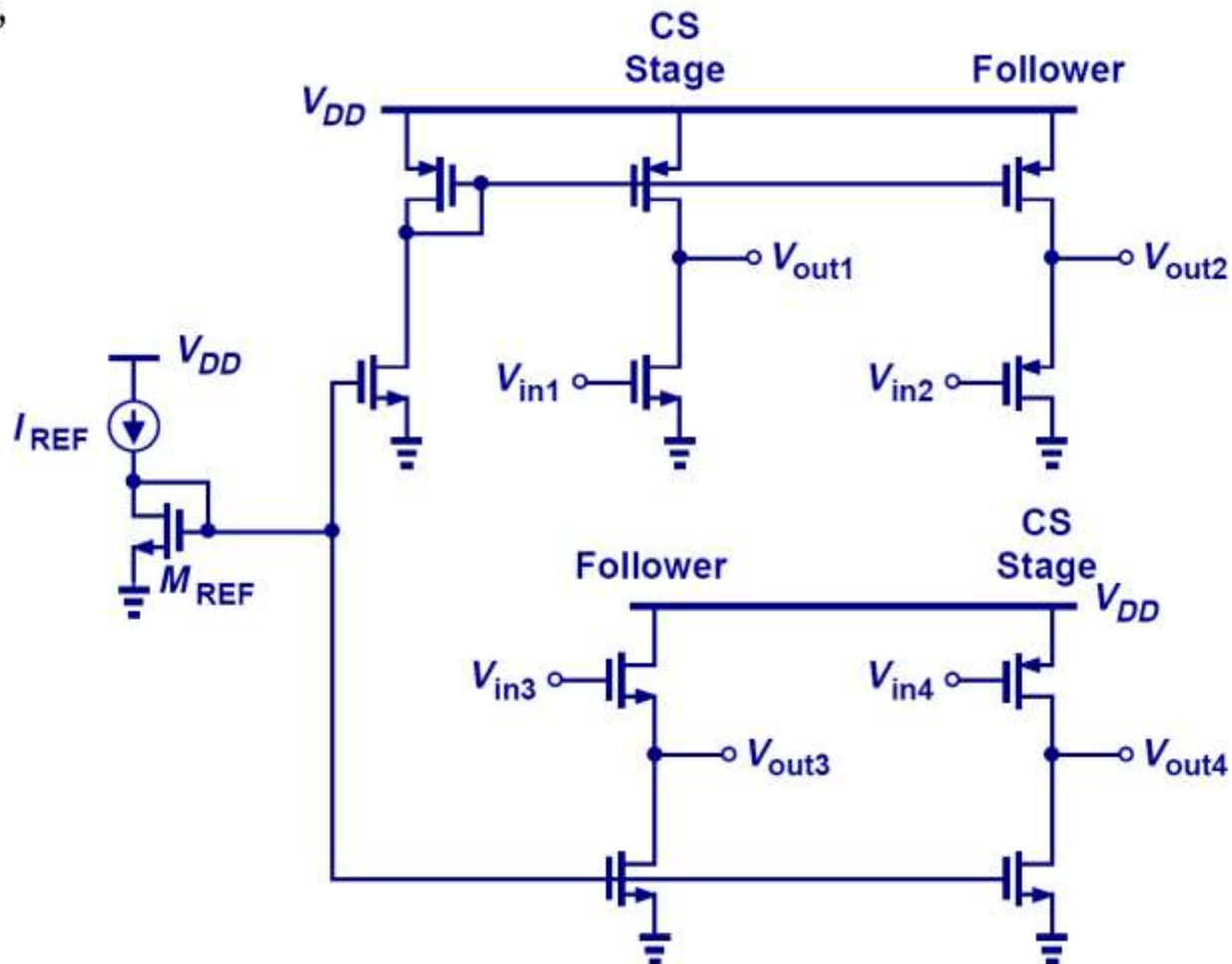
Example: Current Scaling



- Similar to their bipolar counterpart, MOS current mirrors can also scale I_{REF} up or down ($I_1 = 0.2 \text{ mA}$, $I_2 = 0.5 \text{ mA}$).



CMOS Current Mirror



- The idea of combining NMOS and PMOS to produce CMOS current mirror is shown above.